#### **Curriculum Book**

and

#### **Assessment and Evaluation Scheme**

Based on

#### **Outcome Based Education (OBE)**

and Choice-Based Credit System(CBCS)

in

M.Sc. Mathematics Program

**2Year Degree Program** 

Revised as on 01 August 2023 Applicable w.e.f. Academic Session 2023-24



#### **AKS University**

Satna 485001, Madhya Pradesh, India

Faculty of Basic Science Department of Mathematics



# Faculty of Basic Science Department of Mathematics Curriculum & Syllabus of M.Sc. Mathematics program (Revised as on 01 August 2023)

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Department of Mathematics

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Professor B.A. Chopade Vice - Chancellor AKS University Satna, 485001 (M.P.)



(Revised as on 01 August 2023)

#### **Forwarding**

I am thrilled to observe the updated curriculum of the Department of Mathematics for M.Sc. Mathematics Program, which seamlessly integrates the most recent technological advancements and adheres to the guidelines set forth by UGC. The revised curriculum also thoughtfully incorporates the directives of NEP-2020 and the Sustainable Development Goals.

The alignment of course outcomes(COs), Programme Outcome (POs) and Programme specific outcomes(PSOs) has been intricately executed, aligning perfectly with the requisites of NEP-2020 and NAAC standards. I hold the belief that this revised syllabus will significantly enhance the skills and employability of our students.

With immense satisfaction, I hereby present the revised curriculum for the *M.Sc. Mathematics* program for implementation in the upcoming session.

ER. Anant Soni Pro Chancellor & Chairman AKS University, Satna

01 August 2023



## Faculty of Basic Science Department of Mathematics Curriculum & Syllabus of M.Sc. Mathematics program (Povised as on 01 August 2022)

(Revised as on 01 August 2023)

#### From the Desk of the Vice-Chancellor

AKSUniversityiscurrentlyundergoingaprocesstorevampitscurriculumintoanoutcomebased approach, with the aim of enhancing the teaching and learning process. The foundation of quality of quality education lies in the implementation of a curriculum that aligns with both societal and industrial needs, focusing on relevant outcomes. This entails dedicated and inspired



Hence, it is of utmost importance to begin this endeavor by crafting an outcome-based curriculum in collaboration with academia and industry experts. This curriculum design should be informed by the latest technological advancements, market demands, the guidelines outlined in the National Education Policy (NEP) of 2020, and sustainable goals.

I'm delighted to learn that the revised curriculum has been meticulously crafted by the Mathematics Department, in consultation with an array of experts from the different universities of the mathematics research institutes and academia. This curriculum effectively integrates the principles outlined in the NEP-2020 guidelines, as well as sustainable goals. It also adeptly incorporates the latest advancements in the area of Mathematic.

Our University is known for conducting its academic programmes and examinations as per schedule. The credit based semester system at the postgraduate level and the choice based credit system for the two year (four semesters) Master's degree programme are working well.

To enhance student's skills, the curriculum integrates the research skills, research and progress. This well-rounded approach ensures that students receive a comprehensive education, fostering their skill development and preparing them for success in the field of Mathematics.

I am confident that the updated curriculum for Mathematics will not only enhance students' technical skills but also contribute significantly to their employability. During the process of revising the curriculum, I am pleased to observe that the mathematics department has diligently adhered to the guidelines provided by the UGC. Additionally, they have maintained a total credit requirement of Mathematics for M.Sc. Mathematics program.

It's worth noting that curriculum revision is an ongoing and dynamic process, designed to address the continuous evolution of technological advancements and both local and global concerns. This ensures that the curriculum remains responsive and attuned to the changing landscape of education and industry.

AKS University warmly invites input and suggestions from industry experts and technocrats and Alumni students to enhance the curriculum and make it more student-centered. Your valuable insights will greatly contribute to shaping an education that best serves the needs and aspirations of our students.

AKS University, Satna 01 August 2023 Professor B. A. Chopade Vice- Chancellor



(Revised as on 01 August 2023)

**Preface** 

As par to four commitments to ongoing enhancement, the Department of Mathematics consistently reviews and updates its M.Sc. Mathematics program curriculum every two years. Through this process, we ensure that the curriculum remains aligned with the latest technological advancements, as well as local and global industrial and social demands.

During this procedure, the existing curriculum for the M.Sc. Mathematics Program undergoes evaluation by a panel of technocrats, industry specialists, and academics. Following meticulous scrutiny, the revised curriculum has been formulated and is set to be implemented starting from August 01,2023. This implementation is contingent upon the endorsement of the curriculum by the University's Board of Studies and Governing Body.

This curriculum closely adheres to the UGC model syllabus distributed in May 2023. It seamlessly integrates the guide lines set forth by the Ministry of Higher Education, Government of India, through NEP- 2020, as well as the principles of Sustainable Development Goals. In order to foster the holistic skill development of students, a range of practical activities, including Hands-On Training, Project planning and execution, Report Writing, Seminars, and Industrial On-Job Training, have been incorporated. Furthermore, in alignment with UGC's directives, the total credit all allocation on for the M.Sc. Mathematics program is capped at 87 credits.

This curriculum is enriched with course components in alignment with UGC guidelines, encompassing various disciplines such as ,Core Program Courses: 60 credits, Program Elective Courses: 04 credits, Open Electives: 04 credits, Research Courses: 19 credits.

To ensure a comprehensive learning experience, detailed evaluations schemes and rubrics have also been meticulously provided.

For each course, a thorough mapping of Course Outcomes, Program Outcomes and Programme Specific Out comes has been undertaken. As the courses syllabus is being meticulously developed, various elements such as session outcomes, laboratory instruction, classroom instruction, self-learning activities, assignments, and mini projects are meticulously outlined.

We hold the belief that this dynamic curriculum will undoubtedly enhance independent thinking, skills, and overall employability of the students.

Dr. R.S. Nigam Dean, Faculty of Basic Science AKS University, Satna

01August2023



(Revised as on 01 August 2023)

#### Introduction

The Department of Mathematics was established in the academic year 2017. Department of Mathematics is a diverse and vibrant academic unit, of AKS University, consisting of expertise in Mathematics that offers a wide variety of courses and degree options in Pure Mathematics and Applied Mathematics at the Bachelors, Masters, and Ph.D. levels. Department of Mathematics is engaged in outstanding research in Pure and Applied Mathematics.

The department provides opportunities for the students to choose their careers in education and research in various fields of Mathematics. Department has striven to set high standards of teaching.. Graduates of Mathematics Department are distinctively placed in reputed institutions and organizations. It has been the cherished goal of the Department to inculcate in the students a desire to excel, to demonstrate originality and to develop a sense of responsibility towards the society. Accordingly, the Department continuously reviews and monitors the curriculum of its academic programs.

#### Vision

Imparting the quality of Mathematics education and inculcating education of the spirit of research through innovative teaching and research methodologies.

#### Mission

- **M-1:** To provide an environment where student can learn, become competent users of Mathematics and understand the use of Mathematics in other disciplines.
- M-2: To produce post graduate students with strong foundation to join research or to serve industry.
- **M-3:** To provide the best possible facilities for our students, particularly in the area of computer facilities, library facilities and administrative support.
- **M-4:** To strive by introducing the students to main ideas and methods of Mathematics for building up their reasoning and analytical skills.

#### **Program Educational Outcomes (PEOs)**

The Postgraduate students will:

- **PEO-1:** Have significant opportunities in various service domains at National and International levels like banking, insurance, government jobs, consultancy, teaching, defence, industry, research and entrepreneurial pursuit.
- **PEO-2:** Achieve peer recognition as an individual or as a team member having specialized knowledge and expertise to investigate, formulate, analyze and implement on the problems of pure, applied and computational mathematics to compete at global level.
- **PEO-3:** Have leadership quality to handle all kind of circumstances in diversities by providing interdisciplinary and multidisciplinary learning environment.



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**PEO-4:** Have continuous learning attitude to adopt new skills and techniques to overcome the problems related with new technologies.

**PEO-5:** Inculcate value system while working in a team assigned with a important targets they will contribute through their critical thinking and mathematical competence holding the ethical values.

#### **Program Outcomes (Pos)**

#### Students will:

- 1. **Advanced Mathematical Knowledge:** Students will: Graduates gain a comprehensive understanding of various branches of pure mathematics, including algebra, analysis, topology, geometry, number theory, and logic.
- **2. Problem-solving Skills**: They develop advanced problem-solving skills, essential for various fields like finance, engineering, and data analysis and the ability to tackle complex mathematical problems using logical reasoning and critical thinking.
- **3. Research Abilities**: Many pursue a Ph.D. after their M.Sc. to become mathematicians or professors. This can involve conducting research, publishing papers, and teaching at universities.
- **4.Quantitative Analysis**: Graduates are adept at quantitative analysis, which is highly sought after in fields like finance, economics, and computer science.
- **5. Teaching and Academia**: Many pursue careers in academia as professors or researchers, contributing to the development of mathematical theories and teaching future mathematicians.
- **6. Theoretical Understanding**: A strong foundation in mathematical theory helps students understand abstract concepts and their applications in various areas, such as physics, computer science, and finance.
- **7. Communication Skills:** Graduates learn to effectively communicate complex mathematical ideas both in written and oral forms, essential for presenting research findings or teaching.
- **8.Operations Research**: Mathematicians optimize processes and solve complex problems in industries such as logistics, supply chain management and manufacturing.
- **9. Application in Industry**: Graduates might find opportunities in sectors like finance, data analysis, cryptography, or technology, where strong analytical skills and problem-solving abilities are highly valued.
- **10.Engineering and Technology**: Mathematics is the backbone of engineering and technology fields, enabling graduates to work in areas like cryptography, robotics, and computer graphics.



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- **11.Government and Public Sector**: Mathematicians are employed in government agencies for statistical analysis, policy development, and research.
- **12. Consulting**: Mathematicians often work as consultants, providing expertise in problem-solving and quantitative analysis to various industries.

#### **Program Specific Outcomes (PSOs)**

Students will:

**PSO-1:** Understand the mathematical concepts and applications in the field of algebra, analysis, computational techniques, optimization, differential equations, engineering, finance and actuarial science.

**PSO-2:** Handle the advanced techniques in algebra, analysis, computational techniques, optimization, differential equations, engineering, finance and actuarial science to analyze and design algorithms solving variety of problems related to real life problems.

**PSO-3:** Develop necessary skills and expertise in the field of research and developments through seminar and dissertation.

PSO-4: Creates Mathematical Models.

#### Consistency/Mapping of PEOs with Mission of the Department

PEO M1 M2 M3 M4 PEO-1 3 2 2 3 2 3 PEO-2 3 3 PEO-3 3 3 1 1 PEO-4 2 2 3 3 PEO-5 1 2 2 3

1: Slight Moderate Substantial

correlation

(Low), 2: (Medium), 3: (High) "-": No

#### **GENERAL COURSE STRUCTURE & THEME**

#### 1. Definition of Credit

1 Hr. Lecture (L) per week	1 Credit
1 Hr. Tutorial (T) per week	1 Credit

#### 2. Range of Credits:

In the light of the fact that a typical Model Two-year Post Graduate degree program in Basic Science has about 87 credits, the total number of credits proposed for the Two-year M.Sc.Mathematics is kept as considering NEP-20 and NAAC guidelines.



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#### 3. Structure of PG Program in Mathematics:

The structure of PG program in Mathematics shall have essentially the following categories of courses with the breakup of credits as given:

#### **Components of the Curriculum**

#### (Program curriculum grouping based on course components)

SI No	Course Component	% of total number of	Total number of
		credits of the	Credits
		Program	
2	Program Core (PCC)		
		68.97	60
3	Program Electives (PEC)		
		4.59	4
4	Open Electives (OEC)		
		4.59	4
5	Project(s) (PRC)/ On job Plant Training		
	(OJT) and seminar	21.84	19
	Total		87
		100.00	

#### **General Course Structure and Credit Distribution**

#### Curriculum of M.Sc. Mathematics

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Semester -I		Semester - II				
Course Title Credit		Course Title	Credit			
1. Advanced Abstract Algebra-I	3:1:0=4	Advanced Abstract Algebra-II	3:1:0=4			
2. Real Analysis-l	3:1:0=4	2. Real Analysis-II	3:1:0=4			
3.Topology	3:1:0=4	3.Complex Analysis-II	3:1:0=4			
4.Complex Analysis-I	3:1:0=4	4.Ordinary and Partial differential Equations	3:1:0=4			
5.Research Methodology	3:1:0=4	5. Advanced Discrete Mathematics	3:1:0=4			
		6. Review of Literature	2:0:0=2			
Total Credit	20	Total Credit	22			
Semester -III		Semester - IV				
Course Title	Credit	Course Title	Credit			
1.Operational Research	3:1:0=4	Analytic Number Theory	3:1:0=4			
2. Integral Equation	3:1:0=4	Functional Analysis	3:1:0=4			
3. Advanced Numerical Techniques	3:1:0=4	General Theory of Relativity	3:1:0=4			



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4. Special Function	3:1:0=4	Research Project and Seminar	10
5. Fundamentals of Computers &	3:0:1=4	-	
Programming			
6. Scientic writing	2:1:0=3	-	
Total Credit	23	Total Credit	22

RM: Research Methodology; Research Project: RP; T- Theory Course, P – Practical course.

1T means 1hr of teaching per week and 1P means 2hrs of teaching/practical /tutorial/lab per week for 15 weeks.

**Total Credit: 87** 

#### **Course code and Definition**

L = Lecture
T = Tutorial
P = Practical
C = Credit

ESC = Engineering Science Courses
PEC = Professional Elective courses

OEC = Open Elective courses

IKS = Indian Knowledge System

**SDGs** = Sustainable Development Goals

#### Course level coding scheme:

Three-digit number (odd numbers are for the odd semester courses and even numbers are for even semester courses) used as suffix with the Course Code for identifying the level of the course. Digit at hundred's place signifies the year in which course is offered. e.g.

101, 102 ... etc. for first Semester.

201, 202 .... Etc. for second Semester.

301, 302 ... for third Semester.

401. 402--- for Fourth Semester

#### **Program Core Course**

(Total Credit-60)

SI.	CodeNo.	Subject	Semester	Credits
1	78MS101	Advanced Abstract Algebra-I	I	4
2	78MS102	Real Analysis-I	I	4
3	78MS103	Topology	I	4
4	78MS104	Complex Analysis-I	I	4
5	78MS201	Advanced Abstract Algebra-II	П	4
6	78MS202	Real Analysis-II	П	4
7	78MS203	Complex Analysis-II	11	4
8	78MS204	Ordinary and Partial differential Equations	П	4



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15	15 78MS402 Functional Analysis IV  Total Credit				
14	78MS401	Analytic Number Theory	IV	4	
13	78MS304	Special Function	III	4	
12	78MS303	Advanced Numerical Techniques	III	4	
11	78MS302	Integral Equation	tegral Equation III		
10	78MS301	Operational Research	Operational Research III		
9	78MS205	Advanced Discrete Mathematics	4		

#### **Category-wise Courses**

#### **PROGRAM ELECTIVE COURSE (PEC)**

#### ( Total 01 from the Program elective subjects = 04 Credit)

SI.	CodeNo.	CodeNo. Subject Semester			
1	78MS403- A	General Theory of Relativity	IV	04	
2	78MS403- B	Jacobi polynomial and H-function	IV	04	
3	78MS403-C	Advanced Mathematical Statistics	IV	04	
4	78MS403-D	Swayam/Mooc Course: (Probability and Statistics)	IV	04	
	Total Credit				

#### **OPEN ELECTIVE COURSE (OEC)**

#### (Total 01 from Open elective subjects= 04 Credits)

SI.	CodeNo.	Subject	Semester	Credits
1	78MS305-A	Fundamentals of Computers & Programming	III	04
2	78MS305-B	Swayam/Mooc Course: (Math for Data Science)	Ш	04
3	78MS305-C	Swayam/Mooc Course: (Python Programming)	Ш	04
		Total Credit		04

#### **RESEARCH COURSE (RC)**

#### (Any One Research Course from each semester = 19 Credits)

SI.	CodeNo.	Subject	Semester	Credits	
1	78MS105	Research Methodology	1	0:0:4=4	
2	<b>2</b> 78MS206 Review of Literature		II	0:0: 2=2	
3	78MS306-A	Scientic Writing	III	0:0:3=3	
	78MS306-B	Swayam/Mooc Course: (Academic and Research	Ш	0:0:3=3	
	781VI3300-B	Report Writing)			
4	4 78MS451 Research Project and Seminar		IV	0:0:10=10	
	Total Credit				

#### **Induction Program**



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Induction program for students to be offered right at the start of the first year. It is mandatory. AKS University has design an induction program for 1<sup>st</sup> year student, details are below:

- i. Physical activity
- ii. Creative Arts
- iii. Universal Human Values
- iv. Literary
- v. Proficiency Modules
- vi. Lectures by Eminent People
- vii. Visits to local Areas
- viii. Familiarization to Dept./Branch & Innovations

#### **Evaluation Scheme:**

#### 1. For Theory Courses:

- i. The weightage of Internal assessment is 50% and
- ii. End Semester Exam is 50%

The student has to obtain at least 40% marks individually both in internal assessment and end semester exams to pass.

#### 2. For Practical Courses:

- i. The weightage of Internal assessment is 50% and
- ii. End Semester Exam is 50%

The student has to obtain at least 40% marks individually both in internal assessment and end semester exams to pass.

#### 3. For Summer Internship / Projects / Seminar etc.

Evaluation is based on work done, quality of report, performance in viva-voce, presentation etc

#### **Semester Wise Course Structure**

#### **Semester wise Brief of total Credits and Teaching Hours**

Semester	L	Т	Р	Total Hour	Total Credit
Semester -I	15	5	00	20	20
Semester -II	17	5	00	22	22
Semester -III	18	5	00	23	23
Semester - IV	9	3	00	12	22
Total	59	18	00	77	87

#### **Semester Wise Course Details**

#### Semester – I



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			-				Hour	
1	PCC	78MS101	Advanced Abstract Algebra-I	3	1	-	4	4
2	PCC	78MS102	Real Analysis-l	3	1	-	4	4
3	PCC	78MS103	Topology	3	1	-	4	4
4	PCC	78MS104	Complex Analysis-I	3	1	-	4	4
5	RC	78MS105	Research Methodology	3	1	-	4	4
			Total	15	5	-	20	20

#### Semester -II

S.N.	Category	Code	Course Title	L	Т	Р	Total H	Credit s
1	PCC	78MS201	Advanced Abstract Algebra-II		1	-	4	4
2	PCC	78MS202	Real Analysis-II 3 1 - 4		4	4		
3	PCC	78MS203	Complex Analysis-II		1	-	4	4
4	PCC	78MS204	Ordinary and Partial differential Equations	3	1		4	4
5	PCC	78MS205	Advanced Discrete Mathematics		1	-	4	4
6	RC	78MS206	Review of Literature		0	•	2	2
			Total		5		22	22

#### Semester-III

S. N.	Cate gory	Code	Course Title	L	Т	Р	Total H	Credit s
1	PCC	78MS301	Operational Research	3	1	-	4	4
2	PCC	78MS302	Integral Equation	3	1	-	4	4
3	PCC	78MS303	Advanced Numerical Techniques	3	1	-	4	4
4	PCC	78MS304	Special Function	3	1	-	4	4
5	Open Elective Courses ( OEC) - [Choose any one ]				0	1	4	4
	78MS305-A    Electives   I: Fundamentals of Computers & Programming							



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	78MS305-B	Electives II: Swayam/Mooc Course: (Math for Data Science)					
	78MS305-C	Electives III: Swayam/Mooc Course: (Python Programming)					
6	Research Courses [ Choose any one ]		3	0	-	3	3
78N	IS306-A	Scientific Writing					
78N	IS306-B	Swayam/Mooc Course: (Academic and Research Report Writing)					
		Total	18	4	1	23	23

#### Semester -IV

S.N	Category	Code	Course Title	L			Total H	Credits
1	PCC	78MS401	Analytic Number Theory	3	1	-	4	4
2	PCC	78MS402	Functional Analysis	3	1	-	4	4
3	Program E	lective Cours	es(PEC)- [ Choose any one ]	3	1	-	4	4
	78MS403- A		<b>Electives IV:</b> General Theory of Relativity					
	78MS	5403- B	<b>Electives V:</b> Jacobi polynomial and H-function					
	78MS403-C		Electives VI: Advanced Mathematical Statistics					
			Electives VII: Swayam/Mooc Course: (Probability and Statistics)					
4	RC	78MS451	Research Project and Seminar					10
			Total	9	3	-	12	22

Total credit: 87

PCC – Program Core Courses, PEC - Program Elective Courses OEC - Open Elective Courses

RC -Research Course,

L – Lecture; T - Tutorial; P - Practical



#### Semester-I

Course Code: 78MS101

Course Title : Advanced Abstract Algebra-I

Pre- requisite: Students should have basic knowledge of group

theory

Rationale: The program aims to develop advanced problem-

solving and analytical skills and prepares students for careers in academia, research, industry, or other sectors that require advanced

mathematical expertise.

#### **Course Outcome:**

**CO1-78MS101.1** Understand the importance of algebraic properties with regard to working within various number systems.

**CO2-78MS101.2**. Students will determine whether a given binary operation on the given set gives a group structure by applying the axioms.

**CO3-78MS101.3**. Students will determine whether a given binary operation on the given set gives algebraic structure by applying the axioms of Ring.

**CO4-78MS101.4** Connecting ring theory to other areas of mathematics or applications in computer science, physics, or cryptography.

**CO5-78MS101.5** Students will create the concept of a group action to real life problems such as Counting.

#### Scheme of Studies:

Board of Study	Course Code	Course Title	Scheme of	Scheme of studies (Hours/Week)				Total Credit
J. J			Cl	LI	sw	SL	Total Study Hours (CI+LI+SW+SL)	s (C)
Program Core (PCC)	78MS101	Advanced Abstract Algebra-I	4[3+1]	0	1	1	6	4



#### Legend:

**CI:** Classroom Instruction (Includes different instructional strategies i.e. Lecture (L) and Tutorial (T) and others),

**LI:** Laboratory Instruction (Includes Practical performances in laboratory workshop, field or other locations using different instructional strategies)

SW: Sessional Work (includes assignment, seminar, mini project etc.),

**SL:** Self Learning,

C:Credits.

**Note:** SW & SL has to be planned and performed under the continuous guidance and feedback of teacher to ensure outcome of Learning.

#### **Scheme of Assessment:**

#### Theory

Board of	Couse Code	Course Title	Sc	cheme of Ass	essment ( Marl	ks )				
Study			Progressi	ve Assessmer	nt ( PRA )				End Semester Assessme nt (ESA)	Total Marks (PRA+ ESA)
			Class/Home Assignment 5 number 3 marks each ( CA)	Class Test 2 (2 best out of 3) 10 marks each (CT)	Seminar one ( SA)	Class Activity any one (CAT)	Class Attendanc e (AT)	Total Marks (CA+CT+SA +CAT+AT)		
PCC	78MS101	Advanced Abstract Algebra-I	15	20	5	5	5	50	50	100

#### **Course-Curriculum Detailing:**

This course syllabus illustrates the expected learning achievements, both at the course and session levels, which students are anticipated to accomplish through various modes of instruction including Classroom Instruction (CI), Laboratory Instruction (LI), Sessional Work (SW), and Self Learning (SL). As the course progresses, students should showcase their mastery of Session Outcomes (SOs), culminating in the overall achievement of Course Outcomes (COs) upon the course's conclusion.

#### CO1-78MS101.1

Understand the importance of algebraic properties with regard to working within various number systems.



#### **Approximate Hours**

Item	AppX Hrs
Cl	13
LI	0
SW	1
SL	1
Total	15

Session Outcomes (SOs)	Laboratory Instruction (LI)	Class room Instruction (CI)	Self Learning (SL)
SO1.1 Understand the concept of Group. SO1.2 Understand the relationships between abstract algebraic structures with familiar numbers systems such as the integers and real numbers SO1.3 Understand the relation between order of group and all its possible subgroups. So1.4 Understand the hypothesis of Cauchy's Theorem So1.5 Understand the concept of Mapping.	-	Unit-1.0 Group-I: 1.1 Introduction of Group and properties of group 1.2 Implimentation of Cyclic group 1.3 Centre of a group 1.4 Tutirial -I 1.5 Normal subgroup 1.6 Quotient group 1.7 Class Equation 1.8 Composition series, Normal and subnormal series, 1.9 Jorden-Holder theorem 1.10 Tutirial -II 1.11Homomorphism of Group 1.12 Isomorphism of a group 1.13 Theorems on Mappings	SL.1 Understand the concept of Set theory. SL.2 Decide whether a given group is cyclic, and given a finite cyclic group. SL.3 Understand to Find a generator for a subgroup of a given order.

#### SW-1 Suggested Sessional Work (SW):

#### a. Assignments:

- i. Relationships between abstract algebraic structures with familiar numbers systems such as the Set of natural numbers, Set of rational numbers, Set of integers, Set of real numbers, Set of complex numbers
- ii. Application of group theory in real life.



- iii. Derivation of Cauchy's Theorem for finite groups.
- iv. Mapping defined on groups

#### b. Mini Project:

Oral presentation, Poster presentation, Power Point Presentation.

**c.** Other Activities (Specify): Quiz, Class Test.

#### CO2-78MS101.2

Students will determine whether a given binary operation on the given set gives a group structure by applying the axioms.

Item	AppX Hrs
Cl	12
LI	0
SW	1
SL	1
Total	14

Session Outcomes	Labora	Class room Instruction	Self Learning
(SOs)	tory	(CI)	(SL)
	Instruc		
	tion		
	(LI)		
SO2.1		Unit-2.0	SL.1
Understand the relationships		Group II:	Verify relationships
between operations and mapping.		2.1 Permutation groups	between operations
SO2.2		2.2 Composition series	satisfying various
Learn about structure preserving		2.3 Normal and subnormal	properties.
maps between groups and their		series	
consequences.		2.4 Jordan-Holder theorem	SL.2
SO2.3		2.5 Tutirial -I	Present concepts of the
Understand the concept of		2.6 Introduction of Ring	relationships between
Composition series		27 Unit element, Zero	operations satisfying
		devisors	various properties
SO2.4		2.8 Elementary properties of	SL.3
Understand the Uses of		Ring	
Composition series in Jordan-		2.9 Tutirial -II	Knowledge of
Holder theorem		2.10 Theorems on Ring	polynomial and its
SO2.5		2.11 Nilpotent element	degree



Understand the Relation of Ring and Various polynomials	2.12 Polynomial Ring in one and several variables.	

#### SW-2 Suggested Sessional Work (SW):

#### a. Assignments:

- i. Relationships between algebraic structures of ring with familiar numbers systems.
- ii. Application of Ring group theory in real life.
- iii. Permutation group.
- iv. Mapping defined on Rings.
- V. Polynomial Ring

#### b. Mini Project:

Oral presentation, Poster presentation, Power Point Presentation.

c. Other Activities (Specify):

Quiz, Class Test

#### CO3-78MS101.3

Students will determine whether a given binary operation on the given set gives algebraic structure by applying the axioms of Ring.

Item	AppX Hrs
Cl	12
LI	0
SW	1
SL	1
Total	14

Session Outcomes (SOs)	Laborat ory Instructi on (LI)	Class room Instruction (CI)	Self Learning (SL)
SO3.1		Unit-3.0 Ring	SL.1
Understand the relationships		3.1 SubRings:	Understand
between operations and mapping.		Definition, Properties	the concept
SO3.2		3.2 Quotent ring	of Mapping.
Structural Understanding: Exploring		3.3 Fundamental theorem on	SL.2
rings and subrings helps		ring	Understand



mathematicians understand the	3.4 Ideals in quotent ring	the
underlying structure of mathematical	3.5 Tutorial-I	structure of
objects, providing insight into their	3.6 Ring Homomorphism and	kernel of
properties and behaviors.	Ring Isomorphism	Mapping
	3.7 Kernel of Homomorphism	
SO3.3	3.8 Theorems on Ideals	
Algebraic Properties: Understand the	3.9 Relation between Ring and	
Rings and subrings properties, which	Ideal	
help in studying algebraic properties	3.10 Tutorial-II	
such as factorization, divisibility, and	3.11 Theorems on Rings	
solution of equations within these	3.12 Application of Ring in Real	
structures.	life.	

#### SW-3 Suggested Sessional Work (SW):

#### a. Assignments:

- i. Relationships between algebraic structures of ring with familiar numbers systems.
- ii. Application of Ring group theory in real life.
- iii. Permutation group.
- iv. Mapping defined on Rings.
- V. Polynomial Ring

#### b. Mini Project:

Oral presentation, Poster presentation, Power Point Presentation.

**c.** Other Activities (Specify):

Quiz, Class Test.

#### CO4-78MS101.4

Connecting ring theory to other areas of mathematics or applications in computer science, physics, or cryptography.

Item	AppX Hrs
Cl	12
LI	0
SW	1
SL	1
Total	14



## AKS University Faculty of Basic Science Department of Mathematics

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Session Outcomes (SOs)	Laborator y Instructio n	Class room Instruction (CI)	Self Learning (SL)
	(LI)		
SO4.1 Understand the examples of integral domains, exploring the properties that define them. SO4.2 Understand the demonstration of, how they differ from other types of rings.  SO4.3 Understand The Difference between Integral domain and Field		Unit-4.0 Integral domain and Field 4.1 Integral domain: Definition and properties 4.2 Proof of the Properties Integral domain 4.3 Theorems on Integral Domain 4.4 Tutorial-I 4.5 Establish the relationship between Ring and Integral Domain 4.6 Field: Definition and properties 4.7 Proof of the Properties of Field 4.8 Establish the relationship between Ring and Field 4.9 Tutorial-II 4.10 Theorems on field 4.11 Theorems on Relation between Integral domain and Field 4.12 Implimentation of the conceptes in number system	SL.1 Verify relationships between operations satisfying various properties.  SL.2 Basic properties of Ring with properties

#### SW-4 Suggested Sessional Work (SW):

#### a. Assignments:

- i. Relationships between algebraic structures of ring with familiar numbers systems.
- ii. Application of Ring group theory in real life.
- iii. Permutation group.
- iv. Mapping defined on Rings.
- V. Polynomial Ring

#### b. Mini Project:

Oral presentation, Poster presentation, Power Point Presentation.

c. Other Activities (Specify):

Quiz, Class Test.

#### CO5-78MS101.5

Students will create the concept of a group action to real life problems such as Counting.



#### **Approximate Hours**

Item	AppX Hrs
Cl	11
LI	0
SW	1
SL	1
Total	13

Session Outcomes	Laboratory	Class room Instruction	Self Learning
(SOs)	Instruction (LI)	(CI)	(SL)
SO5.1	,	Unit-5.0 Ideals	SL.1
Understand the		5.1	Verify
concept of left and		Ideals : Left and right ideals	relationships
right ideal		5.2	between
SO5.2		Relation between Ideals and ring	operations
Understand the		5.3 Quotient Ring	satisfying various
relationships between		5.4Relation between Ideal and	properties.
quotent ring and Ideal.		Quotient Ring	
SO5.3		5.5 prime ideals	SL.2
Understand the		5.6 Generator of Basic properties of	understand the
relationships between		ideals	criteria to be a
ring and Ideal		5.7 Maximal ideas	subring.
		5.8 Algebra of ideals	SL.3
		5.9 Ideals in quotent ring	Basic properties
		5.10 PID (Principal Ideal Domain)	of Quotient ring .
		5.11 Tutorial	

#### **Brief of Hours suggested for the Course Outcome**

Course Outcomes	Class Lecture (CI)	Sessional Work (SW)	Self Learning (SI)	Total hour (Cl+SW+SI)
CO1-78MS101.1 Understand the importance of algebraic properties with regard to working within various number systems.	13	1	1	15
CO1-78MS101.2  Determine whether a given binary operation on the given set gives a group structure by applying the	12	1	1	14



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#### Curriculum & Syllabus of M.Sc. Mathematics program

axioms.				
CO1-78MS101.3  Students will determine whether a given binary operation on the given set gives algebraic structure by applying the axioms of Ring.	12	1	1	14
CO1-78MS101.4 Compute the expression of permutation groups by using permutation multiplication.	12	1	1	14
CO1-78MS101.5  Create the concept of a group action to real life problems such as Counting.	11	1	1	13
Total Hours	60	5	5	70

#### **Suggestion for End Semester Assessment**

#### Suggested Specification Table (For ESA)

со	Unit Titles	Marks Distribution			Total Marks
		R	U	Α	
CO-1	Group-I	05	03	02	10
CO-2	Group-II	05	03	02	10
CO-3	Ring	05	03	02	10
CO-4	Integral Domain and Field	05	04	01	10
CO-5	Ideals	05	04	01	10
Total		25	17	08	50

Legend: R: Remember, U: Understand, A: Apply



The end of semester assessment for Introduction to Portland cement will be held with written examination of 50 marks

**Note**. Detailed Assessment rubric need to be prepared by the course wise teachers for above tasks. Teachers can also design different tasks as per requirement, for end semester assessment.

#### **Suggested Instructional/Implementation Strategies**

- 1. Improved Lecture
- 2. Tutorial
- 3. Presentation
- 4. Group Discussion
- 5. Online sources
- 6. Seminar
- 7. Workshop

#### **Suggested Learning Resources:**

a) Books:

S. No.	Title	Author	Publisher	Edition & Year
1	Advanced Abstract Algebra	Dr.H.K.Pathak	Shree Sahitya Siksha Prakashan, Meerut.	
2	Contemporar y Abstract Algebra	J. A. Gallian	Narosa Publishing house, New Delhi	4th edition, 2009
3	Abstract Algebra,	D. S. Dummit & R. M.,Foote	John Wiley & Sons, Indian reprint, New Delhi	3rd edition, 2011
4	Basic Abstract Algebra	P.B. Bhattacharya , S.K.Jain &S.R. Nagpaul	Cambridge University press	
5	Basic Algebra,Vol.	N.Jacosan	Hindustan Publishing Company	



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#### Curriculum & Syllabus of M.Sc. Mathematics program

I,II & VIII		
1,11		

#### b) Reference Book:

S. No.	Title	Author	Publisher	Edition & Year
1	Abstract Algebra	I.N. Herstein:, Macmillan	ISBN-10: 0471368792	3rd Edition, 1996
2	Topics in Algebra, John Wiley and Sons	I.N. Herstein	ISBN-10: 0471010901	2nd Edition,1975
3	An Introduction to Ring Theory	P.M. Cohn	Springer Undergraduate Series, ISBN-10: 1852332069	2001
4	Topics in Algebra	Herstein, I. N.	John Wiley & Sons, Indian reprint, New Delhi	2nd edition, 2006
5	A First Course in Abstract Algebra	Fraleigh, J. B.	Pearson Education India, New Delhi	7th edition, 2008

#### c) Suggetsed Digital Platform Web links:

Suggested Digital Platforms Web links:	https://epgp.inflibnet.ac.in https://www.highereducation.mp.gov.in/?page=xhzlQmpZwkylQo2b%2Fy5G7w %3D%3D http://www.bhojvirtualuniversity.com
Suggested Equivalent online courses:	https://nptel.ac.in/courses/111/106/111106137/ https://nptel.ac.in/courses/111/105/111105112/ https://ugemoocs.inflibnet.ac.in/index.php/courses/view_ug/32

#### **Curriculum Development Team**

- 1. Dr.Sudha Agrawal, HOD, Department of Mathematics.
- 2. Dr.Ekta Shrivastava , Assistant Professor, Department of Mathematics.
- 3. Mr. Neelkanth Napit, Assistant Professor, Department of Mathematics.
- 4. Mrs. Vandana Soni, Assistant Professor, Department of Mathematics.
- 5. Mr.Radhakrishna Shukla, Assistant Professor, Department of Mathematics.
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- 7. Ms. Pushpa Kushwaha, Assistant Professor, Department of Mathematics.
- 8. Ms. Arpana Tripathi, Assistant Professor, Department of Mathematics



#### **Cos, POs and PSOs Mapping**

**Course Title: M.Sc. Mathematics** 

Course Code: 78MS101

**Course Title: Advanced Abstract Algebra-I** 

	Title: Advanced Appendic Algebra 1															
					1				1				,			1
	PO1	PO2	PO	PO	PO5	PO6	PO7	PO	PO9	PO10	PO11	PO	PSO 1	PSO 2	PSO 3	PSO 4
Course			3	4				8				12				
Outcome	Adva	Pro	Re	Qu	Tea	Theo	Com	Op	Applicati	Engin	Govern	Co	Understan	Han	Develop	Creat
Outcome	nced	ble	se	an	chin	retic	muni	era	on in	eerin	ment	nsu	d the	dle	necessar	es
	Math	m-	ar	tit	g	al	catio	tio	Industry	g and	and	ltin	mathemat	the	y skills	Math
	emati	solv	ch	ati	and	Unde	n	ns		Tech	Public	g	ical	adva	and	emati
	cal	ing	Ab	ve	Aca	rstan	Skills	Res		nolog	Sector		concepts	nced	expertis	cal
	Know	Skill	ilit	An	de	ding		ear		у			and	tech	e in the	Mode
	ledge	S	ies	aly	mia			ch					applicatio	niqu	field of	ls
	_			sis									ns in the	es	research	
													field of			
													algebra			
CO1- <b>78MS101.1</b>	2	3	1	2	1	2	2	2	1	1	1	1	<u>2</u>	1	<u>1</u>	<u>3</u>
Understand the													_	_	_	_
importance of																
<u> </u>																
algebraic properties									1							
with regard to working																
within various number									1							
systems.	1	2	1	1	1	1	1	1	1	-	2	1	2	1	1	2
CO2-78MS101.2.	1	3	2	1	1	1	1	1	1	2	3	1	<u>3</u>	1	<u>1</u>	<u>2</u>
Students will																
determine whether a																
given binary																
operation on the																
given set gives a																
group structure by																
applying the axioms.																
CO3-78MS101.3.	2	3	2	2	1	1	3	2	1	1	3	1	<u>2</u>	<u>1</u>	<u>2</u>	2
Students will	_		_	_	_			_		_		_	=	l =	=	_
determine whether a																
given binary operation																
on the given set gives																
algebraic structure									1							
by applying the axioms																
of Ring.									1							
CO4-78MS101.4	2	3	2	2	1	1	3	2	1	1	3	1	<u>2</u>	1	<u>2</u>	2
Connecting ring theory		5	_	_	-	1	,	_	*	1		_	<u> </u>	^	<u> </u>	_
to other areas of									1							
mathematics or									1							
applications in									1							
• •																
computer science,																
physics, or									1							
cryptography.	-	2	-	2	1	1	2		1	1	-	1	2	1	2	2
CO5-78MS101.5	2	3	2	2	1	1	3	2	1	1	3	1	<u>2</u>	<u>1</u>	<u>2</u>	3
Students will create									1							
the concept of a group									1							
action to real life									1							
problems such as									1							
Counting.																

Legend: 1 – Low, 2 – Medium, 3 – High



#### **Course Curriculum Map:**

POs & PSOs No.	COs No.& Titles	SOs No.	Labo rator y Instr uctio n(LI)	Classroom Instruction (CI)	Self Learning (SL)
PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2, 3, 4	CO1-78MS101.1 Understand the importance of algebraic properties with regard to working within various number systems.	SO1.1 SO1.2 SO1.3 SO1.4 SO1.5	-	Unit-1.0 Group 1.1,1.2,1.3,1.4,1.5,1.6,1.7,1 .8,1.9,1.10,1.11,1.12,1.13	SL1.1 SL1.2
PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2, 3, 4	CO2-78MS101.2.  Students will determine whether a given binary operation on the given set gives a group structure by applying the axioms.	SO1.1 SO1.2 SO1.3 SO1.4 SO1.5		Unit-2 Ring 2.1, 2.2, 2.3, 2.4, 2.5, 2.6, 2.7, 2.8,2.9,2.10, 1.11,1.12	SL2.1 SL2.2
PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2, 3, 4	CO3-78MS101.3. Students will be able to describe all elements in a cyclic subgroup by using generators.	SO1.1 SO1.2 SO1.3 SO1.4 SO1.5		Unit-3 2.1, 2.2, 2.3, 2.4, 2.5, 2.6, 2.7, 2.8,2.9,2.10, 1.11,1.12	SL3.1 SL3.2
PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2, 3, 4	CO4- 78MS101.4 Connecting ring theory to other areas of mathematics or applications in computer science, physics, or cryptography.	SO1.1 SO1.2 SO1.3 SO1.4 SO1.5		Unit-4 2.1, 2.2, 2.3, 2.4, 2.5, 2.6, 2.7, 2.8,2.9,2.10, 1.11,1.12	SL4.1 SL4.2
PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2, 3, 4	CO5-78MS101.5 Students will create the concept of a group action to real life problems such as Counting.	SO1.1 SO1.2 SO1.3 SO1.4 SO1.5		Unit-5 2.1, 2.2, 2.3, 2.4, 2.5, 2.6, 2.7, 2.8,2.9,2.10, 1.11	SL5.1 SL5.2 SL5.3



#### Semester-I

Course Code: 78MS102
Course Title : Real Analysis-l

Pre-requisite: Students should have basic knowledge of and

deep understanding of the theory of the functions of real variables and Riemann-Stieltjes

Integral

Rationale: The program aims to develop advanced problem-

solving and analytical skills and prepares students for careers in academia, research, industry, or other sectors that require advanced

mathematical expertise.

CO1-78MS102.1 Understand the importance of properties of Riemann-Stieltjes integrals.

CO2-78MS102.2 Determine the Rearrangements of terms of a series.

**CO3-78MS102.3** Demonstrate an understanding of the theory of sequence and Students will be able to describe all elements in Uniform Convergence of Sequence.

**CO4-78MS102.4** Define and recognize the series and Students will compute the expression of Linear transformations.

**CO5-78MS102.5** Students will create the concept of a Differential forms, Stoke's theorem to sequences, and series.

#### **Scheme of Studies:**

Board of	Course Code	Course Title	Scheme of studies (Hours/Week)					
Study			Cl	LI	sw	SL	Total Study Hours (CI+LI+SW+SL)	ts (C)
Program Core (PCC)	78MS102	Real Analysis-I	4[3+1]	0	1	1	6	4

#### Legend:



**CI:** Classroom Instruction (Includes different instructional strategies i.e. Lecture (L) and Tutorial (T) and others),

**LI:** Laboratory Instruction (Includes Practical performances in laboratory workshop, field or other locations using different instructional strategies)

**SW:** Sessional Work (includes assignment, seminar, mini project etc.),

SL: Self Learning,

C:Credits.

**Note:** SW & SL has to be planned and performed under the continuous guidance and feedback of teacher to ensure outcome of Learning.

#### **Scheme of Assessment:**

#### Theory

Board of	Couse	Course Title	Scheme of	Assessme	nt ( Marks	)				
Study	Code		Progr	End Semester Assessm ent (ESA)	Total Marks (PRA+ ESA)					
			Class/Ho me Assignme nt 5 number 3 marks each ( CA)	Class Test 2 (2 best out of 3) 10 marks each (CT)	Seminar one (SA)	Class Activit y any one (CAT)	Class Attend ance (AT)	Total Marks (CA+CT+ SA +CAT+A T)		
PCC	78MS102	Real Analysis-I	15	20	5	5	5	50	50	100

#### **Course-Curriculum Detailing:**

This course syllabus illustrates the expected learning achievements, both at the course and session levels, which students are anticipated to accomplish through various modes of instruction including Classroom Instruction (CI), Laboratory Instruction (LI), Sessional Work (SW), and Self Learning (SL). As the course progresses, students should showcase their mastery of Session Outcomes (SOs), culminating in the overall achievement of Course Outcomes (COs) upon the course's conclusion.



#### CO1-78MS102.1

Understand the importance of Understand the concept of Riemann-Stieltjes Integral

Item	AppXHrs
Cl	14
LI	0
SW	1
SL	1
Total	16

Session Outcomes (SOs)	Laboratory Instruction (LI)	Class room Instruction (CI)	Self Learning (SL)
SO1.1		Unit-1.0	
Understand the		1.1 Introduction of	SL.1
concept of		Riemann-Stieltjes	Theorems on Riemann
Riemann-Stieltjes		Integral,	Stieltjes Integrals
IntegralSO1.2		<b>1.2</b> Some theorems on	
Understand the		Riemann-Stieltjes	
Properties of the		Integral,	
Riemann Stieltjes		1.3 Riemann-Stieltjes	
Integral		Integral,as limit of sum	
SO1.3		<b>1.4</b> Some classes of	
Understand The		Riemann-	
fundamental		Stieltjesfunction.	
theorem		<b>1.5</b> Properties of the	
SO1.4		Riemann-Stieltjes	
Understand the		Integral,	
Rectifiable Curves		1.6 Integration	
SO1.5		<b>1.7</b> differentiation,	
Understand the		1.8 The fundamental	
Mean value		theorem of calculus	
theorem		<b>1.9</b> Tutorial 1	
		1.10 Mean value	
		theorem	
		<b>1.11</b> Integration of vector	
		valued function	
		<b>1.12</b> Rectifiable Curves-	
		Introduction	
		<b>1.13</b> Rectifiable Curves-	
		theorems	
		<b>1.14</b> Tutorial 2	



#### SW-1 Suggested Sessional Work (SW):

#### a. Assignments:

- i. State and prove fundamental theorem of calculus
- ii. State and prove Mean Value theorem
- iii. Properties of R S Integral.
- iv. Theorems on Rectifiable Curve

#### b. Mini Project:

Oral presentation, Poster presentation, Power Point Presentation.

**c.** Other Activities (Specify):

Quiz, Class Test.

#### CO2-78MS102.2

determine Rearrangements of terms of a series Approximate Hours

Item	AppXHrs
Cl	5
LI	0
SW	1
SL	1
Total	7

Session Outcomes	Laboratory Instruction	Class room Instruction	Self Learning
(SOs)	(LI)	(CI)	(SL.1) Some examples
SO2.1A Relation		Unit2.0	on Riemann's
between the Riemann			
Integral and RS		2.1A Relation between	
Integral,		the Riemann Integral	
SO2.2Rearrangements		and Riemann stieltjes	
of terms of a series,		Integral,	
SO2.3Riemann's		2.2 Tutorial 1	
		2.3 Rearrangements of	
		terms of a series	
		2.4 Tutorial 2	
		2.5 Riemann's theorem	

#### SW-2 Suggested Sessional Work (SW):

#### a. Assignments:

- i. The sum of an absolute convergent series does not alter with any rearrangements of terms.
- ii. State and prove Riemanns theorems



iii. some theorems on Riemanns

#### b. Mini Project:

Oral presentation, Poster presentation, Power Point Presentation.

**c.** Other Activities (Specify): Quiz, Class Test.

#### CO3-78MS102.3

Students will be able to describe all elements in Uniform Convergence of Sequence

Item	AppXHrs
Cl	15
П	0
SW	1
SL	1
Total	17

Session Outcomes (SOs)	Laboratory Instruction (LI)	Class room Instruction (CI)	Self Learning (SL)
SO3.1		Unit-	<b>SL.1</b> Algebra of
Understand the Cauchy criterion for uniform		3.0 3.1 Sequence and Series of	Power Series
convergence		function,	
SO3.2 Understand the		3.2 Point wise convergence in a	
Power series,		metric space	
		3.3Pointwise and uniform	
SO3.3 Understand the Radius of Convergence		convergence of sequence.	
		3.4 Cauchy criterion for uniform	
SO3.4Understand the Radius of Convergence		convergence,	
		3.5Test for uniform convergence	
		3.6 Weierstrass M-Test,	
		3.7 Abel's test	
		3.8 Direchlets test	



3.9 Uniform convergence and
continuity,
3.10 Weierstrass's approximation
theorem,
3.11Power series,
3.12Uniqueness for power series,
3.13Radius of Convergence of
power series,
3.14Abel's theorem,
3.15Tauber's theorem.

#### SW-3 Suggested Sessional Work (SW):

#### a. Assignments:

- i. state and prove Tauber's theorem.
- ii. State and prove Weierstrass's approximation theorem
- iii. State and prove Cauchy 's general principle.

#### b. Mini Project:

Oral presentation, Poster presentation, Power Point Presentation.

**c.** Other Activities (Specify):

Quiz, Class Test.

#### CO4-78MS101.4

Students will compute the expression of Linear transformations

AppXHrs
12
0
1
1
14



Session Outcomes (SOs)	Outcomes Laboratory Instruction Class room Instruction (CI)		Self Learning (SL)
	•	Unit-4.0 4.1 Linear transformation, 4.2 Derivatives in an open subset of R <sup>n</sup> , 4.3 Chain rule of Differentiation, 4.4 Interchange of order of Differentiation, 4.4 Derivatives of higher order, 4.5 Taylor's theorem, 4.6 Inverse function theorem, 4.7 The Implicit function theorem 4.8 Derivatives of higher order 4.9 interchange of order of differentiation 4.10 Tutorial 1 4.11 Repeated partial derivatives 4.12 Tutorial 2	_

#### **SW-4 Suggested Sessional Work (SW):**

#### a. Assignments:

- i. Taylor's theorem
- ii. Inverse function theorem
- iii. The Implicit function theorem

#### b. Mini Project:

Oral presentation, Poster presentation, Power Point Presentation.

#### **c.** Other Activities (Specify):

Quiz, Class Test.



#### CO5-78MS101.5

Students will create the concept of a Differential forms ,Stoke's theorem.

Item	AppXHrs
Cl	14
LI	0
SW	1
SL	1
Total	16

Session Outcomes (SOs)	Laboratory Instruction (LI)	Class room Instruction (CI)	Self Learning (SL)		
	<u>-</u>		_		
		Proof 5.14 Tutorial 2			



#### **Brief of Hours suggested for the Course Outcome**

Course Outcomes	Class Lecture (CI)	Sessional Work (SW)	Self Learning (SI)	Total hour (Cl+SW+SI)
CO1-78MS102.1 Understand the importance of Riemann-Stieltjes Integral .	14	1	1	16
CO1-78MS102.2  Determine the Rearrangements of terms of a series	5	1	1	7
CO1-78MS102.3  Students will be able to describe all elements in Uniform Convergence of Sequence	15	1	1	17
CO1-78MS102.4 Students will compute the expression of Linear transformations.	12	1	1	14
CO1-78MS102.5 Students will create the concept of a Differential forms, Stoke's theorem	14	1	1	16
Total Hours	60	5	5	70

#### **Suggestion for End Semester Assessment**

#### Suggested Specification Table (For ESA)

СО	Unit Titles	Marks Distribution			Total Marks	
		R	U	A		
CO-1	Understand the importance of Riemann-Stieltjes Integral .	03	01	01		05
CO-2	Determine the Rearrangements of terms of a series	02	06	02		10
CO-3	Students will be able to describe all elements in Uniform Convergence of Sequence	03	07	05		15



CO-4	Students will compute the expression of Linear transformations.	-	10	05		15
CO-5	Students will create the concept of a Differential forms, Stoke's theorem	03	02		-	05
Total		11	26		13	50

Legend: R: Remember, U: Understand, A: Apply

The end of semester assessment for Introduction to Portland cement will be held with written examination of 50 marks

**Note**. Detailed Assessment rubric need to be prepared by the course wise teachers for above tasks. Teachers can also design different tasks as per requirement, for end semester assessment.

### **Suggested Instructional/Implementation Strategies**

- 1. Improved Lecture
- 2. Tutorial
- 3. Presentation
- 4. Group Discussion
- 5. Online sources
- 6 .Seminar
- 7. Workshop



### **Suggested Learning Resources:**

### a) Books:

S. N	Title	Author	Publisher	Edition & Year
1	Real Analysis-l	Dr.H.K.Pathak	Shree Sahitya Siksha Prakashan, Meerut.	2018
2	Real Analysis	S. C. Malik	Willey Eastern Ltd.,ew Delhi, 1985.	
3	Real Analysis,.	N. L. Carothers,	Cambridge University Press, UK, 2000	
4	Elementary Analysis:	Kenneth A. Ross	The theory of Calculus, Springer, New York, 2004.	
5	Principles of Mathematical Analysis	Walter Rudin	3 rd Edition, McGraw – Hill International Book Company, Singapore, 1982.	

### Curriculum Development Team

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### **Cos, POs and PSOs Mapping**

**Course Title: M.Sc. Mathematics** 

Course Code : 78MS102 Course Title: Real Analysis-I

	РО	РО	PO3	PO4	PO5	РО	PO7	PO8	PO9	PO1	PO1	Р	PSO	PS	PSO	PSO
Course	1	2				6				0	1	0	1	02	3	4
Outcome												1				
												2				
	Ad	Pr	Resea	Quan	Teac	Th	Com	Ope	Appli	Engi	Gov	С	Unde	На	Dev	Cre
	van	obl	rch	titati	hing	eor	muni	rati	catio	neer	ern	0	rstan	ndl	elop	ates
	ced	em	Abiliti	ve	and	eti	catio	ons	n in	ing	men	n	d the	е	nec	Mat
	Ma	-	es	Analy	Acad	cal	n	Res	Indus	and	t .	S	math	the	essa	hem
	the	sol		sis	emia	Un	Skills	earc	try	Tec	and	u	emat	adv	ry	atic
	ma	vin				der		h		hnol	Publ	lt	ical	anc	skill	al
	tica	g Skil				sta				ogy	ic	i	conc	ed	S	Mo
	ı Kn	Is				ndi					Sect or	n	epts and	tec hni	and exp	dels
	owl	15				ng					UI	g	appli	qu	ertis	
	ed												catio	es	e in	
	ge												ns in		the	
	80												the		field	
													field		of	
													of		rese	
													algeb		arch	
													ra			
CO1-	2	3	1	2	1	2	2	2	1	1	1	1	<u>2</u>	<u>1</u>	<u>1</u>	
78MS102.1																
Understand																
the																
importance																
of																
Understand																
the concept																
of Riemann-																
Stieltjes																
Integral																
CO1-	1	3	2	1	1	1	1	1	1	1	1	1	<u>1</u>	<u>1</u>	<u>1</u>	
78MS102.2																



Determine the Rearrangem ents of terms of a series																
CO1- 78MS102.3 Students will be able to describe all element in Uniform Convergen ce of Sequence.	2	3	1	1	1	1	3	2	2	1	2	2	1	2	<u>1</u>	
CO1- 78MS102.4 Students will compute the expression of Linear transformatio ns.	2	3	1	2	3	2	1	1	1	1	1	2	2	<u>1</u>	<u>1</u>	
CO1- 78MS102.5 Students will create the concept of a Differential forms, Stoke's theorem	1	2	3	2	2	2	2	2	1	1	1	1	1	1	1	

Legend: 1 – Low, 2 – Medium, 3 – High



### **Course Curriculum Map:**

POs & PSOs No.	COs No.& Titles	SOs No.	Laboratory Instruction(LI)	Classroom Instruction (CI)
PO 1,2,3,4,5,6 7,8,9,10,11,12	CO1-78MS102.1 Understand the importance of properties of	SO1.1		Unit-1.0 Riemann-Stieltjes Integral
PSO 1,2, 3, 4	Riemann-Stieltjes integrals	SO1.2		1.1,1.2,1.3,1.4,1.5,1.6,1.7,1.8,1.9. 1.10,1.11,1.12,1.13,1.14
		SO1.3		
		SO1.4		
		SO1.5		
PO 1,2,3,4,5,6 7,8,9,10,11,12	CO2-78MS102.2 Rearrangements of terms of a	SO2.1		Unit-2 Rearrangements of term of series
PSO 1,2, 3, 4	series	SO2.2		2.1, 2.2, 2.3, 2.4,2.5
		SO2.3		
PO 1,2,3,4,5,6	CO3-78MS102.3 Students will be	SO3.1		Unit-3 Uniform Convergence of
7,8,9,10,11,12	able to describe all elements in	SO3.2		Sequence
PSO 1,2, 3, 4	Uniform Convergence of Sequence	SO3.3 SO3.4		3.1, 3.2, 3.3, 3.4, 3.5, 3.6, 3.7, 3.8,3.9,3.10,3.11,3.12,3.13,2.14,3 .15.
PO 1,2,3,4,5,6		SO4.1		Unit-4
7,8,9,10,11,12 PSO 1,2, 3, 4	CO4-78MS102.4 Students will compute the expression of	SO4.2		4.1, 4.2, 4.3, 4.4, 4.5, 4.6, 4.7,4.8,4.9,4.10,4.11,4.12
	Linear transformations	SO4.3		
PO 1,2,3,4,5,6 7,8,9,10,11,12	<b>CO5-78MS102.5</b> Students will create the concept of a Differential	SO5.1		Unit-5 5.1, 5.2, 5.3, 5.4, 5.5,
PSO 1,2, 3, 4	forms, Stoke's theorem	SO5.2		5.6,5.7,5.8,8.9,5.10,5.11,5.12,5.1 3,5.14
		SO5.3		5,5.17
		SO5.4		
		1		

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#### Semester-I

Course Title: Topology
Course Code: - 78MS103

Prerequisite: Students should review the fundamentals of B.Sc. class in

topics of series and functions and basic knowledge of

differential and integration.

Rationale: The program aims to develop abstract and hypothetical

thinking problem-solving

and analytical skills and prepares students for careers in academia, research, industry, or other sectors that

require advanced mathematical expertise.

### **Course Outcomes (CO):**

#### CO1-78MS103.1

Define and understand the concept of sets, theorems based on countable and uncountable sets, algebraicallyhypotheiss of continum ,topolocal space .Apply to know the interior , exteriorand boundary point, limit points. Continuous functions and homeomorphism.

#### CO2-78MS103.2

Define and understand the basic concepts of countable spaces I and II ,lindelofftheorem, seperable space compactness and finite intersection property sequentially and countably compact set , logical compactness connectness on real line component and locally connectness spaces

### CO3- - 78MS103.3

Define and computeseperations axiomsT0,T1,T2,T3,T4and their characteristics and basic properties .lemma of uryshons and tietz extension

### CO4- - 78MS103.4

Understand the definition of product compact space ,connected space, and path connectedness, path component tychnoff product space in terma of subspace and its characterization projection map.

### CO5- - 78MS103.5

Understand and state the embedding and metrization .embedding lemma and tychnoff embedding . the uryshonsmetrizationtheorem . nets and filters . topology convergence of nets ,hausdroffness and nets . compactness and nets filters and their convergence. Canonoical way of converting nets and filters and vice versa. Ultrafilter and compactness.



### Curriculum & Syllabus of M.Sc. Mathematics program

#### Scheme of Studies:

Board of Study	Course Code	Course Code Course Scheme of studies (Hours/Week) Title						
Juay			Cl	LI	SW	SL	Total Study Hours (CI+LI+SW+SL)	(C)
PCC	78MS103	Topology	4[3+1]	0	1	1	6	4

### Legend:

**CI:** Classroom Instruction (Includes different instructional strategies i.e. Lecture (L) and Tutorial (T) and others)

LI: Laboratory Instruction (Includes Practical performances in laboratory workshop, field or other locations using different instructional strategies)

**SW:** Sessional Work (includes assignment, seminar, mini project etc.)

SL: Self Learning,

**C**:Credits

**Note:** SW & SL has to be planned and performed under the continuous guidance and feedback of teacher to ensure outcome of Learning.

#### Scheme of Assessment:

### Theory

HILLO	Theory									
Board of	Couse Code	Course Title	Scheme of Asse	ssment ( Mai	rks )					
Study			Progressi	Progressive Assessment ( PRA )						
			Class/Home Assignment 5 number 3 marks each ( CA)	Class Test 2 (2 best out of 3) 10 marks each (CT)	Seminar one (SA)	Class Activity any one (CAT)	Class Attendanc e (AT)	Total Marks (CA+CT+SA +CAT+AT)		
PCC	78MS103	Topology	15	20	5	5	5	50	50	100

### **Course-Curriculum Detailing:**

This course syllabus illustrates the expected learning achievements, both at the course and session levels, which students are anticipated to accomplish through various modes of instruction including Classroom Instruction (CI), Laboratory Instruction (LI), Sessional Work (SW), and Self Learning (SL). As



the course progresses, students should showcase their mastery of Session Outcomes (SOs), culminating in the overall achievement of Course Outcomes (COs) upon the course's conclusion.

### CO1- - 78MS103.1

Define and understand the concept of sets, theorems based on countable and uncountable sets, algebraicallyhypotheiss of continum ,topolocal space .Apply to know the interior , exterior and boundary point, limit points. Continuous functions and homeomorphism.

**Approximate Hours** 

Item	AppXHrs
Cl	12
LI	0
SW	1
SL	1
Total	14

Session Outcomes (SOs)	Laboratory Instruction (LI)	Class room Instruction (CI)	Self Learning (SL)
SO1.1		Unit-1.0	SL.1
Understand the concept of			State and prove
sets and countable of		1.1.countable and	schreoder Bernstein
numbers or		uncountable sets.	theorem
uncountablility.		1.2. cardinal number and its	
SO1.2	-	arithmetic.	SL.2
Understand the topological		1.3. schreoderbernstein	Apply topological spce
space with their properties		theorem	to find bases , closure ,
and theorems.		1.4.cantor theorem and	interior , exterior and
SO1.3		continuum hypotheis	boundary point , limit
Apply limit points , interior		1.5 topological space ,bases,	point.
and exterior and boundary		1.6 Tutorial-1	SL.3
points.		1.7. subspace	Apply theorems and
So1.4		neighbourhood,	problem based on
Understand the bases and		1.8. closure,inferior	continuous functions
subspace of a topological		1.9exterior ,boundary	and homeomorphism
space.		1.10 limit points	and equivalence
So1.5		1.11continous function and	relation.
Understand the concept of		homeomorphism	



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continuous and	1.12 Tutorial- 2	
homeomorphism.		

### SW-1 Suggested Sessional Work (SW):

### a. Assignments:

- i. State and prove schreoder Bernstein theorem.
- ii. Define topological space with their properties.
- iii. Apply topological aspace and find bases, subspaces, interior point exterior points and boundary points and limit points as well as closure points.

### b. Mini Project:

Oral presentation, Poster presentation, Power Point Presentation.

**c.** Other Activities (Specify): Quiz, Class Test.

### CO2-78MS103.2

Define and understand the basic concepts of countable spaces I and II ,lindelofftheorem,seperable space compactness and finite intersection property sequentially and countably compact set , logical compactness.connectness on real line component and locally connectness spaces

#### **Approximate Hours**

AppXHrs
12
0
1
1
14

Session Outcomes (SOs)	Laboratory Instruction (LI)	Class room Instruction (CI)	Self Learning (SL)



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SO2.1		Unit-2.0	SL.1
Define and		2.1.countable space I & II	Explore more advanced
understand the		2.2. lindeloff theorem	topics, compactness
basic concepts of		2.3.seperable space	and finite intersection
first and second		2.4-compactness	property
countable space.	-	2.5. finite intersection	SL.2
SO2.2		property	Understand
Perform seperable		2.6. sequentially and	sequentially and
space and		countabliy compact sets	countably compactness
compactness and		2.7. logical comactness	SL.3
finite intersection		2.8. separated sets and	Apply connectness on a
property.		connected spaces.	real line and locally
SO2.3		2.9. connectness on a real	connectned space.
Understand the		line	
sequentially and		2.10 component	
countabily		2.11 locally connected space	
compact sets and		2.12 Tutorial-1	
logicalcompactnes			
S.			
SO2.4			
Define and			
separated sets			
connected space			
SO2.5			
Understand			
connectness on a			
real line.			

### SW-2 Suggested Sessional Work (SW):

### a. Assignments:

- i. Write the first and second countable space.
- ii. Write the sequentially and countabily compact set and logically compactness.
- iii. Write a short note on separated sets and connected space.
- iv. Describe the method of connectness on a real line.

### b. Mini Project:

Oral presentation, Poster presentation, Power Point Presentation.



**c.** Other Activities (Specify): Quiz, Class Test.

### CO3-78MS103.3

Define and computeseperations axiomsT0,T1,T2,T3,T4and their characterstics and basic properties .lemma of uryshons and tietz extension

### **Approximate Hours**

Item	AppXHrs
Cl	12
LI	0
SW	1
SL	1
Total	14

Session Outcomes (SOs)	Laboratory Instruction	Class room Instruction (CI)	Self Learning (SL)
	(LI)		



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SO3.1	Unit-3.0	SL.1
Define and		Apply seperations
Compute separation	3.1. separation axioms	axioms with examples.
axioms	3.2. T0 space	SL.2
SO3.2	3.3. T1 space	Applycharactersctics
Understand the	- 3.4. T2 space	and basic properties of
T0,T1,T3,T4 spaces	3.5. T3 space	seperationsaxioms
SO3.3	3.6.T4 space	SL.3
Apply the chain rule to	3.7. characterization	Solve and prove
compute basic properties	3.8basic properties	uryshons lemma and
of seperations axioms.	3.9. uryshons lemma	tietz extension
SO3.4	3.10. tietz extension	theorem.
Understand mixed	theorem	
characterization of	3.11 theorems on	
seperations axioms	seperations axioms	
theorem	3.12 Tutorial-1	
SO3.5		
Identify uryshons lemma		
and tietz extension		
theorem.		

### SW-2 Suggested Sessional Work (SW):

### a. Assignments:

- i. Write the seperations axioms with exmples.
- ii. Explain the characterization and basic properties of separation axioms.
- iii. Write the uryshons lemma and tietz extension theorem.

### b. Mini Project:

Oral presentation,

**c.** Other Activities (Specify):

Quiz, Class Test.

### CO4-78MS103.4



Understand the definition of product compact space ,connected space, and path connectedness , path component . tychnoff product space in terma of subspace and its characterization projection map.

**Approximate Hours** 

Item	AppXHrs
Cl	12
LI	0
SW	1
SL	1
Total	14

Session Outcomes	Laboratory	Class room Instruction	Self Learning
(SOs)	Instruction	(CI)	(SL)
604.4	(LI)	11	C1 4
SO4.1		Unit-4.0	SL.1
Understand the			Apply product of
definition of a product		4.1.product of compact space	compact space.
of compact space.		4.2connectd space	SL.2
SO4.2		4.3.path connectedness	Apply path
Solve and apply path	-	4.4. Path components	connectedness and
connectedness and		4.5 Tutorial-1	path components.
path components		4.6. tychnoff product topology in	SL.3
SO4.3		terms of topological spaces.	Analyze tychnoff
Identify tychnoff		4.7. its characterization projection	product topology in
product topology.		map.	terms of topological
SO4.4		4.8.theorem on product space.	space.
Identify		4.9.theorem on connected space	
The characterization		4.10. theorem on path	
map.		connectedness	
SO4.5		4.11theorem on path components.	
Recognize the		4.12 Tutorial-2	
theorem on product			
topology in compact			
and connectned			
space.			

SW-2 Suggested Sessional Work (SW):

### a. Assignments:



- I. Explain the product space in a compact space and connectedness.
- **b.** Other Activities (Specify): Quiz, Class Test.

#### CO5-78MS103.5

Understand and state the embedding and metrization .embedding lemma and tychnoff embedding . the uryshonsmetrizationtheorem . nets and filters . topology convergence of nets ,hausdroffness and nets . compactness and nets filters and their convergence. Canonoical way of converting nets and filters and vice versa. Ultrafilter and compactness.

### **Approximate Hours**

Item	AppXHrs
Cl	12
LI	0
SW	1
SL	1
Total	14

Session Outcomes (SOs)	Laboratory Instruction (LI)	Class room Instruction (CI)	Self Learning (SL)
SO4.1		Unit-5.0	SL.1
Understand the			Apply embedding and
embedding and		5.1.Embedding and	metrization theorem
metrization.		metrization	and prove.
SO4.2		5.2. embedding lemma	SL.2
Find embedding	-	5.3. tychnoff embedding	Use tychnoff
lemma and		5.4 the uryshonsmetrization	embedding and the
tychnoff		theorem	uryshonsmetrization
embedding		5.5. nets and filters	theorem
SO4.3		5.6 topology and	SL.3
Understand the		convergence of nets	Apply nets and filters
uryshonsmetrizati		5.7. hausdroffness and nets	and convergence of
on theorem		5.8 compactness and nets	nets and canonical way
SO4.4		filtersand their convergence	of converting nets ato
Interpret nets and		5.9. canonical way of	filters and vice versa.
filters		converting nets to filters	
SO4.5		and vice versa	



Understand	5.10. ultrafilters	
convergence of	5.11compactness	
nets and filters	5.12 Tutorial-1	
and vice versa.		

### **SW-2 Suggested Sessional Work (SW):**

### a. Assignments:

- i. Write the short note on embedding and metrization .
- ii. Write about nets and filter with their convergene and converting nets to filters and vice versa.

### b. Mini Project:

Power Point Presentation.

**c.** Other Activities (Specify): Quiz, Class Test.

### **Brief of Hours suggested for the Course Outcome**

Course Outcomes	Class	Sessional Work	Self Learning	Total hour
	Lecture (CI)	(SW)	(SI)	(CI+SW+SI)
CO1-78MS103.1	12	1	1	14
Define and understand the concept of				
sets, theorems based on countable and				
uncountable sets, algebraicallyhypotheiss				
of continum ,topolocal space .Apply to				
know the interior , exterior and boundary				
point, limit points. Continuous functions				
and homeomorphism				
CO2-78MS103.2 Define and understand	12	1	1	14
the basic concepts of countable spaces I				
and II ,lindelofftheorem,seperable space				
compactness and finite intersection				
property sequentially and countably				
compact set , logical				



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compactness.connectness on real line component and locally connectness spaces				
CO3-78MS103.3  Define and computeseperations axiomsT0,T1,T2,T3,T4and their	12	1	1	14
characterstics and basic properties .lemma of uryshons and tietz extension				
CO4-78MS103.4 Understand the definition of product compact space ,connected space, and	12	1	1	14
path connectedness , path component . tychnoff product space in terma of subspace and its				
characterization projection map.				
CO5-78MS103.5  Understand and state the embedding and metrization .embedding lemma and tychnoff embedding . the uryshonsmetrizationtheorem . nets and filters . topology convergence of nets ,hausdroffness and nets . compactness and nets filters and their convergence. Canonoical way of converting nets and filters and vice versa. Ultrafilter and compactness.	12	1	1	14
Total Hours	60	5	5	70

### **Suggestion for End Semester Assessment**

Suggested Specification Table (For ESA)

СО	Unit Titles	Marks Distribution	Total
			Marks



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		R	U	Α		
CO-1		02	04	05		07
	Countable and topological					
	space					
CO-2		03	07	04		14
	Compactness and connectedness					
CO-3		02	06	02		10
	Seperations axioms					
CO-4		03	03	02		11
	Product topology					
CO-5		03	02	02		08
	Embedding and metrizations.					
Total		13	22	15	•	50

Legend: R: Remember, U: Understand, A: Apply

The end of semester assessment for Introduction to Portland cement will be held with written examination of 50 marks

**Note**. Detailed Assessment rubric need to be prepared by the course wise teachers for above tasks. Teachers can also design different tasks as per requirement, for end semester assessment.

### **Suggested Instructional/Implementation Strategies**

- 1. Improved Lecture
- 2. Tutorial
- 3. Presentation
- 4. Group Discussion
- 5. Online sources
- 6 .Seminar
- 7. Workshop

### **Suggested Learning Resources:**

a) Books:

S.	Title	Author	Publisher	Edition & Year
N				
о.				



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1	Topology	J. R. munkers	Prentice-hall of india	A first edition
2	Introduction to topology	G.F simmons	Tata McGraw Hill	Second editions
3	topology	James R munkers	Pearson education	2 <sup>nd</sup> Edition 2006
4	general topology	J.L kelly	Springer verlag	New York 1966

### **Curriculum Development Team**

- 1. Dr.Sudha Agrawal, HOD, Department of Mathematics.
- 2. Dr.Ekta Shrivastava, Assistant Professor, Department of Mathematics.
- 3. Mr. Neelkanth Napit, Assistant Professor, Department of Mathematics.
- 4. Mrs. Vandana Soni, Assistant Professor, Department of Mathematics.
- 5. Mr.Radhakrishna Shukla, Assistant Professor, Department of Mathematics.
- 6. Mr.Ghanhyam sen, Assistant Professor, Department of Mathematics.
- 7. Ms. Pushpa Kushwaha, Assistant Professor, Department of Mathematics.
- 8. Ms. Arpana Tripathi, Assistant Professor, Department of Mathematics

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### **Cos, POs and PSOs Mapping**

**Course Title: M.Sc. Mathematics** 

Course Code: 78MS103 Course Title: Topology

	PO1	PO	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10	PO1	PO1	PSO 1	PSO	PSO 3	PSO
Course	Adv	2 Pr	Res	Qua	Teachi	The	Comm	Opera	Applic	Engine	1 Gov	2 Con	Understand	2 Han	Develop	4 Cre
Outcome	anc	ob	earc	ntita	ng and	oreti	unicati	tions	ation	ering	ern	sulti	the	dle	necessar	ates
	ed	le	h	tive	Acade	cal	on	Resear	in	and	men	ng	mathematical	the	y skills	Mat
	Mat	m-	Abili	Anal	mia	Und	Skills	ch	Indust	Techn	t		concepts and	adv	and	hem
	he	sol	ties	ysis		erst andi			ry	ology	and Publ		applications in the field of	anc ed	expertis e in the	atic al
	mat ical	vi ng				ng					ic		algebra	tec	field of	Mo
	Kno	Ski				8					Sect		a.gca.a	hni	research	dels
	wle	lls									or			que		
	dge													S		
CO1-	2	3	1	2	1	2	2	2	1	1	1	1	<u>2</u>	<u>1</u>	<u>1</u>	<u>3</u>
78MS103.1													_	_	Ī	_
Defineand																
understand																
the concept of																
sets, theorems																
based on																
countable and																
uncountable																
sets,																
algebraically																
hypotheiss																
of continum																
,topolocal																
space .Apply to																
know the																
interior ,																
exterior and																
boundary point,																
limit points.																
Continuous																
functions and																
homeomorphis																
m .																
CO2-	1	3	2	1	1	1	1	1	1	2	3	1	<u>3</u>	1	<u>1</u>	2



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78MS103.2																
Define and																
understand the																
basic concepts																
of countable																
spaces I and II																
,lindelofftheore																
m,seperable																
space																
compactness																
and finite																
intersection																
property																
sequentially																
and countably																
compact set ,								1								
logical																
compactness.co																
nnectness on																
real line																
component and																
locally																
connectness																
spaces																
CO3-	2	3	2	2	1	1	3	2	1	1	3	1	<u>2</u>	<u>1</u>	<u>2</u>	2
78MS103.3																
Define and																
computesepera																
tions																
axiomsT0,T1,T2																
,T3,T4and their																
characterstics																
and basic																
properties																
.lemma of																
uryshons and																
tietz extension	_	_					_	_			_				_	_
CO4-	2	3	2	2	1	1	3	2	1	1	3	1	<u>2</u>	<u>1</u>	2	2
78MS103.4								1								
Understand the								1								
definition of								[								
product								1								
compact space								1								
,connected																
space, and path connectedness,																



### Curriculum & Syllabus of M.Sc. Mathematics program

			1	1	1		l	l	l	1	I	I				
path																
component																
tychnoff																
product space																
in terma of																
subspace and																
its																
characterization																
projection map.																
CO5-	2	3	2	2	1	1	3	2	1	1	3	1	<u>2</u>	<u>1</u>	<u>2</u>	3
78MS103.5																
Understand and																
state the																
embedding and																
metrization																
embedding																
lemma and																
tychnoff																
embedding .																
the																
uryshonsmetriz																
ationtheorem.																
nets and filters.																
topology																
convergence of																
nets ,																
hausdroffness																
and nets.																
compactness																
and nets filters																
and their																
convergence.																
Canonoical way																
of converting																
nets and filters																
and vice versa.																
Ultrafilter and																
compactness																
compacticos	<u> </u>	<u> </u>	1	<u> </u>	L	L	l	L	L	l	l	l				

Legend: 1 – Low, 2 – Medium, 3 – High



### Curriculum & Syllabus of M.Sc. Mathematics program

### **Course Curriculum Map:**

PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2,3,4 A Political PSO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2,3,4 Political Pso 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2,3,4 PSO 1,	POs & PSOs No.	COs No.& Titles	SOs No.	Laborator	Classroom Instruction (CI)	Self Learning (SL)
PO 1,2,3,4,5,6   Col-78MS103.1   Defineand understand the concept of sets, theorems based on countable and uncountable sets, algebraically hypothesis of continum, topolocal space Apply to know the interior exterior and boundary point, limit points. Continuous functions and homeomorphism						
7.8,9,10,11,12 PSO 1,2, 3, 4 P						
Sol.	PO 1,2,3,4,5,6				•	
Sol.						SL1.2
uncountable sets, algebraically hypothelss of continum, topolocal space Apply to know the interior, exterior and boundary point, limit points. Continuous functions and homeomorphism  PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2,3,4,5,6	PSO 1,2, 3, 4	1 · · · · · · · · · · · · · · · · · · ·			1.8,1.9,1.10	
PO 1,2,3,4,5,6   7,8,9,10,11,12   PSO 1,2,3,4,5,6   PSO 1,2,3,4   PSO			SO1.5			
Apply to know the interior, exterior and boundary point, limit points. Continuous functions and homeomorphism  PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2,3,4,5 PO 1,2,3,4,5,6 PO 1,2,3,4,5,6 PO 1,2,3,4,5,6 PO 1,2,3,4,5,6 Residual points and property sequentially and countably compact set , logical compactness.connectness on real line component and locally connectness spaces or pressure properties. Jemma of uryshons and tietz extension properties. Jemma of uryshons and tietz extension product compact space, connected space, and path connectedness , path component. Lychnoff product compact space, connected component. Lychnoff product component. L		, ,,				
PO 1,2,3,4,5,6						
Ilimit points. Continuous functions and homeomorphism						
Functions   And homeomorphism   Sol.1   Sol.2   Sol.3   Sol.4   Sol.5   Sol.						
PO 1,2,3,4,5,6		· •				
7,8,9,10,11,12 PSO 1,2, 3, 4  PSO 1,		homeomorphism				
PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2, 3, 4  PSO 1,					_	
PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2,3,4						3L2.2
pO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2,3,4,4 Oronected space, connected space, and path component . tychnoff product intersection property sequentially and countably compact set , logical compactness.connectness on real line component and locally connectness spaces  PO 1,2,3,4,5,6 CO3-78MS103.3 Sol.2 Sol.3 Sol.4 Sol.2 Sol.3 Sol.4 Sol.4 Sol.5 Sol.4 Sol.5 Sol.4 Sol.5 Sol.5 Sol.5 Sol.5 Sol.5 Sol.6	PSO 1,2, 3, 4	1	SO1.4		2.7, 2.8,2.9,2.10	
intersection property sequentially and countably compact set , logical compactness.connectness on real line component and locally connectness spaces  PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2,3,4,5,6 roperties .lemma of uryshons and tietz extension  PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2,3,4,4 formore tedness , path component . tychnoff product  PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2,3,4,4 formore tedness , path component . tychnoff product  PSO 1,2,3,4,5,6 roperties .lemma of uryshons and tietz extension  PO 1,2,3,4,5,6 roperties .lemma of uryshons and tietz extension  PSO 1,2,3,4,5,6 roperties .lemma of uryshons and tietz extension  PSO 1,2,3,4,5,6 roperties .lemma of uryshons and tietz extension  PSO 1,2,3,4,5,6 roperties .lemma of uryshons and tietz extension  PSO 1,2,3,4,5,6 roperties .lemma of uryshons and tietz extension  PSO 1,2,3,4,5,6 roperties .lemma of uryshons and tietz extension  PSO 1,2,3,4,5,6 roperties .lemma of uryshons and tietz extension  PSO 1,2,3,4,5,6 roperties .lemma of uryshons and tietz extension  PSO 1,2,3,4,5,6 roperties .lemma of uryshons and tietz extension  PSO 1,2,3,4,5,6 roperties .lemma of uryshons and tietz extension  PSO 1,2,3,4,5,6 roperties .lemma of uryshons and tietz extension  PSO 1,2,3,4,5,6 roperties .lemma of uryshons and tietz extension  PSO 1,2,3,4,5,6 roperties .lemma of uryshons and tietz extension  PSO 1,2,3,4,5,6 roperties .lemma of uryshons and tietz extension  PSO 1,2,3,4,5,6 roperties .lemma of uryshons and tietz extension  PSO 1,2,3,4,5,6 roperties .lemma of uryshons and tietz extension  PSO 1,2,3,4,5,6 roperties .lemma of uryshons and tietz extension  PSO 1,2,3,4,5,6 roperties .lemma of uryshons and tietz extension  PSO 1,2,3,4,5,6 roperties .lemma of uryshons and tietz extension  PSO 1,2,3,4,5,6 roperties .lemma of uryshons and tietz extension  PSO 1,2,3,4,5,6 roperties .lemma of uryshons and tietz extension  PSO 1,2,3,4,5,6 roperties .lemma of uryshons and tietz extension  PSO 1,2,3,4,5,6 roperties .lemma of uryshons and tietz ext		,lindelofftheorem,seperable	SO1.5			
sequentially and countably compact set , logical compactness.connectness on real line component and locally connectness spaces  PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2,3,4 PSO 1,2,3,4 PSO 1,2,3,4,5,6  Od-78MS103.4 PO 1,2,3,4,5,6 T,8,9,10,11,12 PSO 1,2,3,4 From the definition of product compact space connected space, and path connected space, and path connectedness , path component tychnoff product  PSO 1,2,3,4 From the definition of product compact space connected space, and path connectedness , path component tychnoff product  PSO 1,2,3,4 From the definition of product compact space connected space, and path connectedness , path component tychnoff product  PSO 1,2,3,4 From the definition of product compact space connected space, and path connectedness , path component tychnoff product  PSO 1,2,3,4,5,6 From the definition of product compact space connected space, and path connectedness , path component tychnoff product  PSO 1,2,3,4,5,6 From the definition of product compact space connected space, and path connectedness , path component tychnoff product  PSO 1,2,3,4,5,6 From the definition of product compact space connected space, and path connectedness , path component tychnoff product  PSO 1,2,3,4,5,6 From the definition of product compact space connected space, and path connectedness , path component tychnoff product  PSO 1,2,3,4,5,6 From the definition of product compact space connected space, and path connectedness of the definition of product compact space connected space connec		1 -				
compact set , logical compactness.connectness on real line component and locally connectness spaces  PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2,3,4 Note that the definition of product compact space connected space, and path connectedness , path component . tychnoff product  Compact set , logical compact set set set set set set set set set se						
compactness.connectness on real line component and locally connectness spaces  PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2,3,4 PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2,3,4 PSO 1,2,4						
PO 1,2,3,4,5,6   CO3-78MS103.3   Define and computeseperations axiomsT0,T1,T2,T3,T4and their characterstics and basic properties .lemma of uryshons and tietz extension   PO 1,2,3,4,5,6   7,8,9,10,11,12   PSO 1,2, 3, 4   Understand the definition of product compact space ,connected space, and path component . tychnoff product   tychn		_				
PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2,3,4 From the component of the comp		-				
7,8,9,10,11,12 PSO 1,2,3,4  PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2,3,4  Computeseperations axiomsT0,T1,T2,T3,T4and their characterstics and basic properties .lemma of uryshons and tietz extension  PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2,3,4  Cod-78MS103.4 Understand the definition of product compact space connected space, and path connectedness , path component . tychnoff product  PSO 1,2,3,4  Cod-78MS103.4 Understand the definition of product compact space connected space, and path connectedness , path component . tychnoff product  Computeseperations So1.2 SO1.3 SO1.4 SO1.5  Unit-4 2.1, 2.2, 2.3, 2.4, 2.5, 2.6, 2.7, 2.8,2.9,2.10  SL4.1 So1.3 SO1.4 SO1.5  Cod-78MS103.4 Cod-78MS103.4 SO1.1 SO1.2 SO1.3 SO1.4 SO1.5 SO1.4 SO1.5 SO1.4 SO1.5 SO1.4 SO1.5 Computeseperations axiomsT0,T1,T2,T3,T4and their characterstics and basic properties .lemma of uryshons and tietz extension  Unit-4 2.1, 2.2, 2.3, 2.4, 2.5, 2.6, 2.7, 2.8,2.9,2.10  SL4.1 SO1.5 Computeseperations SU3.2 SO1.4 SO1.5		1				
PSO 1,2, 3, 4  PSO 1,						
axiomsT0,T1,T2,T3,T4and their characterstics and basic properties .lemma of uryshons and tietz extension  PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2,3,4 PSO 1,2,3,4 Component . tychnoff product  PO 1,2,3,4,5,6 Todate and basic properties .lemma of uryshons and tietz extension  PO 1,2,3,4,5,6 Todate and basic properties .lemma of uryshons and tietz extension  Sol.4 Sol.5  Unit-4 2.1, 2.2, 2.3, 2.4, 2.5, 2.6, 2.7, 2.8,2.9,2.10						323.2
PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2,3,4 PSO 1,2,3,4 Component . tychnoff product  Their characterstics and basic properties .lemma of uryshons and tietz extension  Sol.1 Sol.2 Sol.2 Sol.3 Sol.4 Sol.5 Sol.4 Sol.5 Sol.4 Sol.5	P3U 1,2, 3, 4				2.7, 2.8,2.9,2.10	
uryshons and tietz extension  PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2, 3, 4 PSO 1,2, 3, 4 CO4-78MS103.4 Understand the definition of product compact space, connected space, and path connectedness , path component . tychnoff product  Unit-4 2.1, 2.2, 2.3, 2.4, 2.5, 2.6, 2.7, 2.8,2.9,2.10  2.7, 2.8,2.9,2.10			501.5			
PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2,3,4 PSO 1,2,3,4,5,6 Product compact space		1				
7,8,9,10,11,12 PSO 1,2, 3, 4 Understand the definition of product compact space, connected space, and path connectedness , path component . tychnoff product  Understand the definition of product space, sol.2 Sol.3 Sol.4 Sol.5	DO 1 2 2 4 5 6		SO1 1		Unit 1	SI 4 1
PSO 1,2, 3, 4 product compact space connected space, and path connectedness , path component . tychnoff product compact space						
connected space, and path connectedness , path component . tychnoff product			SO1.3			
connectedness , path component . tychnoff product	. 55 2,2, 5, 1	-				
		, ,	301.3			
space in terma of subspace		space in terma of subspace				
and its characterization		, · · · · · · · · · · · · · · · · · · ·				



### Curriculum & Syllabus of M.Sc. Mathematics program

	projection map.			
PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2, 3, 4	CO5-78MS103.5 Understand and state the embedding and metrization .embedding lemma and tychnoff embedding . the uryshonsmetrizationtheorem . nets and filters . topology convergence of nets , hausdroffness and nets. compactness and nets filters and their convergence. Canonoical way of converting nets and filters and vice versa. Ultrafilter and compactness.	SO1.1 SO1.2 SO1.3 SO1.4 SO1.5	Unit-5 2.1, 2.2, 2.3, 2.4, 2.5, 2.6, 2.7, 2.8,2.9,2.10	SL5.1 SL5.2 SL5.3



### Semester-I

Course Code: 78MS104
Course Title : Complex Analysis-I

perquisite: Students should have basic knowledge of

complex numbers

Rationale: The program aims to develop advanced problem-

solving and analytical skills and prepares students for careers in academia, research, industry, or other sectors that require advanced

mathematical expertise.

#### **Course Outcomes:**

**CO1-78MS104.1** Understand the importance of algebra of complex numbers with regard to working within various number systems.

**CO2-78MS104.2**. Students will determine a given function which is on the closed contour 'c' and the value of integration of this function .

**CO3-78MS104.3**. Students will Calculate Residues in some special cases by using Residue theorem.

CO4-78MS104.4 Students will compute the Expansion of Analytic function as power series by using Taylor and Laurent theorem.

**CO5-78MS104.5** .Students will create the concept of a Mapping or Transformation and their representation

### **Scheme of Studies:**

Board of Study	Course Code	Course Title	Scheme of st		Total Credit			
			CI	LI	SW	SL	Total Study Hours (CI+LI+SW+SL)	s (C)
Program Core (PCC)	78MS104	Complex analysis-l	4[3+1]	0	1	1	6	4



### Legend:

**CI:** Classroom Instruction (Includes different instructional strategies i.e. Lecture (L) and Tutorial (T) and others),

**LI:** Laboratory Instruction (Includes Practical performances in laboratory workshop, field or other locations using different instructional strategies)

**SW:** Sessional Work (includes assignment, seminar, mini project etc.),

SL: Self Learning,

C:Credits.

**Note:** SW & SL has to be planned and performed under the continuous guidance and feedback of teacher to ensure outcome of Learning.

#### **Scheme of Assessment:**

#### Theory

Board	Couse Code	Course Title	So	Scheme of Assessment ( Marks )						
of Study			Progressi	Progressive Assessment ( PRA )  So A (E						
			Class/Home Assignment 5 number 3 marks each ( CA)	Class Test 2 (2 best out of 3) 10 marks each (CT)	Seminar one ( SA)	Class Activity any one (CAT)	Class Attendanc e (AT)	Total Marks (CA+CT+SA +CAT+AT)		
PCC	78MS104	Complex analysis-I	15	20	5	5	5	50	50	100

### **Course-Curriculum Detailing:**

This course syllabus illustrates the expected learning achievements, both at the course and session levels, which students are anticipated to accomplish through various modes of instruction including Classroom Instruction (CI), Laboratory Instruction (LI), Sessional Work (SW), and Self Learning (SL). As the course progresses, students should showcase their mastery of Session Outcomes (SOs), culminating in the overall achievement of Course Outcomes (COs) upon the course's conclusion.

#### CO1-78MS104.1

Understand the importance of algebra of complex numbers with regard to working within various number systems.



### **Approximate Hours**

Item	AppX Hrs
Cl	12
LI	0
SW	1
SL	1
Total	14

Session Outcomes (SOs)	Laboratory Instruction (LI)	Class room Instruction (CI)	Self Learning (SL)
SO1.1 Understand the Algebra of complex numbers.  SO1.2 Understand the relationships between complex numbers structures with familiar numbers systems such as the integers and real numbers  SO1.3 Understand the concept of contur integration  So1.4 Understand the hypothesis of Cauchy's Theorem  So1.5 Understand the concept of function.		Unit-1.0 The Complex Number systems, Analytic functions.  1.1 Introduction of complex numbers 1.2 Geometric representation of complex numbers 1.3 limit, continuity and differentiability of complex function 1.4 Analytic function. 1.5 Tutorial-I 1.6 complex integration 1.7 Cauchy's Theorem. 1.8 Cauchy Gaursat theorem 1.9 Cauchy integral formula. 1.10 Cauchy integral	SL.1 Understand the complex numbers. SL.2 knowledge of the difference and division between two complex numbers. SL.3 Properties of Modulus and Argument of complex numbers.
		formula for derivative of the function 1.11 Cauchy integral formula for Higher order derivatives. 1.12 Tutorial-II	

### SW-1 Suggested Sessional Work (SW):

### a. Assignments:



- i. Relationships between complex numbers structures with familiar numbers systems such as the Set of natural numbers, Set of rational numbers, Set of integers, Set of real numbers, Set of complex numbers. ii. Geometric representation of complex numbers.
- iii. State and proof cauchy Gaursat theorem.
- iv. Cauchy integral formula for Higher order derivative.

### b. Mini Project:

Oral presentation, Poster presentation, Power Point Presentation.

c. Other Activities (Specify):

Quiz, Class Test.

#### CO2-78MS104.2

Students will determine a given function which is on the closed contour c and the value of integration of this function.

Item	AppX Hrs
Cl	12
LI	0
SW	1
SL	1
Total	14

Session Outcomes (SOs)	Laboratory Instruction	Class room Instruction (CI)	Self Learning (SL)
	(LI)		



### Curriculum & Syllabus of M.Sc. Mathematics program

SO2.1	Unit-2.0 Complex	SL.1
Understand the concept	Integration:	Evaluation Elementary
of Moderate 's theorem		function of a complex
	2.1 Morera's theorem	variables
SO2.2	2.2 Cauchy's inequality	SL.2
Learn about structure	2.3 Liousville's theorem	Knowledge of the
	2.4 Certain theorem on power	Analyticity of the sum
preserving maps	series	function of a series
between groups and	2.5 Tutorial-I	runction of a series
their consequences.	2.6 Fundamental theorem of	a. a
SO2.3	algebraic function	SL.3
Understand the concept	2.7the concept of Taylor's series	Knowledge of some
of	2.8 the concept of Taylor's	Elementary properties
Composition series	theorem	of complex numbers.
SO2.4		
Understand the Uses of	2.9 Theorems on inequality	
Composition series in	·	
Jordan-Holder theorem	2.10 Expansion of analytic	
SO2.5	function as power series	
Understand the Relation	2.11 the concept of Laurent	
of Ring and Various	theorem	
polynomials	2.12 Tutorial-I	

### **SW-2 Suggested Sessional Work (SW):**

### a. Assignments:

- i. State and prove Morera's theorem.
- ii. State and prove cauchy inequality.
- iii. State and prove Liousville's theorem.
- iv. State and prove Fundamental theorem of algebra.
- V. Taylor's series.

### b. Mini Project:

Oral presentation, Poster presentation, Power Point Presentation.

c. Other Activities (Specify):

Quiz, Class Test.

### CO3-78MS104.3

Students will Calculate Residues in some special cases by using Residue theorem .



### AKS University Faculty of Basic Science

### Department of Mathematics

### Curriculum & Syllabus of M.Sc. Mathematics program

### **Approximate Hours**

AppX Hrs
12
0
1
1
14

Session Outcomes (SOs)	Laboratory Instruction (LI)	Class room Instruction (CI)	Self Learning (SL)
SO3.1 Understand the principal of Argument  SO3.2 Rouche's theorem  SO3.3 the concept of Maximum Modulus principal		Unit-3.0 principal of Argument and Rouche's theorem  3.1 Maximum Modulus principle.  3.2 Minimum Modulus principle.  3.3 the concept of Schwartz lemma.  3.4 Laurent's series.  3.5 Tutorial –I  3.6 Meromorphic function.  3.7 The poles and zeros of a Meromorphic function .  3.8 singular and classification of singularity .  3.9 some Theorems on poles .  3.10 Inverse function theorem  3.11 The concept of Argument principle.  3.12 Tutorial –II	Knowledge of the poles and zeros of a Meromorphic function.  SL.2  Understand an application of Rouche's theorem.

### **SW-3 Suggested Sessional Work (SW):**

### a. Assignments:

- i. The concept of Argument principle.
- ii. Application of Rouche's theorem .
- iii. Definition of Meromorphic function.
- iv. State and prove Maximum Modulus theorem.
- V. Schwarz lemma.

### b. Mini Project:

Oral presentation, Poster presentation, Power Point Presentation.



**c.** Other Activities (Specify): Quiz, Class Test.

### CO4-78MS104.4

Students will compute the Expansion of Analytic function as power series by using Taylor and Laurent theorem.

### **Approximate Hours**

Item	AppX Hrs
Cl	12
LI	0
SW	1
SL	1
Total	14

Session Labo	oratory	Class room Instruction	Self Learning (SL)
Outcomes Instr	truction	(CI)	
(SOs) (LI)			
SO4.1 Understand the concept of Residues at a singularity SO4.2 Residues at infinity  SO4.3 Understand the importance of Residues theorem		Unit -4 Residue Theory and Calculus of Residue.  4.1 Understand the Residue.  4.2 Cauchy Residue theorem.  4.3 Evaluation of Integrals.  4.3 Branches of many valued function  4.4 Residue at infinity  4.5 Tutorial —I  4.6 The residue at a singularity.  4.7 Special reference to arg z, log z  4.8 Evaluation of definite Integrals by contour integration  4.9 some residue theorem  4.10 Residue at a simple poles  4.11 Integration round the unit circle  4.12 Tutorial —I	• Calculation of Residues in some special cases. • Evaluation of definite integral by contour integration.

SW-4 Suggested Sessional Work (SW):



### a. Assignments:

- i. Evaluation of definite integral by contour integration.
- ii. Application of Residues theorem.
- iii. State and prove cauchy residue theorem .
- iv. Calculation of residues in some special cases.
- V. Evaluation of integrals.

### b. Mini Project:

Oral presentation, Poster presentation, Power Point Presentation.

c. Other Activities (Specify):

Quiz, Class Test.

### CO5-78MS104.5

Students will create the concept of a Mapping or Transformation and their representation.

### **Approximate Hours**

Item	AppX Hrs
Cl	12
LI	0
SW	1
SL	1
Total	14

Session Outcomes (SOs)	Laboratory Instruction (LI)	Class room Instruction (CI)	Self Learning (SL)



### Curriculum & Syllabus of M.Sc. Mathematics program

SO5.1 Understand the concept of Mapping or	Unit-5.0 Understand the Bilinear Transformations &	SL.1 knowledge of the
Transformation. SO5.2 Product of two Bilinear Transformation.	Conformal Mappings. 5.1 The concept of Mappings or Transformation. 5.2 Bilinear Transformation. 5.3 their properties and	linear Transformation.  SL.2 The
SO5.3 Conformal mapping.	5.3 their properties and Classification. 5.4 Definition and Example of conformal mapping. 5.5 Tutorial -I 5.6 Space of analytic function. 5.7 Hurwitz theorem. 5.8 Montel's. theorem. 5.9 Riemann mapping. 5.10jacobian of a Transformation. 5.11 Some Elementary Transformation. 5.12 Tutorial -II	Representation of a conformal mapping.

### **Brief of Hours suggested for the Course Outcome**

Course Outcomes	Class Lecture (CI)	Sessional Work (SW)	Self Learning (SI)	Total hour (Cl+SW+SI)
<b>CO1-78MS104.1</b> Understand the importance of algebra of complex numbers with regard to working within various number systems.	-	1	1	12



### Curriculum & Syllabus of M.Sc. Mathematics program

CO1-78MS104.2				12
Students will determine a	12	1	1	
given function which is				
on the closed contur c '				
and also find the value of				
integration of this				
function .				12
CO3-78MS101.3	12	1	1	12
Students will Calculate	12	1	1	
Residues in some special				
cases by using Residue				
theorem .	12	4	4	12
CO4-78MS101.4	12	1	1	12
Students will compute				
the Expansion of Analytic				
function as power series by				
using Taylor and Laurent				
theorem.	42	4	4	4.2
CO1-78MS104.5 Students will	12	1	1	12
create the concept of a Mapping				
or Transformation and their				
representation.				
Total Hours	60	5	5	70

### • Suggestion for End Semester Assessment

Suggested Specification Table For(ESA)

со	Unit Titles	Marks Distril	Total Marks		
		R	U	Α	



### Curriculum & Syllabus of M.Sc. Mathematics program

CO-1	Understand the importance of algebra of complex numbers with regard to working within various number systems.	03	01	01	05
CO-2	Students will determine a given function which is on the closed contur c 'and also find the value of integration of this function.	02	05	03	10
СО-3	Students will Calculate Residues in some special cases by using Residue theorem.	03	06	06	15
CO-4	Students will compute the Expansion of Analytic function as power series by using Taylor and Laurent theorem.	-	10	05	15
CO-5	Students will create the concept of a Mapping or Transformation and their representation.	03	02	-	05
Total		11	26	13	50

Legend: R: Remember, U: Understand, A: Apply

The end of semester assessment for Introduction to Portland cement will be held with written examination of 50 marks

**Note**. Detailed Assessment rubric need to be prepared by the course wise teachers for above tasks. Teachers can also design different tasks as per requirement, for end semester assessment.



### Curriculum & Syllabus of M.Sc. Mathematics program

### **Suggested Instructional/Implementation Strategies**

- 1. Improved Lecture
- 2. Tutorial
- 3. Presentation
- 4. Group Discussion
- 5. Online sources
- 6 .Seminar
- 7. Workshop

### **Suggested Learning Resources:**

### a) Books:

S.	Title	Author	Publisher	Edition & Year
N				
о.				
1	Complex variables and applications	R.V.Churchill,J.W. Brown	McGraw-Hill,New York,	2nd edition, 1989
2.	Fundamentals of	C Donnuovuonev	Narosa Publishing	4th edition, 1985
	complex analysis	S.Ponnuswamy,	house	
3.	Theory and Problems of	Lars.V.Ahlfors,	McGraw-Hill,New York	
	complex variables		McGraw Hill book company International	Edition, Singapore,1979

### **Curriculum Development Team**

- 1. Dr.Sudha Agrawal, HOD, Department of Mathematics.
- 2. Dr.Ekta Shrivastava , Assistant Professor, Department of Mathematics.
- 3. Mr. Neelkanth Napit, Assistant Professor, Department of Mathematics.
- 4. Mrs. Vandana Soni, Assistant Professor, Department of Mathematics.
- 5. Mr.Radhakrishna Shukla, Assistant Professor, Department of Mathematics.
- 6. Mr.Ghanhyam sen, Assistant Professor, Department of Mathematics.
- 7. Ms. Pushpa Kushwaha, Assistant Professor, Department of Mathematics.
- 8. Ms. Arpana Tripathi, Assistant Professor, Department of Mathematics.



### **Cos, POs and PSOs Mapping**

**Course Title: M.Sc. Mathematics** 

Course Code: 78MS104

**Course Title: Complex Analysis-I** 

Course Outcome	PO1	PO 2	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10	PO11	P O 12	PSO 1	PSO 2	PSO 3	PSO 4
Outcome	Adva nced Mat hem atica I Kno wled ge	Pr ob le m- sol vin g Ski Ils	Research Abilities	Qua ntita tive Anal ysis	Teachi ng and Acade mia	Theo retic al Und ersta ndin g	Comm unicati on Skills	Ope ratio ns Rese arch	Applica tion in Industr y	Engine ering and Techno logy	Gover nment and Public Sector	Co ns ul ti ng	Underst and the mathem atical concepts and applicati ons in the field of algebra	Han dle the adva nced tech niqu es	Develop necessar y skills and expertis e in the field of research	Creat es Math emati cal Mode Is
78MS101.1 Understand the importance of algebraic properties with regard to working within various number systems.	2	1	2	3	2	2	2	3	1	2	2	1	2	<u>3</u>	1	<u>2</u>
CO2- 78MS101.2. Students will determine whether a given binary operation on the given set gives a group structure by applying the axioms.	3	2	2	2	2	3	2	3	1	2	3	1	2	3	1	2
CO3- 78MS101.3. Students will be able to describe all elements in a cyclic subgroup by using generators.	2	3	2	2	3	2	2	1	3	1	2	2	3	2	2	2



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CO4- 78MS101.4 Students will compute the expression of permutation groups by using	2	3	3	2	2	3	2	1	2	3	3	3	2	1	1	2
permutation multiplication.																
CO5- 78MS101.5 Students will create the concept of a group action to real life problems such as Counting.	2	3	3	3	2	2	2	1	2	1	2	2	3	3]	2	2

Legend: 1 – Low, 2 – Medium, 3 – High



### AKS University Faculty of Basic Science Department of Mathematics

### Curriculum & Syllabus of M.Sc. Mathematics program

### **Course Curriculum Map:**

POs & PSOs No.	COs No.& Titles	SOs No.	Laboratory Instruction(L	Classroom Instruction (CI)	Self Learning (SL)
PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2, 3, 4	CO1-78MS101.1 Understand the importance of algebraic properties with regard to working within various number systems.	\$01.1 \$01.2 \$01.3 \$01.4 \$01.5	1	Jnit-1.0 Group I.1,1.2,1.3,1.4,1.5,1.6,1.7,1.8, I.9,1.10	SL1.1 SL1.2
PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2, 3, 4	CO2-78MS101.2.  Students will determine whether a given binary operation on the given set gives a group structure by applying the axioms.	SO1.1 SO1.2 SO1.3 SO1.4 SO1.5	2	Jnit-2 Ring 2.1, 2.2, 2.3, 2.4, 2.5, 2.6, 2.7, 2.8,2.9,2.10	SL2.1 SL2.2
PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2, 3, 4	CO3-78MS101.3. Students will be able to describe all elements in a cyclic subgroup by using generators.	\$01.1 \$01.2 \$01.3 \$01.4 \$01.5	2	Jnit-3 2.1, 2.2, 2.3, 2.4, 2.5, 2.6, 2.7, 2.8,2.9,2.10	SL3.1 SL3.2
PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2, 3, 4	CO4- 78MS101.4 Students will compute the expression of permutation groups by using permutation multiplication.	SO1.1 SO1.2 SO1.3 SO1.4 SO1.5		Jnit-4 2.1, 2.2, 2.3, 2.4, 2.5, 2.6, 2.7, 2.8,2.9,2.10	SL4.1 SL4.2
PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2, 3, 4	CO5-78MS101.5 Students will create the concept of a group action to real life problems such as Counting.	SO1.1 SO1.2 SO1.3 SO1.4 SO1.5	2	Jnit-5 2.1, 2.2, 2.3, 2.4, 2.5, 2.6, 2.7, 2.8,2.9,2.10	SL5.1 SL5.2

\*



#### M.Sc. Semester-I

Course Code:	78MS105
Course Title :	[Research Methodology]
Pre- requisite:	Among then of great importance are first, the actuality of
	the theme of the research; second-the choice of
	adequate research instruments and taxonomy to the
	chosen object field.
Rationale:	Think of a research rationale as a set of reasons that
	explain why a study is necessary and important based on
	its background.

#### **Course Outcome:**

**CO1-78MS105.1** Students will understand research approaches.

**CO2-78MS105.2** With the help of this course, students will be able to take up and implement a research project/ study.

**CO3-78MS105.3.** Define a research problem.

**CO4-78MS105.4** The Students will develop skills in qualitative and quantitative data analysis and presentation.

**CO5-78MS105.5** To teach students different techniques of research modelling, data collection, designing and planning of experiments.

#### **Scheme of Studies:**

Board of	Course	Course Title	Scheme of studies (Hours/Week)						
Study	Code		Cl	LI	sw	SL	Total Study Hours (CI+LI+SW+SL)	ts (C)	
Program Core (PCC)	78MS105	Research Methodolog y	4[3+1]	0	1	1	6	4	

#### Legend:

**CI:** Classroom Instruction (Includes different instructional strategies i.e. Lecture (L) and Tutorial (T) and others),

**LI:** Laboratory Instruction (Includes Practical performances in laboratory workshop, field or other locations using different instructional strategies)

SW: Sessional Work (includes assignment, seminar, mini project etc.),



**SL:** Self Learning, **C:**Credits.

**Note:** SW & SL has to be planned and performed under the continuous guidance and feedback of teacher to ensure outcome of Learning.

**Scheme of Assessment: Theory** 

Boa	Couse Code	Course Title	1	Schem	e of Assess	ment ( M	arks )			
rd			Progi	Progressive Assessment ( PRA )					End	Total
of	78MS105	Research							Semester	Marks
Stu		Methodology							Assessm	(PRA+
dy									ent	ESA)
					1	1			(ESA)	
			Class/Ho	Class	Seminar	Class	Class	Total		
			me	Test 2	one	Activit	Attend	Marks		
			Assignme	(2 best	( SA)	y any	ance	(CA+CT+		
			nt 5	out of		one	(AT)	SA		
			number	3)		(CAT)		+CAT+A		
			3 marks	10				T)		
			each	marks						
			( CA)	each						
				(CT)						
PCC	78MS105	Research	15	20	5	5	5	50	50	100
		Methodology								

#### **Course-Curriculum Detailing:**

This course syllabus illustrates the expected learning achievements, both at the course and session levels, which students are anticipated to accomplish through various modes of instruction including Classroom Instruction (CI), Laboratory Instruction (LI), Sessional Work (SW), and Self Learning (SL). As the course progresses, students should showcase their mastery of Session Outcomes (SOs), culminating in the overall achievement of Course Outcomes (COs) upon the course's conclusion.

**CO1-78MS105.1** Students will understand research approaches.

Item	AppX Hrs
Cl	14
LI	0
SW	1
SL	1
Total	16



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Session Outcomes (SOs)	Laboratory Instruction (LI)	Class room Instruction (CI)	Self Learning (SL)
SO1.1 Understand the concept of research meaning, SO1.2 Understand the research approaches SO1.3 Recognize the mathematical objects of methodology.  SO1.4 Learn about research process SO1.5 Understand the criteria of good research	<u>-</u>	Unit-1.0 1.1 Introduction of Research 1.2 : Meaning, 1.3 Objectives, 1.4 Motivation 1.5 Types of Research 1.6 Research Approaches, 1.4 Significance of Research, 1.5 Research Methods 1.6 tutorial-1 1.7 versus of Research Methodology, 1.8 Research 1.9 Scientific Method, 1.10 Importance of knowing	SL.1 Understand the concept. Research Methodology SL.2 Understand significance of research SL.3 Understand the concept of research process
		<ul> <li>1.11 how research is done,</li> <li>1.12 Research Process,</li> <li>1.13 Criteria of good research,</li> <li>1.14 Problems encountered by researchers in India.</li> </ul>	

#### SW-1 Suggested Sessional Work (SW):

#### a. Assignments:

- i. explain the significance of research,
- ii. write the Criteria of good research, ;
- iii. write Problems encountered by researchers in India

#### b. Mini Project:

Oral presentation, Poster presentation, Power Point Presentation.

**c.** Other Activities (Specify):

Quiz, Class Test.



**78MS105.2:** With the help of this course, students will be able to take up and implement a research project/ study. **Approximate Hours** 

Item	AppXHrs
Cl	11
SW	1
SL	1
Total	13

SessionOutcomes (SOs)	LaboratoryInstruction (LI)	ClassroomInstruction (CI)	SelfLearning (SL)
<b>SO2.1</b> . What is a		UNIT 2	SL.1
research problem		<b>2.1</b> What is a	Learn about
		research problem	research
SO2.2 discuss Selecting the		<b>2.2</b> , Selecting the	problem
problem		problem	
		2.3 Necessity of	
SO2.3		defining the	SL.2
To learn about		problem	Understand the
Necessity of defining		2.4 find the	concept.
the problem		research problem	Selecting the
		2.5 research	problem
SO2.4		problem	
Explain defining a problem		<b>2.6</b> types of	
		research problem	
		<b>2.7</b> Technique	
		involved in	
		problem	
		2.8 Explain	
		Technique	
		2.9 involved in	
		problem	
		<b>2.10</b> defining a	
		problem	
		2.11 tutorial	

#### SW-2 Suggested SessionalWork(SW):

- a. Assignments:-
- (1) Difine the research problem



(2) Understand the basics of Selecting the problem

#### b. MiniProject:

**Power Point Presentation** 

**c.** Other Activities (Specify): Class Test.

CO3-78MS105.3. Define a research problem.

#### **Approximate Hours**

• •	
Item	AppXHrs
Cl	13
LI	0
SW	1
SL	1
Total	15

SessionOutcomes (SOs)	LaboratoryInstr uction (LI)	ClassroomInstruction (CI)	SelfLearning (SL)
<b>SO3.1</b> To Understand the		Unit-3	SL.1
Meaning of Research		<b>3.1.1</b> Meaning of Research	To learn Research
Design		Design	Design
SO3.2To learn Research		<b>3.2</b> Define Research Design	
Design.		<b>3.3</b> Need for Research Design.	SL.2
		3.4 Need for Research Design	
SO3.3Explain Features of a		area	To learn Important
good design		<b>3.5</b> Features of a good design	concepts of
		<b>3.6</b> Important concepts of	Research Design
SO3.4 To Understand		research design	
different type of		3.7 relating to research design	
Research Design		3.8 Tutorial	
		<b>3.9</b> Different research designs.	
		<b>3.10</b> Basic Principles of	
		Experimental Designs.	
		3.11 Types of Experimental	
		Designs.	
		<b>3.12</b> good design	
		<b>3.13</b> problem of good research design	

#### SW-3 SuggestedSessionalWork(SW):

- a. Assignments:-
- (1) Basic Features of a good design
- (2) Different research designs



#### b. MiniProject:

Oral presentation, Poster presentation,

**c.**Other Activities (Specify): Class Test.

**CO4-78MS105.4** The Students will develop skills in qualitative and quantitative data analysis and presentation.

#### **Approximate Hours**

Item	AppXHrs
Cl	12
LI	0
SW	1
SL	1
Total	14

SessionOutcomes (SOs)	LaboratoryInstr uction (LI)	ClassroomInstruction (CI)	SelfLearning (SL)
SO4.1To Understand concept Central Tendency		Unit-4 4.1Statistics in Research 4.2 Measures of Central	Statistics in Research
SO4.2To learn Measures of Relationship SO4.3 To understand Multiple Correlation and Regression		<ul> <li>Tendency</li> <li>4.3 Central Tendency</li> <li>4.4 Measures of Dispersion</li> <li>4.5 Measures of Asymmetry (Skewness)</li> <li>4.6 Measures of Relationship</li> <li>4.7 Simple Regression Analysis</li> <li>4.8 Regression Analysis</li> </ul>	2. Measures of Relationship
SO4.4ExplainSimple Regression Analysis .		<ul><li>4.9 Multiple Correlation and Regression</li><li>4.10 Regression</li><li>4.11 Partial Correlation.</li><li>4.12 Tutorial</li></ul>	

#### SW-4 **SuggestedSessionalWork(SW)**:

#### **Assignments:**

(1) Partial Correlation.



(2) Simple Regression Analysis.

#### a. MiniProject:

Oral presentation, Power Point Presentation.

c.Other Activities (Specify): No

**CO5-78MS105.5** To teach students different techniques of research modelling, data collection, designing and planning of experiments.

#### **Approximate Hours**

Item	AppXHrs
Cl	10
LI	0
SW	1
SL	1
Total	12

SessionOutcomes	LaboratoryInstruction (LI)	ClassroomInstruction	SelfLearning
(SOs)		(CI)	(SL)
SO5.1To understand Report Writing  SO5.2To learn about Different steps in writing report  SO5.3 Explain Types of report .		Unit 5 5.1 Significance of Report Writing 5.2 Example of Report Writing 5.3 Problem define of Report Writing 5.4. Different steps in writing report. 5.5 Layout of a research report 5.6 Oral Presentation 5.6 Mechanics of writing a research report 5.7 tutorial -1 5.8 research report 5.9 Precautions for writing research reports. 5.10 writing research reports.	<ol> <li>To learn about Types of report</li> <li>Definition and examples of Report Writing</li> </ol>

#### SW-5 SuggestedSessionalWork(SW):

#### a. Assignments:-

(1) Binary operation, group and sub types of group.



- (2) Definition and examples of rings and field.
- (3) homeomorphism and isomorphism of group.
- b. MiniProject:

Oral presentation, Power Point Presentation,

c. OtherActivities(Specify):

Report writing

#### **Brief of Hours suggested for the Course Outcome**

Course Outcomes	Class Lecture (CI)	Sessional Work (SW)	Self Learning (SI)	Total hour (CI+SW+SI)
CO1-78MS105.1 Students will Understand research approaches.	14	1	1	13
CO2-78MS105.2 With the help of this course, students will be able to take up and implement a research project/ study.	11	1	1	10
CO3-78MS105.3. Define a research problem.	13	1	1	12
CO4-78MS105.4 The Students will develop skills in qualitative and quantitative data analysis and presentation.	12	1	1	13
CO5-78MS105.5 To teach students different techniques of research modelling, data collection, designing and planning of experiments.	10	1	1	11
Total Hours	60	5	5	70

**Suggestion for End Semester Assessment** 

Suggested Specification Table (For ESA)

СО	Unit Titles	Marks Distribution	Total
			Marks



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		R	U	Α		
CO-1	Research meaning	03	01	01		05
CO-2	Research problem	02	06	02		10
CO-3	Research Design	03	07	05		15
CO-4	Central Tendency	-	10	05		15
CO-5	Research report	03	02		-	05
Total		11	26		13	50

Legend: R: Remember, U: Understand, A: Apply

The end of semester assessment for Introduction to Portland cement will be held with written examination of 50 marks

**Note**. Detailed Assessment rubric need to be prepared by the course wise teachers for above tasks. Teachers can also design different tasks as per requirement, for end semester assessment.

#### **Suggested Instructional/Implementation Strategies**

- 1. Improved Lecture 2. Tutorial 3. Presentation 4. Group Discussion 5. Online sources 6. Seminar
- 7. Workshop



#### **Suggested Learning Resources:**

#### a) Books:

S. N o.	Title	Author	Publisher	Edition & Year
1	Research Methodology Methods and Techniques	C.R.Kothari	Wishwa Prakashan	Publishers Second Edition.
2	Research Methodology for Biological Sciences Abstract Algebra,	N. Gurumani	MJP Publishers	
3	Introduction to educational technology.	Sampath.K., Panneerselvam. Aand Santhanam.	New Delhi: Sterling Publishers	(2nd revised). (1984),

#### **Curriculum Development Team:**

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- 3. Mr. Neelkanth Napit, Assistant Professor, Department of Mathematics.
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### AKS University Faculty of Basic Science Department of Mathematics

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### **Cos, POs and PSOs Mapping**

**Course Title: M.Sc. Mathematics** 

Course Code: 78MS105

**Course Title: Research Methodology** 

Course	PO1	PO 2	PO 3	PO4	PO5	PO6	PO7	PO8	PO9	PO10	PO11	PO 12	PSO 1	PSO 2	PSO 3	PSO 4
Outcome	Advan ced Math emati cal Knowl edge	Proble m-sol vin g Skil Is	Res ear ch Abi liti es	Quant itative Analy sis	Teac hing and Aca dem ia	The oretical Understanding	Comm unicati on Skills	Ope rati ons Res earc h	Applic ation in Indust ry	Engine ering and Techno logy	Gover nmen t and Public Secto r	Co nsu Itin g	Understand the mathematica I concepts and applications in the field of algebra	Handl e the advan ced techni ques	Develop necessa ry skills and expertis e in the field of research	Cre ates Mat hem atic al Mo dels
CO1-78MS105.1 Students will understand research approaches.	2	3	1	2	1	2	2	2	1	1	1	1	2	1	1	<u>3</u>
CO2-78MS105.2 With the help of this course, students will be able to take up and implement a research project/ study.	1	3	2	1	1	1	1	1	1	2	3	1	3	1	1	2
CO3-78MS105.3. Define a research problem.	2	3	2	2	1	1	3	2	1	1	3	1	2	1	<u>2</u>	2
CO4-78MS105.4 The Students will develop skills in qualitative and quantitative data analysis and presentation.	2	3	2	2	1	1	3	2	1	1	3	1	2	1	2	2
CO5-78MS105.5 To teach students different techniques of research modelling, data collection, designin g and planning of experiments.	2	3	2	2	1	1	3	2	1	1	3	1	2	1	2	3

Legend: 1 – Low, 2 – Medium, 3 – High



### AKS University Faculty of Basic Science Department of Mathematics

Curriculum & Syllabus of M.Sc. Mathematics program

### **Course Curriculum Map:**

POs & PSOs No.	COs No.& Titles	SOs No.	Laboratory Instruction(LI)	Classroom Instruction (CI)	Self Learning (SL)
PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2, 3, 4	CO1-78MS105.1 Students will understand research approaches.	SO1.1 SO1.2 SO1.3 SO1.4 SO1.5	1.1	nit-1.0 l,1.2,1.3,1.4,1.5,1.6,1.7,1.8, 9,1.10	SL1.1 SL1.2
PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2, 3, 4	CO2-78MS105.2 With the help of this course, students will be able to take up and implement a research project/study.	SO1.1 SO1.2 SO1.3 SO1.4	2.1	nit-2 1, 2.2, 2.3, 2.4, 2.5, 2.6, 2.7, 3,2.9,2.10	SL2.1 SL2.2
PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2, 3, 4	CO3-78MS105.3. Define a research problem.	SO1.1 SO1.2 SO1.3 SO1.4 SO1.5	2.1	nit-3 1, 2.2, 2.3, 2.4, 2.5, 2.6, 2.7, 3,2.9,2.10	SL3.1 SL3.2
PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2, 3, 4	CO4-78MS105.4 The Students will develop skills in qualitative and quantitative data analysis and presentation.	SO1.1 SO1.2 SO1.3 SO1.4 SO1.5	2.1	nit-4 1, 2.2, 2.3, 2.4, 2.5, 2.6, 2.7, 3,2.9,2.10	SL4.1 SL4.2
PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2, 3, 4	cO5-78MS105.5 To teach students different techniques of research modelling, data collection, designing and planning of experiments.	S01.1 S01.2 S01.3 S01.4 S01.5	2.1	nit-5 1, 2.2, 2.3, 2.4, 2.5, 2.6, 2.7, 3,2.9,2.10	SL5.1 SL5.2 SL5.3

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#### Semester-II

Course Code: 78MS201

Course Title: Advanced Abstract Algebra-II

Pre- requisite: Students should have basic knowledge of group

theory and Mapping

Rationale: The objective of Advanced Abstract Algebra is to

deepen the understanding and explore more advanced topics in the field of abstract algebra. Abstract algebra is a branch of mathematics that studies algebraic structures such as groups, rings, fields, and modules, focusing on their properties

and relationships.

#### **Course Outcome:**

**78MS201.1** Determine whether a particular subset of a ring R is a subring, ideal, or radical

**78MS201.2**. Prove elementary facts about subrings and ideals from the relevant definitions and other elementary facts;

**78MS201.3**. Prove basic relationships between subrings and ideals (e.g., all ideals are subrings but not all subrings are ideals)

**78MS201.4** Learn about the concept of linear independence of vectors over a field, and the dimension of a vector space.

**78MS201.5** Basic concepts of linear transformations, dimension theorem, matrix representation of a linear transformation, and the change of coordinate matrix.

#### **Scheme of Studies:**

Board of Course Study Code	Course Title	Scheme of studies (Hours/Week)						
Study	Code	Title	Cl	LI	sw	SL	Total Study Hours (CI+LI+SW+SL)	Credi ts (C)
Program Core (PCC)	78MS201	Advanced Abstract Algebra-II	4[3+1]	0	1	1	6	4



#### Legend:

**CI:** Classroom Instruction (Includes different instructional strategies i.e. Lecture (L) and Tutorial (T) and others),

**LI:** Laboratory Instruction (Includes Practical performances in laboratory workshop, field or other locations using different instructional strategies)

**SW:** Sessional Work (includes assignment, seminar, mini project etc.)

**SL:** Self Learning,

C:Credits.

**Note:** SW & SL has to be planned and performed under the continuous guidance and feedback of teacher to ensure outcome of Learning.

#### **Scheme of Assessment:**

#### Theory

Board of	Couse Code	Course Title	So	Scheme of Assessment ( Marks )						
Study			S A						Semester Assessmen t	Total Marks (PRA+ ESA)
			Class/Home Assignment 5 number 3 marks each ( CA)	Class Test 2 (2 best out of 3) 10 marks each (CT)	Seminar one (SA)	Class Activity any one (CAT)	Class Attendanc e (AT)	Total Marks (CA+CT+SA + CAT+AT)		
PCC	78MS201	Advanced Abstract Algebra-II	15	20	5	5	5	50	50	100

#### **Course-Curriculum Detailing:**

This course syllabus illustrates the expected learning achievements, both at the course and session levels, which students are anticipated to accomplish through various modes of instruction including Classroom Instruction (CI), Laboratory Instruction (LI), Sessional Work (SW), and Self Learning (SL). As the course progresses, students should showcase their mastery of Session Outcomes (SOs), culminating in the overall achievement of Course Outcomes (COs) upon the course's conclusion.



**CO1-78MS201.1** Determine whether a particular subset of a ring R is a subring, ideal, or radical.

#### **Approximate Hours**

Item	AppX Hrs
Cl	12
LI	0
SW	1
SL	1
Total	14

Session Outcomes (SOs)	Laboratory Instruction (LI)	Class room Instru (CI)	iction	Self Learning (SL)
SO1.1 Understand the concept of Finite Group. SO1.2 Understand the relationships between subgroups SO1.3 Understand the construction of composition series  So1.4 Understand the hypothesis of Cauchy's Theorem So1.5 Understand the hypothesis of Sylow's Theorem	-	group  1.4 p-Subgrou  1.5 Nilpoten  1.6 Tutorial-I  1.7 Commute group of  1.8 Theorem Commute group  1.9 Cauchy's finite abe  1.10 Ca theorem abelian g  1.11 Sy	tion series group as on Solvable  up at group l ator sub- a group as on ator sub- stheorem for elian group auchy's for finite	SL.1 Understand the properties of group, ring, subgroup SL.2 learn to formation of Quotient group  SL.3 Understand the concept of Improper and proper subgroups

#### SW-1 Suggested Sessional Work (SW):

#### a. Assignments:



Solvable group, Nilpotent group, commutator sub-group of a group, Cauchy's theorem, Sylow's theorem.

#### b. Mini Project:

Oral presentation, Poster presentation, Power Point Presentation.

**c.** Other Activities (Specify): Quiz, Class Test.

#### CO2-78MS201.2

Prove elementary facts about subrings and ideals from the relevant definitions and other elementary facts

Item	AppX Hrs
Cl	12
LI	0
SW	1
SL	1
Total	14

		Total	14
Session Outcomes	Labora	Class room Instruction	Self Learning
(SOs)	tory	(CI)	(SL)
	Instruc		
	tion		
	(LI)		
SO2.1		Unit-2.0 Module -I	SL.1
Understand the relationships		2.1 Introduction	learn the no. of
between Ring and modules		<b>2.2</b> Definition	properties of
SO2.2		2.3 Submodules	Module
Learn about properties associated		<b>2.4</b> Properties of Modules	
with modules		<b>2.5</b> Tutorial-I	SL.2
SO2.3		<b>2.6</b> Theorems on Modules	Understand the
Understand the concept of		<b>2.7</b> Theorems on	proof of elemetary
Submodule		SubModules	properties of
SO2.4			module
Understand the concept of		2.8 Semisimple modules	
Quotient module		<b>2.9</b> Algebra of modules	
SO2.5		<b>2.10</b> Theorems on Algebra	
Understand the proof of		of modules	
Fundamental Theorem on		<b>2.11</b> Quotient modules	
Modules		2.12 Fundamental	
		Theorem on Modules	



#### SW-2 Suggested Sessional Work (SW):

- a. Assignments:
- i. Module and Submodule
- ii. Algebra of Module
- iii. Quotient Module
- iv. Mapping defined on Rings
- V. Kernel of mapping
- **b.** Other Activities (Specify): Quiz, Class Test.

#### CO3-78MS201.3

Prove basic relationships between subrings and ideals (e.g., all ideals are subrings but not all subrings are ideals)

Item	AppX Hrs
Cl	12
LI	0
SW	1
SL	1
Total	14

Session Outcomes (SOs)	Laborator y Instructio n (LI)	Class room Instruction (CI)	Self Learning (SL)
SO3.1 Understand the concept Domain, Codomain and Range of mapping SO3.2 Understand the concept of Range of module.		Unit-3.0 Module –II 3.1 Primary Modules 3.2 Theorem on Primary Modules 3.3 Uniform modules 3.4 Theorem on Uniform modules	SL.1 Understan d the concept of mapping on Module. SL.2
SO3.3 Understand the kernel of Homomorphism of module. S03.4 Understand the Notherian and Artinian modules S03.5 Understand the relation of Ring		<ul> <li>3.5 Domain and Codomain of modules</li> <li>3.6 Mapping defined on modules</li> <li>3.7 Homomorphism of modules</li> <li>3.8 Isomorphism of modules</li> </ul>	Understan d the structure of kernel of Mapping



with Notherian and Artinian	3.9 Kernel of Homomorphism
modules.	of modules
	<b>3.10</b> Finitely generated
	modules
	<b>3.11</b> Notherian and Artinian
	modules
	<b>3.12</b> Theorem on Notherian
	and Artinian modules

#### SW-3 Suggested Sessional Work (SW):

- a. Assignments:
- **b.** Other Activities (Specify): Quiz, Class Test.

#### CO4-78MS201.4

Learn about the concept of linear independence of vectors over a field, and the dimension of a vector space.

Item	AppX Hrs
Cl	12
LI	0
SW	1
SL	1
Total	14

Session Outcomes (SOs)	Laborator y Instructio n (LI)	Class room Instruction (CI)	Self Learning (SL)
SO4.1		Unit-4.0 Canonical Forms	SL.1
Understand the		<b>4.1</b> Vector Space	Vector Space
relation between		4.2 Canonical Forms	
vector space and		<b>4.3</b> Similarity of linear	SL.2
Transformation		transformations	Concept of
SO4.2 Understand the index		<b>4.4</b> Invariant subspace Reduction to triangular form	Transformation or mapping
of		4.5 Theorems on Invariant	
Nilpotent		subspace	
transformations		<b>4.6</b> Nilpotent transformations	
		4.7 Index of Nilpotency	
SO4.3		4.8 Theorems on Nilpotent	



Understand The	transformations
concept of Jordan	4.9 Invariants of Nilpotent
blocks and Jordan	transformation
forms	4.10 Jordan blocks
	4.11 Jordan forms
	4.12 Theorems on Jordan forms

#### **SW-4 Suggested Sessional Work (SW):**

#### a. Assignments:

- i. Relationships between algebraic structures of ring with familiar numbers systems.
- ii. Application of Ring group theory in real life.
- iii. Permutation group.
- iv. Mapping defined on Rings.
- V. Polynomial Ring

#### b. Mini Project:

Oral presentation, Poster presentation, Power Point Presentation.

c. Other Activities (Specify):

Quiz, Class Test.

#### CO5-78MS201.5

Basic concepts of linear transformations, dimension theorem, matrix representation of a linear transformation, and the change of coordinate matrix.

AppX Hrs
12
0
1
1
14

Session Outcomes (SOs)	Laboratory Instruction (LI)	Class room Instruction (CI)	Self Learning (SL)
SO5.1		Unit-5.0 Field theory	SL.1
Understand the		5.1 Field theory	Verify
concept Field theory		5.2 Extension field	relationships
SO5.2		5.3 Algebraic Extension	between vector
Understand the		3.3 Algebraic Exterision	space and its



relationships between	5.4 Theorems on Algebraic	subspace
Algebraic Extension	Extension	'
Transcendental	5.5 Transcendental extensions	SL.2
Extension	5.6 Theorems on	understand the
SO5.3	Transcendental Extension	degree of
Understand the	5.7 Seperable extension	extension
relationships between	5.8 Inseperable extension	
seperable and	5.9 finite field	
Insepearable Extension	5.10 Perfect field	
Extension	5.11 Normal extension of a	
	Field	
	5.12 Tutorial	

#### SW-5 Suggested Sessional Work (SW):

- a. Assignments:
- i. Field theory
- ii. Extension field theory
- iii. Application of Field theory
- **b.** Other Activities (Specify): Quiz, Class Test.

#### **Brief of Hours suggested for the Course Outcome**

Course Outcomes	Class Lecture (CI)	Sessional Work (SW)	Self Learning (SI)	Total hour (Cl+SW+SI)
<b>78MS201.1</b> Determine whether a particular subset of a ring R is a subring, ideal, or radical.	12	1	1	14
78MS201.2. Prove elementary facts about subrings and ideals from the relevant definitions and other elementary facts.	12	1	1	14
78MS201.3. Prove basic relationships between subrings and ideals (e.g., all ideals are subrings but not all subrings are	12	1	1	14



ideals)				
78MS201.4 Learn about the concept of linear independence of vectors over a field, and the dimension of a vector space.	12	1	1	14
<b>78MS201.5</b> Basic concepts of linear transformations, dimension theorem, matrix representation of a linear transformation, and the change of coordinate matrix.	12	1	1	14
Total Hours	60	5	5	70

#### **Suggestion for End Semester Assessment**

#### Suggested Specification Table (For ESA)

СО	Unit Titles	Marks D	istributio	n	Total Marks
		R	U	Α	
CO-1	Finite Group	05	03	02	10
CO-2	Module-I	05	03	02	10
CO-3	Module-II	05	03	02	10
CO-4	Canonical form	05	04	01	10
CO-5	Field Theory	05	04	01	10
	Total	25	17	08	50

Legend: R: Remember, U: Understand, A: Apply

The end of semester assessment for Introduction to Portland cement will be held with written examination of 50 marks

**Note**. Detailed Assessment rubric need to be prepared by the course wise teachers for above tasks. Teachers can also design different tasks as per requirement, for end semester assessment.



#### **Suggested Instructional/Implementation Strategies**

- 1. Improved Lecture
- 2. Tutorial
- 3. Presentation
- 4. Group Discussion
- 5. Online sources
- 6. Seminar
- 7. Workshop

#### **Suggested Learning Resources:**

a) Books:

S. N	Title	Author	Publisher	Edition & Year
1	Advanced Abstract Algebra	Dr.H.K.Pathak	Shree Sahitya Siksha Prakashan, Meerut.	
2	Contemporary Abstract Algebra	J. A. Gallian	Narosa Publishing house, New Delhi	4th edition, 2009
3	Abstract Algebra,	D. S. Dummit & R. M.,Foote	John Wiley & Sons, Indian reprint, New Delhi	3rd edition, 2011
4	Basic Abstract Algebra	P.B. Bhattacharya , S.K.Jain &S.R. Nagpaul	Cambridge University press	
5	1. Topics in Algebra,	Herstein, I. N.,	John Wiley & Sons, Indian reprint, New Delhi	2nd edition, 2006.

#### b) Reference Books:

S. No.	Title	Author	Publisher	Edition & Year
1	Abstract Algebra	I.N. Herstein	Macmillan, 3rd Edition,	
				1996, ISBN-10:



2.	Topics in Algebra,	I.N. Herstein	John Wiley and Sons, 2nd Edition	1976, N-10: 0471010901
3.	First Course in Abstract Algebra	Fraleigh, J. B. A	7th edition (Pearson Education India, New Delhi	2008

#### c) Suggetsed Digital Platform Web links:

Suggested Digital Platform s Web links:	https://epgp.inflibnet.ac.in https://www.highereducation.mp.gov.in/?page=xhzlQmpZwkylQo2b%2Fy5G7w %3D%3D http://www.bhojvirtualuniversity.com
Suggested Equivale nt online courses:	https://nptel.ac.in/courses/111/106/111106137/ https://nptel.ac.in/courses/111/105/111105112/ https://ugemoocs.inflibnet.ac.in/index.php/courses/view_ug/32

#### **Curriculum Development Team**

- 1. Dr.Sudha Agrawal, HOD, Department of Mathematics.
- 2. Dr.Ekta Shrivastava , Assistant Professor, Department of Mathematics.
- 3. Mr. Neelkanth Napit, Assistant Professor, Department of Mathematics.
- 4. Mrs. Vandana Soni, Assistant Professor, Department of Mathematics.
- 5. Mr.Radhakrishna Shukla, Assistant Professor, Department of Mathematics.
- 6. Mr.Ghanhyam sen, Assistant Professor, Department of Mathematics.
- 7. Ms. Pushpa Kushwaha, Assistant Professor, Department of Mathematics.
- 8. Ms. Arpana Tripathi, Assistant Professor, Department of Mathematics

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### **Cos, POs and PSOs Mapping**

**Course Title: M.Sc. Mathematics** 

Course Code: 78MS201

**Course Title: Advanced Abstract Algebra-II** 

	PO1	PO2	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10	PO1 1	P O 12	PSO 1	PSO 2	PSO 3	PSO 4
Course	Advanc	Probl	Res	Qua	Teachi	Theo	Comm	Operat	Applic	Engine	Gov	12 C	Unders	Handl	Develop	Creates
Outcome	ed	em-	earc	ntita	ng and	retic	unicati	ions	ation	ering	ern	on	tand	e the	necessar	Mathe
	Mathe	solvin	h	tive	Acade	al	on	Resear	in	and	men	su	the	advan	y skills	matical
	matical	g	Abili	Anal	mia	Und	Skills	ch	Industr	Techn	t	lti	mathe	ced	and	Models
	Knowle	Skills	ties	ysis		ersta			У	ology	and	ng	matical	techni	expertis	
	dge					ndin					Publi		concep	ques	e in the	
						g					c Sect		ts and applica		field of research	
											or		tions in		research	
													the			
													field of			
													algebra			
78MS201.	2	3	1	2	1	2	2	2	1	1	1	1	2	<u>1</u>	<u>1</u>	<u>3</u>
1																
Determine																
whether a																
particular																
subset of																
a ring R is																
a subring,																
ideal, or																
radical.																



	1 .				ı .									Ι.	T -	
78MS20	1	3	2	1	1	1	1	1	1	2	3	1	<u>3</u>	<u>1</u>	<u>1</u>	<u>2</u>
<b>1.2</b> Prove																
element																
ary facts																
about																
subrings																
and																
ideals																
from the																
relevant																
definitio																
ns and																
other																
element																
ary facts		2	2	2	1	1	2	2	4	1	3	1	2	1	2	2
78MS201.		3	2	2	1	1	3	2	1	1	3	1	<u>2</u>	1	<u>2</u>	2
<b>3</b> . Prove																
basic																
relationsh																
ips																
between																
subrings																
and ideals																
(e.g., all																
ideals are																
subrings																
but not all																
subrings																
are ideals) 78MS201.	2	3	2	2	1	1	3	2	1	1	3	1	<u>2</u>	<u>1</u>	<u>2</u>	2
	_		-	-	-	_	J	-	-	-	3	_	=	=	=	-
4																
Learn																
about the																
concept of																
linear																
independe																
nce of																
vectors																
over a																
field, and																
ncia, ana																



the																
dimension																
of a vector																
space																
78MS201.5 Basic concepts of linear transformati ons, dimension theorem, matrix representatio n of a linear	2	3	2	2	1	1	3	2	1	1	3	1	2	1	2	3
transformati on, and the change of coordinate matrix.																

Legend: 1 – Low, 2 – Medium, 3 – High



### **Course Curriculum Map:**

POs & PSOs No.	COs No.& Titles	SOs No.	Laborato ry Instructi on(LI)	Classroom Instruction (CI)	Self Learning (SL)
PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2, 3, 4	<b>78MS201.1</b> Determine whether a particular subset of a ring R is a subring, ideal, or radical.	SO1.1 SO1.2 SO1.3 SO1.4 SO1.5		Unit-1.0 Group 1.1,1.2,1.3,1.4,1.5,1.6,1. 7,1.8,1.9,1.10,1.11,1.12	SL1.1 SL1.2 SL1.3
PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2, 3, 4	78MS201.2. Prove elementary facts about subrings and ideals from the relevant definitions and other elementary facts.	SO1.1 SO1.2 SO1.3 SO1.4 SO1.5		Unit-2 Ring 2.1, 2.2, 2.3, 2.4, 2.5, 2.6, 2.7, 2.8,2.9,2.10,2.11,2.12	SL2.1 SL2.2
PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2, 3, 4	78MS201.3. Prove basic relationships between subrings and ideals (e.g., all ideals are subrings but not all subrings are ideals)	SO1.1 SO1.2 SO1.3 SO1.4 SO1.5		Unit-3 3.1, 3.2, 3.3, 3.4, 3.5, 3.6, 3.7, 3.8,3.9,3.10,3.11,3.12	SL3.1 SL3.2
PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2, 3, 4	78MS201.4 Learn about the concept of linear independence of vectors over a field, and the dimension of a vector space.	SO1.1 SO1.2 SO1.3		Unit-4 4.1, 4.2, 4.3, 4.4, 4.5, 4.6, 4.7,4.8,4.9,4.10,4.11,4.1 2	SL4.1 SL4.2
PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2, 3, 4	78MS201.5 Basic concepts of linear transformations, dimension theorem, matrix representation of a linear transformation, and the change of coordinate matrix.	SO1.1 SO1.2 SO1.3		Unit-5 5.1, 5.2, 5.3, 5.4, 5.5, 5.6,5.7,5.8,8.9,5.10,5.11, 5.12,	SL5.1 SL5.2



#### Semester-II

Course Code: 78MS202
Course Title: Real Analysis-II

(Lebesgue Measure & Integration)

Pre-requisite: Students should have basic knowledge of and

deep understanding of the theory of the

Lebesgue measure & Integration.

Rationale: The program aims to develop advanced problem-

solving and analytical skills and prepares students for careers in academia, research, industry, or other sectors that require advanced

mathematical expertise.

**CO1-78MS202.1** Understand the importance of properties of Lebesgue outer measure and Borel measurability of sets

CO2-78MS202.2 Determine the Measurable function and Lebesgue Integral

**CO3-78MS202.3** Demonstrate an understanding of the theory of Four derivatives and Lebesgue Differentiation theorem

**CO4-78MS202.4** Define and recognize the series and Students will compute the expression of L<sup>p</sup> Space and convex function .

**CO5-78MS202.5** Students will create the concept of a Riesz theorem and uniform convergence.

#### **Scheme of Studies:**

		Course	Scheme of studies (Hours/Week)								
	Title	Cl	LI	SW	SL	Total Study Hours (CI+LI+SW+SL)	ts (C)				
Program Core (PCC)	78MS202	Real Analysis- II	4[3+1]	0	1	1	6	4			



#### Legend:

**CI:** Classroom Instruction (Includes different instructional strategies i.e. Lecture (L) and Tutorial (T) and others),

LI: Laboratory Instruction (Includes Practical performances in laboratory workshop, field or other locations using different instructional strategies)

SW: Sessional Work (includes assignment, seminar, mini project etc.),

SL: Self Learning,

C:Credits.

**Note:** SW & SL has to be planned and performed under the continuous guidance and feedback of teacher to ensure outcome of Learning.

#### **Scheme of Assessment:**

#### Theory

Board of	Couse	Course Title	Scheme of	Assessme	nt ( Marks	)				
Study	Code					End Semester Assessm ent (ESA)	Total Marks (PRA+ ESA)			
			Class/Ho me Assignme nt 5 number 3 marks each ( CA)	Class Test 2 (2 best out of 3) 10 marks each (CT)	Seminar one ( SA)	Class Activit y any one (CAT)	Class Attend ance (AT)	Total Marks (CA+CT+ SA +CAT+A T)		
PCC	78MS202	Real Analysis-II	15	20	5	5	5	50	50	100

#### **Course-Curriculum Detailing:**

This course syllabus illustrates the expected learning achievements, both at the course and session levels, which students are anticipated to accomplish through various modes of instruction including Classroom Instruction (CI), Laboratory Instruction (LI), Sessional Work (SW), and Self Learning (SL). As the course progresses, students should showcase their mastery of Session Outcomes (SOs), culminating in the overall achievement of Course Outcomes (COs) upon the course's conclusion.



**CO1-78MS202.1** Understand the importance of properties of Lebesgue outer measure and Borel measurability of sets

Item	AppXHrs
Cl	13
LI	0
SW	1
SL	1
Total	15

Session Outcomes (SOs)	Laboratory Instruction (LI)	Class room Instruction (CI)	Self Learning (SL)
SO1.1 Understand the concept of Lebesgueouter measure SO1.2 Understand the Properties of Measurable set SO1.3 Understand the Regularity of a measure. SO1.4 Understand the Lebesgue Measurability of Sets, SO1.5 Understand the Non- measurable of Sets.		Unit-1.0 1.1Introduction  1.2 Lebesgueouter measure  1.3 Lebesgue Measurable set.  1.4 Regularity of a measure.  1.5Borel measurability of Sets.  1.6 Borel Set – Examples  1.7 Translational Invariant  1.8Lebesgue Measurability of Sets,  1.9Non- measurable of Sets.  1.10 F $\sigma$ and $F_{\delta}$ sets  Algebra of sets  1.11 First fundamental theorem	SL.1  A set A is measurable iff its complement A' is measurable.



	1.12 Second fundamental theorem	
	1.13 Tutorial 1	

#### SW-1 Suggested Sessional Work (SW):

#### a. Assignments:

i. Let E be a measurable set then any translate E+y is measurable where y is a real number

furthermore m(E+y) = m(E)

ii State and prove Second fundamental form of measurable set.

iii If E<sub>1</sub> and E<sub>2</sub> are any measurable set then show that

 $m(E_1 \cup E_2) + m(E_1 \cap E_2) = m(E_1) + m(E_2)$ 

iv Prove that the Intersection and Difference of two measurable sets are measurable.

V A Borel measurable set is Lebesgue measurable.

#### b. Mini Project:

Oral presentation, Poster presentation, Power Point Presentation.

**c.** Other Activities (Specify):

Quiz, Class Test.

CO2-78MS202.2 Determine the Measurable function and Lebesgue Integral

-p-p	
Item	AppXHrs
Cl	15
LI	0
SW	1
SL	1
Total	16

Session Outcomes	Laboratory Instruction	Class room Instruction	Self Learning
(SOs)	(LI)	(CI)	(SL)
SO2. <b>1</b>		Unit2.0	<b>SL1</b> Some Properties of
Understand the			Lebesgue Measurable



concept of	2.1Measurable	function
concept of		Turiction
LebesgueMeasurable	function,	
function,	2.2Properties of	
SO2.2 Understand the	Lebesgue measurable	
Properties of Lebesgue	functions.	
measurable functions.	2.3 Integral of Non	
SO2.3 Understand the	negative Measurable	
Integral of Non	function.	
negative Measurable	2.4 Step function	
function.	2.5 Operations on	
SO2.4Understand the	Measurable functions	
Properties of	2.6 Characteristic	
Measurable se.	Function of set	
	2.7 Integration of series	
	2.8 Borel measurable	
	function	
	2.9 Littlewood's three	
	principles,	
	2.10Fatou's lemma	
	2.11 Reimann	
	andLebesgue integral.	
	2.12The general	
	integral	
	2.13 Properties of the	
	Lebesgue integral for	
	bounded measurable	
	function	
	2.14 Lebesgue bounded	
	convergence theorem	
	2.15 Lebesgue	
	dominated	
	convergence theorem	

#### SW-2 Suggested Sessional Work (SW):

#### a. Assignments:

- i. Operations on Measurable functions.
- ii. Show that a step function is a measurable function
- iii. Theorems on Measurable function
- iv Show that every function defined on a set of measure zero is measurable .
- v The limit of convergence sequence of measurable function is measurable

#### b. Mini Project:



Oral presentation, Poster presentation, Power Point Presentation.

**c.** Other Activities (Specify): Quiz, Class Test.

**CO3-78MS202.3** Demonstrate an understanding of the theory of Four derivatives and Lebesgue Differentiation theorem

Item	AppXHrs
Cl	10
LI	0
SW	1
SL	1
Total	12

Session Outcomes (SOs)	Laboratory Instruction (LI)	Class room Instruction (CI)	Self Learning (SL)
SO3.1 Understand the the four		Unit-3.0 3.1 The four derivatives	SL.1 Examples of
derivatives. Lebesgue		Introduction	function of bounded variation
SO3.2 Understand the Differentiation of an Integral		<ul><li>3.2 Tutorial 1</li><li>3.3 Lebesgue Differentiation</li><li>Theorem</li></ul>	
SO3.3 Understand the Functions of Bounded Variation		<ul><li>3.4 Differentiation of an Integral-lemma</li><li>3.5 Fundamental theorem of</li></ul>	
SO3.4Understand the Jordan Decomposition		Integral Calculus  3.6 Functions of Bounded Variation  3.7 Tutorial 2	
theorem		3.8 Jordan Decomposition theorem	



	3.9 Absolute continuous function	
	3.10Integral of the derivatives	

#### SW-3 Suggested Sessional Work (SW):

#### a. Assignments:

- i. state and prove Jordan Decomposition theorem
- ii. State and prove Lebesgue Differentiation Theorem
- iii. State and prove Fundamental theorem of Integral Calculus.

#### b. Mini Project:

Oral presentation, Poster presentation, Power Point Presentation.

**c.** Other Activities (Specify):

Quiz, Class Test.

#### CO4-78MS101.4

 ${f CO4-78MS202.4}$  Define and recognize the series and Students will compute the expression of  $L^p$  Space and convex function .

Item	AppXHrs
Cl	11
LI	0
SW	1
SL	1
Total	13

Session Outcomes	Laboratory Instruction	Class room Instruction	Self Learning
(SOs)	(LI)	(CI)	(SL)



SO4.1	Unit-4.0	SL.1
UnderstandTheLp-	4.1Introduction The Lp-	Some theorems of Lp-
Space	Space	Space
SO4.2 Understand	4.2 Theorems of L <sup>p</sup> -	
theConvex function	Space	
SO4.3Understand the	4.3 Convex function	
Holder and	4.4 Theorems on	
Minkowski's	Convex function	
Inequalities for L <sup>p</sup>	4.5 Jensen's Inequality.	
SO4.4 Completeness of	4.6 Holder Inequalities	
L <sup>p</sup> -Space.	for L <sup>p</sup> -Space.	
	4.7Minkowski's	
	Inequalities for L <sup>p</sup> -	
	Space	
	4.8 Completeness of	
	L <sup>p</sup> -Space	
	4.9 L <sup>p</sup> -Space is normed	
	linear space	
	4.10 Riesz-Fischer	
	theorem	
	4.11 Tutorial 1	

### SW-4 Suggested Sessional Work (SW):

### a. Assignments:

- (i) Jensen's Inequality.
- (ii) Holder Inequalities for L<sup>p</sup>-Space.
- (iii) Minkowski's Inequalities for Lp-Space

### b. Mini Project:

Oral presentation, Poster presentation, Power Point Presentation.

**c.** Other Activities (Specify):

Quiz, Class Test.

CO5-78MS202.5 Students will create the concept of a Riesz theorem and uniform convergence

the commute	110410
Item	Appx Hrs
Cl	11
LI	0
SW	1
SL	1



Total	13

SO5.1 Understand the concept Convergence in measure,  SO5.2 Understand the Riesz theorem  SO5.3 Understand Uniform Convergence  SO5.4Understand Egoroff's theorem  SO5.4Understand Egoroff's theorem  Unit-5.0  5.1 Convergence in measure, So5.2 Riesz theorem  So2.1 If <fn> is a Cauchy sequence then it has limit  So3.1 If <fn> is a Cauchy sequence then it has limit  So3.1 If <fn> is couplede  So3.4Uniform Convergence - L<sup>p</sup> is complete  So4.4Uniform Convergence - L<sup>∞</sup> is complete  So5.4Uniform Convergence - L<sup>∞</sup> is complete</fn></fn></fn>	Session Outcomes (SOs)	Laboratory Instruction (LI)	Class room Instruction (CI)	Self Learning (SL)
5.6 Almost Uniform Convergence- Example 2 5.7 Theorems on Convergence in measure, 5.8 Test of consistency 5.9 Lebesgue integrable function on [0,1] 5.10 Egoroff's theorem 5.11 Tutorial 1	Understand the concept Convergence in measure SO5.2 Understand the Riesz theorem SO5.3 Understand Uniform Convergence		5.1 Convergence in measure,  5.2 Riesz theorem  5.3Uniform Convergence - L <sup>p</sup> is complete  5.4Uniform Convergence - L <sup>∞</sup> is complete  5.5 Almost Uniform Convergence-Example 1  5.6 Almost Uniform Convergence-Example 2  5.7 Theorems on Convergence in measure, 5.8 Test of consistency 5.9 Lebesgue integrable function on [0,1]  5.10 Egoroff's theorem	If <fn> is a Cauchy sequence then it has</fn>



### **Brief of Hours suggested for the Course Outcome**

Course Outcomes	Class Lecture (CI)	Sessional Work (SW)	Self Learning (SI)	Total hour (Cl+SW+SI)
CO1-78MS202.1 Understand the importance of properties of Lebesgue outer measure and Borel measurability of sets	13	1	1	15
CO2-78MS202.2 Determine the Measurable function and Lebesgue Integral	15	1	1	17
CO3-78MS202.3 Demonstrate an understanding of the theory of Four derivatives and Lebesgue Differentiation theorem	10	1	1	12
<b>CO4-78MS202.4</b> Define and recognize the series and Students will compute the expression of L <sup>p</sup> Space and convex function .	11	1	1	13
CO5-78MS202.5 Students will create the concept of a Riesz theorem and uniform convergence.	11	1	1	13
Total Hours	60	5	5	70

### **Suggestion for End Semester Assessment**

### Suggested Specification Table (For ESA)

СО	Unit Titles	Mark	s Distrib	oution	Total Marks	
		R	U	Α		
CO-1	Understand the importance of properties of Lebesgue outer measure and Borel measurability of sets	03	01	01		05
CO-2	Determine the Measurable function and Lebesgue Integral	02	06	02		10



CO-3	Demonstrate an understanding of the theory of Four derivatives and Lebesgue Differentiation theorem	03	07	05		15
CO-4	Define and recognize the series and Students will compute the expression of L <sup>p</sup> Space and convex function.	-	10	05		15
CO-5	Students will create the concept of a Riesz theorem and uniform convergence.	03	02		-	05
Total		11	26		13	50

Legend: R: Remember, U: Understand, A: Apply

The end of semester assessment for Introduction to Portland cement will be held with written examination of 50 marks

**Note**. Detailed Assessment rubric need to be prepared by the course wise teachers for above tasks. Teachers can also design different tasks as per requirement, for end semester assessment.

### **Suggested Instructional/Implementation Strategies**

- 1. Improved Lecture
- 2. Tutorial
- 3. Presentation
- 4. Group Discussion
- 5. Online sources
- 6 .Seminar
- 7. Workshop



### **Suggested Learning Resources:**

#### a) Books:

S. N o.	Title	Author	Publisher	Edition & Year
1	Real Analysis	Dr.H.K.Pathak	Shree Sahitya Siksha Prakashan, Meerut.	2018
2	Real Analysis	S. C. Malik	Willey Eastern Ltd.,ew Delhi, 1985.	
3	Real Analysis,.	N. L. Carothers,	Cambridge University Press, UK, 2000	
4	Elementary Analysis:	Kenneth A. Ross	The theory of Calculus, Springer, New York, 2004.	
5	Principles of Mathematical Analysis	Walter Rudin	3 rd Edition, McGraw – Hill International Book Company, Singapore, 1982.	

### **Curriculum Development Team:**

- 1. 1. Dr. Sudha Agrawal, HOD, Department of Mathematics.
- 2. Dr.Ekta Shrivastava , Assistant Professor, Department of Mathematics.
- 3. Mr. Neelkanth Napit, Assistant Professor, Department of Mathematics.
- 4. Mrs. Vandana Soni, Assistant Professor, Department of Mathematics.
- 5. Mr.Radhakrishna Shukla, Assistant Professor, Department of Mathematics.
- 6. Mr.Ghanhyam sen, Assistant Professor, Department of Mathematics.
- 7. Ms. Pushpa Kushwaha, Assistant Professor, Department of Mathematics.
- 8. Ms. Arpana Tripathi, Assistant Professor, Department of Mathematics

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### **Cos, POs and PSOs Mapping**

**Course Title: M.Sc. Mathematics** 

Course Code :78MS202 Course Title: Real Analysis-II

_	PO1	PO 2	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO1 0	PO1 1	PO 12	PSO 1	PSO 2	PSO 3	PSO 4
Course Outcome	Adva nced Mat hem atica I Kno wled ge	Pr ob le m- sol vin g Ski Ils	Research Abilities	Qua ntita tive Anal ysis	Teachi ng and Acade mia	Theo retic al Und ersta ndin g	Co mm unic atio n Skill s	Oper ation s Resea rch	Appli catio n in Indu stry	Engi neer ing and Tech nolo gy	Gove rnm ent and Publi c Sect or	Co ns ulti ng	Understan d the mathemat ical concepts and applicatio ns in the field of algebra	Handle the advanc ed techniq ues	Develop necessary skills and expertise in the field of research	Creates Mathe matical Models
78MS202.1 Understan d the importance of properties of Lebesgue outer measure and Borel measurabili ty of sets.	2	3	1	2	1	2	1	2	1	1	2	1	2	2	1	
CO1- 78MS202. 2 Determine the Measurabl e function and Lebesgue Integral	2	3	1	1	1	1	1	1	1	1	1	1	1	2	2	
CO1- 78MS202.3	3	3	1	2	1	1	3	2	2	1	2	2	1	2	<u>3</u>	



Demonstra te an understand ing of the theory of Four derivatives and Lebesgue Differentiat ion theorem																
CO1- 78MS202.4 Define and recognize the series and Students will compute the expression of L <sup>p</sup> Space and convex function.	2	3	1	2	3	2	3	1	1	1	1	2	2	1	1	
CO1- 78MS202.5 Students will create the concept of a Riesz theorem and uniform convergenc e	3	2	3	1	2	1	2	3	1	1	1	1	1	1	1	

Legend: 1 – Low, 2 – Medium, 3 – High



### **Course Curriculum Map:**

POs & PSOs No.	COs No.& Titles	SOs No.	Laborato Instruction	,	Classroom Instruction (CI)	Self Learning (SL)
PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2, 3, 4	CO1-78MS202.1 Understand the Lebesgue outer measure and measurable set	SO1.1 SO1.2 SO1.3 SO1.4 SO1.5		mea set1	t-1.0 Lebesgue outer asure and measurable 1.1,1.2,1.3,1.4,1.5,1.6,1.7, 1.9,1.10,1.11,1.12,1.13	SL1.1
PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2, 3, 4	CO2-78MS202.2 Measurable function and Lebesgue Integral	SO2.1 SO2.2 SO2.3 So2.4		Unit and 2.2, 2.3, 0,2.	SL2.1	
PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2, 3, 4	CO3-78MS202.3 Students will be able to describe all elements in Differentiation and Integration	SO3.1 SO3.2 SO3.3 SO3.4		Inte 3.1,	t-3 Differentiation and egration 3.2, 3.3, 3.4, 3.5, 3.6, 3.8,3.9,3.10	SL3.1
PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2, 3, 4	CO4-78MS202.4 Students will compute the expression The L <sup>p</sup> - space	SO4.1 SO4.2 SO4.3 SO4.4		4.1,	t-4 The L <sup>p</sup> -space 4.2, 4.3, 4.4, 4.5, 4.6, 4.7, 4.9,4.10,4.11	SL4.1
PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2, 3, 4	CO5-78MS202.5 Students will create the concept of a Convergence in Measure:	SO5.1 SO5.2 SO5.3 SO5.4		Me:	t-5Convergence in asure: 5.2, 5.3, 5.4, 5.5, 5.7,5.8,5.9,5.10,5.11	SL5.1

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#### Semester-II

Course Code: 78MS203
Course Title : Complex Analysis-II

guisite: Students should have basic knowledge of

complex numbers

Rationale: The program aims to develop advanced problem-

solving and analytical skills and prepares students for careers in academia, research, industry, or other sectors that require advanced

mathematical expertise.

#### **Course Outcome:**

**CO1-78MS203.1** This course gives more Understanding about Analysis in mathematics.

**CO2-78MS203.2**. Students will be equipped with the understanding of the fundamental concepts of complex variable theory and skill of contour integration.

**CO3-78MS203.3**. This course involved complex number properties of them, analytic function, residues fundamental theorem.

**CO4-78MS203.4** With this Course students are prepared to learn about advance complex analysis.

**CO5-78MS203.5** Students will Constructing mobius transformations mapping given circle to given Circle.

#### **Scheme of Studies:**

Board of Study	Course Code	Course Title	Scheme of studies (Hours/Week)							
,			CI	LI	SW	SL	Total Study Hours (CI+LI+SW+SL)	ts (C)		
Program Core (PCC)	78MS203	Complex Analysis- II	4[3+1]	0	1	1	6	4		



### Legend:

**CI:** Classroom Instruction (Includes different instructional strategies i.e. Lecture (L) and Tutorial (T) and others),

**LI:** Laboratory Instruction (Includes Practical performances in laboratory workshop, field or other locations using different instructional strategies)

**SW:** Sessional Work (includes assignment, seminar, mini project etc.),

SL: Self Learning,

C:Credits.

**Note:** SW & SL has to be planned and performed under the continuous guidance and feedback of teacher to ensure outcome of Learning.

#### **Scheme of Assessment:**

#### Theory

Board of	Couse	Course Title		Scheme of Assessment ( Marks )						
Study	Code		Progressive Assessment ( PRA )  End Sem Asse ent			Semester Assessm	Total Marks (PRA+ ESA)			
			Class/Ho me Assignme nt 5 number 3 marks each ( CA)	Class Test 2 (2 best out of 3) 10 marks each (CT)	Seminar one ( SA)	Class Activit y any one (CAT)	Class Attend ance (AT)	Total Marks (CA+CT+ SA +CAT+A T)		
PCC	78MS203	Complex Analysis-ll	15	20	5	5	5	50	50	100

#### **Course-Curriculum Detailing:**

This course syllabus illustrates the expected learning achievements, both at the course and session levels, which students are anticipated to accomplish through various modes of instruction including



Classroom Instruction (CI), Laboratory Instruction (LI), Sessional Work (SW), and Self Learning (SL). As the course progresses, students should showcase their mastery of Session Outcomes (SOs), culminating in the overall achievement of Course Outcomes.

**CO1-78MS203.1** This course gives more Understanding about Analysis in mathematics.

Item	AppX Hrs
Cl	12
LI	0
SW	1
SL	1
Total	14

Session Outcomes (SOs)	Laborat ory Instructi	Class room Instruction (CI)	Self Learning (SL)
	on		
	(LI)		



SO1.1	Unit-1.0 The spaces of Analytic	SL.1
Understand the concept	functions	Understand the
of analytic function		complex numbers.
	1.1 Introduction of analytic	
SO1.2	function	<b>SL.2</b> knowledge of the
Understand the	1.2 spaces of analytic functions.	difference of Analytic
relationships between two	1.3 limit, continuity and	and Entire functions.
functions, analytic and	differentiability of complex	SL.3
entire functions.	function	Properties of Analytic
SO1.3	1.4 introduction of entire function.	function.
Understand the concept of	1.5 Tutorial –I	
contur integration	1.6 complex integration.	
So1.4	1.7 The Weierstress factorization	
Understand the	theorem.	
hypothesis of Cauchy's	1.8 The Concept of Gamma	
Theorem	function.	
So1.5	1.9 The Riemann zeta function.	
Understand the concept of	1.10 Extension of zeta function.	
function.	1.11 Riemann s functional	
	equations.	
	1.12Tutorial –II	

### SW-1 Suggested Sessional Work (SW):

#### a. Assignments:

- i. Relationships between complex numbers structures with familiar numbers systems such as the Set of natural numbers, Set of rational numbers, Set of integers, Set of real numbers, Set of complex numbers.
- ii. State and prove Weierstress factorization theorem
- iii. State and prove Gamma functions
- iv Riemann s zeta function.

#### b. Mini Project:

Oral presentation, Poster presentation, Power Point Presentation.

#### c. Other Activities (Specify):

Quiz, Class Test.

**CO2-78MS203.2**. Students will be equipped with the understanding of the fundamental concepts of complex variable theory and skill of contour integration.



### **Approximate Hours**

Item	AppX Hrs
Cl	12
LI	0
SW	1
SL	1
Total	14

Session Outcomes	Laboratory	Class room Instruction	Self Learning
(SOs)	Instruction (LI)	(CI)	(SL)
SO2.1	(/	Unit-2.0 Analytic Continuation.	SL.1
Understand the			Analytic function of a
concept of Runge's		2.1 Introduction	complex variables.
theorem.		2.2 Analytic Continuation	
		2.3 Runge's theorem.	SL.2
		2.4 Uniqueness of Analytic	Knowledge of the
SO2.2		Continuation.	Analyticity of the sum
Learn about Analytic		2.5 Tutorial –I	function of a series
Continuation.		2.6 power series method of	
SO2.3		Analytic Continuation.	SL.3
Understand the		2.7 Application of Riemann	Knowledge of Analytic
concept of		hypothesis in number theory.	Continuation.
Power series.		2.8 tutorial	
SO2.4		2.9 Theorems on Analytic	
Understand the Uses of		function.	
Analytic function.		2.10 Expansion of Riemann 's	
		functional equations.	
SO2.5		2.11 the concept of Mittag-	
Understand the		Leffler's theorem	
concept of mitteg-		2.12 Tutorial –II	
Leffer's theorem			

### SW-2 Suggested Sessional Work (SW):



### a. Assignments:

- i. State and prove Runge's theorem.
- ii. State and prove Mittag Leffler's theorem.
- iii. The Uniqueness of direct Analytic Continuation along a curves
- iv. Analytic Continuation.

### b. Mini Project:

Oral presentation, Poster presentation, Power Point Presentation.

c. Other Activities (Specify):

Quiz, Class Test.

**CO3-78MS203.3**. This course involved complex number properties of them, analytic function, residues fundamental theorem.

Item	AppX Hrs
Cl	12
LI	0
SW	1
SL	1
Total	14

Session Outcomes	Laboratory	Class room Instruction	Self Learning
(SOs)	Instruction	(CI)	(SL)
	(LI)		



SO3.1 Understand the	Unit-3.0 Harmonic Functions.	SL.1
principal of	3.1 Introduction	Knowledge of the
SO3.2 Rouche's theorem	<ul><li>3.2 harmonic functions.</li><li>3.3 the concept of Schwartz lemma.</li></ul>	poles and zeros of a Meromorphic function.
SO3.3 the concept of	3.4 basic properties of harmonic	
Maximum Modulus	functions.	SL.2
principal	3.5 Tutorial –I 3.6 Schwarz's reflection principle 3.7 Monodromy theorem. 3.8 Monodromy theorem and its consequences. 3.9 some Theorems on harmonic functions 3.10 Subharmonic functions 3.11 Harmonic Functions on a disc. 3.12 Tutorial –II	Understand an application of Rouche's theorem.

### SW-3 Suggested Sessional Work (SW):

#### a. Assignments:

- i. The concept of harmonic functions
- ii. Application of harmonic functions
- iii. Schwarz's reflection principle.
- iv. State and prove Monodromy theorem.
- V. Schwarz lemma.

### b. Mini Project:

Oral presentation, Poster presentation, Power Point Presentation.

**c.** Other Activities (Specify):

Quiz, Class Test.



**CO4-78MS203.4** With this Course students are prepared to learn about advance complex analysis.

Item	AppX Hrs
Cl	12
LI	0
SW	1
SL	1
Total	14

Session Outcomes (SOs)	Laboratory Instruction (LI)	Class room Instruction (CI)	Self Learning (SL)



concept of Greens function. SO4.2 understand the Canonical product SO4.3 Understand the importance of Dirichlet problem.		Canonical products, Convergence of Entire functions.  4.1 Introduction 4.2 Harnax's Inequality and theorem . 4.3 The Dirichlet problem 4.4 The concept of Greens functions. 4.5 Tutorial-I 4.6 Canonical products. 4.7 Jensen formula. 4.8 The Poisson -Jensen formula 4.9 Exponents of Convergence. 4.10 Convex functions. 4.11 The convergent function of Entire functions 4.12 Tutorial-II	The concept of Greens functions.  SL.2 Evaluation of Poisson - Jensen formulae
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### SW-4 Suggested Sessional Work (SW):

#### a. Assignments:

- i. Evaluation of Poisson -Jensen formulas.
- ii. Application of the Dirichlet problem.
- iii. State and prove Harnax's Inequality and theorem .
- iv. Canonical products.
- V. Greens functions



### b. Mini Project:

Oral presentation, Poster presentation, Power Point Presentation.

**c.** Other Activities (Specify): Quiz, Class Test.

### CO5-78MS203.5

Circle.

Students will Constructing mobius transformations mapping given circle to given

Item	AppX Hrs
Cl	12
LI	0
SW	1
SL	1
Total	14

Session Outcomes	Laboratory Instruction	Class room Instruction	Self Learning
(SOs)	(LI)	(CI)	(SL)



SO5.1 Understand the concept of Bloch's theorem SO5.2 theorems on the	Unit-5.0 The Range of an Analytic functions.	SL.1 knowledge of the Analytic function
Analytic function  SO5.3 the concept of range of Analytic	<ul><li>5.1 Introduction</li><li>5.2 Analytic function</li><li>5.3 Bloch's theorem.</li><li>5.4 Application of</li></ul>	SL.2 The Concept Bloch's theorem.
	Bloch's theorem.  5.5 Definition and Example Of Bloch's	
	Constant.  5.6 Tutorial-I	
	5.7 The Little Picard theorem. 5.8 the definition of branch of the logarithm	n
	5.9 Schottky 's theorem. 5.10 the Great Picard	
	theorem. 5.11 Application of Picard theorem. 5.12 Tutorial-II	



### **Brief of Hours suggested for the Course Outcome**

Course Outcomes	Class Lecture (CI)	Sessional Work (SW)	Self Learning (SI)	Total hour (Cl+SW+SI)
CO1-78MS203.1 This course gives more Understanding about Analysis in mathematics	. 12	1	1	14
CO2-78MS104.2.  Students will be equipped with the understanding of the fundamental concepts of complex variable theory and skill of contour integration.	12	1	1	14
CO3-78MS104.3.  This course involved complex number properties of them, analytic function, residues fundamental theorem.	. 12	1	1	14
CO4-78MS203.4  With this Course students are prepared to learn about advance complex analysis.	12	1	1	14
CO5-78MS203.5 Students will Constructing Mobius transformations mapping given circle to given Circle	12	1	1	14
Total Hours	60	5	5	70



### o Suggestion for End Semester Assessment

Suggested Specification Table For (ESA)

со	Unit Titles	Marks Distri	ibution		Total Marks
		R	U	Α	
CO1-	Unit-1.0 The spaces of Analytic functions, Entire functions.	03	01	01	05
CO2-	Unit-2.0 Analytic Continuation.	02	05	03	10
соз-	Unit-3.0 Harmonic Functions.	03	06	06	15
CO4-	Unit -4 Canonical products, Convergence of Entire functions	-	10	05	15
CO5-	Unit-5.0 The Range of an Analytic functions.	03	02	-	05
Total		11	26	13	50

Legend: R: Remember, U: Understand, A: Apply

The end of semester assessment for Introduction to Portland cement will be held with written **Note**. Detailed Assessment rubric need to be prepared by the course wise teachers for above tasks. Teachers can also design different tasks as per requirement, for end semester assessment.

**Suggested Instructional/Implementation Strategies** 



- 1. Improved Lecture
- 2. Tutorial
- 3. Presentation
- 4. Group Discussion
- 5. Online sources
- 6 .Seminar
- 7. Workshop

### **Suggested Learning Resources:**

a) Books:

S.	Title	Author	Publisher	Edition & Year
N				
0.				
1	Fundamental Theorem of Complex Analysis	S.Punnuswamy	narosa publishing house	2nd edition, New Delhi 2005
2	Fundamentals of complex analysis	S.Ponnuswamy,	Narosa Publishing house	4th edition, 1985



			McGraw-Hill,New York	Edition,
3.	Theory and Problems of	M.R.spiegel		Singapore,1979
	complex variables		McGraw Hill book	
			company International	

### **Curriculum Development Team:**

- 1. 1. Dr. Sudha Agrawal, HOD, Department of Mathematics.
- 2. Dr. Ekta Shrivastava, Assistant Professor, Department of Mathematics.
- 3. Mr. Neelkanth Napit, Assistant Professor, Department of Mathematics.
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- 7. Ms. Pushpa Kushwaha, Assistant Professor, Department of Mathematics.
- 8. Ms. Arpana Tripathi, Assistant Professor, Department of Mathematics

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### **Cos, POs and PSOs Mapping**

**Course Title: M.Sc. Mathematics** 

Course Code: 78MS203

**Course Title: Complex Analysis-II** 

PO1	PO	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10	PO1	PO12	PSO 1	PSO	PSO 3	PSO
	2									1			2		4



Course	Adv	Pr	Resear	Qu	Teac	The	Com	Oper	Appli	Engi	Go	Cons	Under	На	Develo	Cre
Outcome	anc	О	ch	ant	hing	ore	muni	ation	catio	neeri	ver	ultin	stand	ndl	р	ate
	ed	bl	Abiliti	itat	and	tica	catio	S	n in	ng	nm	g	the	е	necess	S
	Ma	е	es	ive	Acad	1	n	Rese	Indu	and	ent		mathe	the	ary	Ma
	the	m		An	emia	Un	Skills	arch	stry	Tech	and		matica	adv	skills	the
	ma	-		alys		der				nolo	Pub		1	anc	and	ma
	tica	so		is		sta				gy	lic		conce	ed	expert	tic
	I	lvi				ndi					Sec		pts	tec	ise in	al
	Kn	n				ng					tor		and	hni	the	Мо
	owl	g											applic	que	field	del
	edg	Sk											ations	S	of	S
	е	ill											in the		resear	
		S											field		ch	
													of			
													algebr			
.CO1-	2	1	2	2	1	2	3	2	1	1	1	1	<u>1</u>	2	<u>1</u>	2
78MS203.	_	-	_	_	_	_		_	_	-	_	_	_	<u> </u>	_	_
1 This																
course																
gives more																
Understan																
ding about																
Analysis in																
mathemat																
ics.																
								1								



.CO2- 78MS203. 2. Students will be equipped with the understan ding of the fundament al concepts of complex variable theory and skill of contour integration	2	1	1	2	1	2	1	1	1	2	1	1	<u>3</u>	2	1	1
.CO3- 78MS203.3 This course involved complex number properties of them,analy tic function,re sidues fundament al theorem.	2	1	2	2	1	3	2	1	2	2	1	1	2	2	1	1



[ ]		<u>1</u>	<u>1</u>	<u>1</u>
3	<u>1</u>	<u>1</u>	<u>2</u>	1
	3	3 1	3 1 1	3 1 1 2

Legend: 1 – Low, 2 – Medium, 3 – High



### **Course Curriculum Map:**

POs & PSOs No.	COs No.& Titles	SOs No.	Laborato ry Inst ru ction(LI)	Classroom Instruction (CI)	Self Learning (SL)
PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2, 3, 4	CO178MS203.1 This course gives more Understanding about Analysis in mathematics.	SO1.1 SO1.2 SO1.3 SO1.4 SO1.5		Unit-1.0 1.1,1.2,1.3,1.4,1.5,1.6,1. 7,1.8,1.9,1.10	SL1.1 SL1.2
PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2, 3, 4	co278MS203.2. Students will be equipped with the understanding of the fundamental concepts of complex variable theory and skill of contour Integration.	SO1.1 SO1.2 SO1.3 SO1.4 SO1.5		Unit-2 2.1, 2.2, 2.3, 2.4, 2.5, 2.6, 2.7, 2.8,2.9,2.10	SL2.1 SL2.2
PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2, 3, 4	CO378MS203.3. This course involved complex number properties of them,analytic function,residues fundamental theorem.	SO1.1 SO1.2 SO1.3 SO1.4 SO1.5		Unit-3 3.1, 3.2, 3.3, 3.4, 3.5, 3.6, 3.7, 3.8,3.9,3.10	SL3.1 SL3.2
PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2, 3, 4	CO4-78MS203.4 With this Course students are prepared to learn about advance complex analysis	SO1.1 SO1.2 SO1.3 SO1.4 SO1.5		Unit-4 4.1, 4.2, 4.3, 4.4, 4.5, 4.6, 4.7, 4.8,4.9,4.10.	SL4.1 SL4.2
PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2, 3, 4	CO5-78MS203.5 Students will Constructing mobius transformations mapping given circle to given Circle	SO1.1 SO1.2 SO1.3 SO1.4 SO1.5		Unit-5 5.1, 5.2, 5.3, 5.4, 5 .5, 5.6, 5.7, 5.8,5.9,5.10	SL5.1 SL5.2

\*



#### Semester-II

Course Code: 78MS204

Course Title : Ordinary and Partial Differential Equations

Pre- requisite: Students should have basic knowledge of

calculus, linear algebra, and ODE theory.

Rationale: The program aims to develop advanced problem-

solving and analytical skills and prepares students for careers in academia, research, industry, or other sectors that require advanced

mathematical expertise.

#### Course Outcome:

- **CO1- 78MS204.1** Solve first-order non-linear differential equations and linear differential equations.
- **CO2- 78MS204.2** Formulate mathematical models using ODEs to represent real-world problems.
- **CO3-78MS204.3**. Formulate differential equations for various mathematical models.
- **CO4-78MS204.4** Study techniques for handling linear PDEs and understand their behavior and applies partial derivative equation techniques to predict the behavior of certain phenomena.
- **CO3-78MS204.5** Apply numerical methods (e.g., Euler's method, Runge-Kutta methods) to approximate solutions of ODEs.

#### **Scheme of Studies:**

Board of Course Cour Study Code Title			Scheme of studies (Hours/Week)					
Study	code	Title	CI	LI	SW	SL	Total Study Hours (CI+LI+SW+SL)	ts (C)



Program	78MS204	Ordinary	4[3+1]	0	1	1	6	4
Core		and						
(PCC)		Partial						
		Differenti						
		al						
		Equation						
		S						

### Legend:

**CI:** Classroom Instruction (Includes different instructional strategies i.e. Lecture (L) and Tutorial (T) and others),

**LI:** Laboratory Instruction (Includes Practical performances in laboratory workshop, field or other locations using different instructional strategies)

**SW:** Sessional Work (includes assignment, seminar, mini project etc.),

SL: Self Learning,

C:Credits.

**Note:** SW & SL has to be planned and performed under the continuous guidance and feedback of teacher to ensure outcome of Learning.

#### **Scheme of Assessment:**

### **Theory**

Board of	Couse	Course		Schem	e of Assess	ment ( M	arks )			
Study	Code	Title	Progressive Assessment ( PRA )						End Semester Assessm ent (ESA)	Total Marks (PRA+ ESA)
			Class/Ho me Assignme nt 5 number 3 marks each ( CA)	Class Test 2 (2 best out of 3) 10 marks each (CT)	Seminar one (SA)	Class Activit y any one (CAT)	Class Attend ance (AT)	Total Marks (CA+CT+ SA +CAT+A T)		



PCC	78MS204	Ordinary	15	20	5	5	5	50	50	100
		and								
		Partial								
		Differenti								
		al								
		Equation								
		s								

#### **Course-Curriculum Detailing:**

This course syllabus illustrates the expected learning achievements, both at the course and session levels, which students are anticipated to accomplish through various modes of instruction including Classroom Instruction (CI), Laboratory Instruction (LI), Sessional Work (SW), and Self Learning (SL). As the course progresses, students should showcase their mastery of Session Outcomes (SOs), culminating in the overall achievement of Course Outcomes (COs) upon the course's conclusion.

#### CO1-78MS204.1

Solve first-order non-linear differential equations and linear differential equations.

Item	AppX Hrs
Cl	12
LI	0
SW	1
SL	1
Total	14

Session Outcomes (SOs)	Laboratory Instruction (LI)	Class room Instruction (CI)	Self Learning (SL)
SO1.1		Unit-1.0	SL.1
Students should		Ordinary Differential	Student get knowadge
be able to identify		equation of first order and	to solve Homogeneous
ordinary		First Degree:	Differential equation
differential		1.1 concept of differential	SL.2



_			
equations that can	-	equation	Student understand
be solved using			how to solve different
the various		1.2 Classifies the	differential equation
methods.		differential equations with	
		respect to their order and	
SO1.2		degree	
Develop skills in		1.3 explination of variable	
solving initial		separable method	
value problems		1.4 questions based on	
using the variable		variable separable method	
separable method		1.5 Explination of	
SO1.3		Homogeneous Differential	
Develop the ability		equation method	
to solve linear		1.6 Questions of	
differential		Homogeneous Differential	
equations using		equation method	
integrating		1.7 Concept of Linear	
factors.		Differential equation in y	
		and x	
So1.4		1.8 Questions of Linear	
Recognize exact		Differential equation in y	
differential		and x	
equations and		1.9 Questions of Bernoulli's	
understand the		equation	
conditions for		1.10 Tutorial-1	
exactness		1.11 Exact Differential	
So1.5		equation	
Student		1.12 Integrating factor	
understand the			
concept of			
Bernoulli's			
equation and its			
application in			
modeling various			
<u> </u>			
phenomena			
Student understand the concept of Bernoulli's equation and its application in modeling various physical		equation 1.12 Integrating factor	

### SW-1 Suggested Sessional Work (SW):



### a. Assignments:

- i. Write all the formula of exat equation.
- ii. Write a short note on application of Differential equation.
- **b.** Other Activities (Specify): Quiz, Class Test.

### CO2-78MS204.2

Formulate mathematical models using ODEs to represent real-world problems.

Item	AppX Hrs
Cl	12
LI	0
SW	1
SL	1
Total	14

		Total	
Session Outcomes	Laboratory	Class room Instruction	Self Learning
(SOs)	Instruction	(CI)	(SL)
	(LI)		
SO2.1 Understand the		Unit-2.0	<b>SL.1</b> Apply rules of CF
concept of Linear		Ordinary simultaneous	& PI to evaluate
Differential equation		Differential equation 2.1	Differential
with Constant		Introduction of Linear	equation
coefficients		Differential equation with	
SO2.2		Constant coefficients	SL.2
Evaluate complimentary function by different rules SO2.3 Evaluate particular integral by different rules SO2.4		2.2 Rules of CF 2.3 Questions of CF 2.4 Rules for solving PI 2.5 Questions of PI 2.6 Introduction of simultaneous Differential equation in Different form 2.7 Tutorial -1	Students apply methods for solving Simultaneous linear Differential equation
Understand the concept of		2.8 Methods of solving	



Simultaneous linear	Simultaneous linear	
Differential equation	Differential equation with	
SO2.5	Constant coefficients	
Evaluate Different		
problems of	2.9 Rules of solving	
Simultaneous linear	Simultaneous linear	
Differential equation with Constant	Differential equation with	
coefficients	Constant coefficients	
occiniorents		
	2.10 Questions of	
	Simultaneous linear	
	Differential equation with	
	Constant coefficients	
	2.11 Some different	
	questions of Simultaneous	
	linear Differential equation	
	with Constant coefficients	
	2.12 Tutorial -2	

### SW-2 Suggested Sessional Work (SW):

### a. Assignments:

- i. Make a list of all formula of Complimentary function.
- ii. Make a list of all formula of particular integral.
- **b.** Other Activities (Specify): Class Test.



### CO3-78MS204.3

Formulate differential equations for various mathematical models.

Item	AppX Hrs
Cl	12
LI	0
SW	1
SL	1
Total	14

Session Outcomes (SOs)	Laborator y Instructio n (LI)	Class room Instruction (CI)	Self Learning (SL)
SO3.1 Understand the concept of PDE SO3.2 Understand the methods of formation of PDE SO3.3 Apply Charpit formula for solving Differential equation SO3.4 Apply Lagrange method for solving Differential equation SO3.5 Understand the concept of Linear partial Differential equation with constant coefficie		Unit-3.0 Partial Differential equation 3.1 Introduction of PDE 3.2 Difference between PDE and ODE with examples 3.3 Formation of PDE by eliminating arbitrary constant 3.4 Formation of PDE by eliminating arbitrary function 3.5 Explination of Lagrange method by formula 3.6 Questions of Lagrange method 3.7 Explination of Charpit methods by formula 3.8 Questions of Charpit methods 3.9 Linear partial Differential equation with constant coefficients(CF & PI FOR PDE) 3.10 Questions for CF 3.11 Questions of PI 3.12 Tutorial -1	SL.1 Define and understand partial differential equation SL.2 Define and understand Charpit and Lagrange method



### **SW-3 Suggested Sessional Work (SW):**

### a. Assignments:

- i. write the difference between pde and ode.
- ii. Application of PDE.
- iii. Write all formula of unit.

### b. Mini Project:

Oral presentation

**c.** Other Activities (Specify): Class Test.

#### CO4-78MS204.4

Study techniques for handling linear PDEs and understand their behavior and applies partial derivative equation techniques to predict the behavior of certain phenomena.

Item	AppX Hrs
Cl	12
LI	0
SW	1
SL	1
Total	14

Session Outcomes	Laboratory Instruction	Class room Instruction	Self Learning
(SOs)	(LI)	(CI)	(SL)
SO 4.1		Unit-4.0 Linear	SL.1
Understand the		Differential equation	Verify relationships
fundamental concepts		of second order with	between operations
of Linear Differential		variable coefficient	satisfying various
equation of second		4.1 Explination of	properties.
order with variable		Linear Differential	
coefficient		equation of second	
SO 4.2		order with variable	
Student apply different		coefficient	
method of inspection		4.2 explanation of	



method	methods of solution of
SO 4.3	Linear Differential
Student apply change	equation of second
the independent	order with variable
variable method	coefficient
SO 4.4	4.3 Formula of
Student apply Removal	inspection method
of first derivative	4.4 case 1 of inspection
method	method
SO 4.5	4.5 Case 2 of inspection
Understand the	method
fundamental concepts	4.6 Case 3 of inspection
of variation of	method
parameter	4.7 inspection method,
	when one integral
	known
	4.8 change the
	independent variable
	4.9 Questions of
	change the
	independent variable
	4.10 Removal of first
	derivative
	4.11 formula for
	variation of parameter
	4.12 Questions of
	variation of parameter
	·

### **SW-4 Suggested Sessional Work (SW):**

### a. Assignments:

i. Write all the methods of methods of solution of Linear Differential equation of second order with variable coefficient

**b.** Other Activities (Specify): Class Test.

#### CO5-78MS101.5

Apply numerical methods (e.g., Euler's method, Runge-Kutta methods) to approximate solutions of ODEs.



, the commo	110 110 0110					
Item	AppX Hrs					
Cl	12					
LI	0					
SW	1					
SL	1					
Total	14					

Session Outcomes (SOs)	Laboratory Instruction (LI)	Class room Instruction (CI)	Self Learning (SL)
SO5.1 Understand the application of ODE SO 5.2 Understand the application of PDE SO 5.3 Apply Picard's method to solve ODE SO 5.4 Apply Euler's method to solve ODE SO 5.5 Understand concept of one Dimensional Heat and wave equation		Unit-5.0 Application of ODE and PDE'S 5.1 Give explanation of Application of ODE 5.2Explination of different Numerical methods for Solution of Ordinary Differential equation. 5.3 Formula and simple Questions of Picard's method 5.4 Some more questions of Picard's method 5.5 Formula and simple Questions of Taylor's method 5.6 Some more questions of Picard's method 5.7 Formula and simple Questions of Euler's method 5.8 Formula and Questions modified 5.9 Formula and simple Questions of Runge-kutta method 5.10 Method of separation of variables	SL.1 Learn application of ODE SL.2 Learn application of PDE



5.11 one Dimensional Heat	
equation	
5.12 one Dimensional	
wave equation	

### SW-5 Suggested Sessional Work (SW):

### a. Assignments:

- i. Write the application of ODE.
- ii Write the application of PDE.
- **b.** Other Activities (Specify):

Class Test.

### **Brief of Hours suggested for the Course Outcome**

Course Outcomes	Class Lecture (CI)	Sessional Work (SW)	Self Learning (SI)	Total hour (Cl+SW+SI)
CO1- 78MS204.1  Solve first-order non-linear differential equations and linear differential equations.	12	1	1	14
CO1- 78MS204.2 Formulate mathematical models using ODEs to represent real-world problems.	12	1	1	14
CO1- 78MS204.3  Formulate differential equations for various mathematical models.	12	1	1	14
CO1- 78MS204.4 Study techniques for handling linear PDEs and understand their behavior andapplies partial derivative equation techniques to predict the behavior of certain phenomena.	12	1	1	14



CO1- 78MS204.5  Apply numerical methods (e.g., Euler's method, Runge-Kutta methods) to approximate solutions of ODEs.	12	1	1	14
Total Hours	60	5	5	70

### **Suggestion for End Semester Assessment**

### Suggested Specification Table (For ESA)

СО	Unit Titles	Marks	Distribut	Total Marks		
		R U		Α		
CO1-	Solve first-order non-linear differential equations and linear differential equations.		04	01		10
CO2-	Formulate mathematical models using ODEs to represent real-world problems.	02	06	02		10
CO3-	Formulate differential equations for various mathematical models.	03	05	02		10
CO4-	Study techniques for handling linear PDEs and understand their behavior and applies partial derivative equation techniques to predict the behavior of certain phenomena.	05	03	02		10
CO5-	Apply numerical methods (e.g., Euler's method, Runge-Kutta methods) to approximate solutions of ODEs.	02	04	04	-	10
Total		17	22	11		50



Legend: R: Remember, U: Understand, A: Apply

The end of semester assessment for Introduction to Portland cement will be held with written examination of 50 marks

**Note**. Detailed Assessment rubric need to be prepared by the course wise teachers for above tasks. Teachers can also design different tasks as per requirement, for end semester assessment.

### **Suggested Instructional/Implementation Strategies**

- 1. Improved Lecture
- 2. Tutorial
- 3. Presentation
- 4. Group Discussion
- 5. Online sources
- 6 .Seminar
- 7. Workshop

### **Suggested Learning Resources:**

### a) Books:

S. N	Title	Publisher	Edition & Year	
0.				
1	Partial Differential equation	Dr.H.K.Pathak	Shree Sahitya Siksha Prakashan, Meerut.	Edition 2023-24
2	ODE & PDE	M.D.Rai Singhania	S. Chand Publications	20th Edition
3	Mathematics 1	D.K.Jain	Shree ram publication	



	Ordinary Differe	ntial G.F.	Simmons	Tata McGraw Hill	
4	Equations	with			
	Applications				

### b) Reference Book:

S. No	Title	Author	Publisher	Edition & Year
1	Ordinary Differential Equations	M.L. Jain and Satbir Mehla	Jeevansons Publications	Thirteenth Edition
2	Calculus and Ordinary Differential Equations	S.K Mishra and K.K Pradhan	VK Global Publications	2023-24 edition
3	Partial Differential Equation-With Boundary Value Problems	Dr. H.K. Pathak and J.P. Chauhan	Shree Shiksha Sahitya Prakashan;	Fourth Revised Edition Reprint 2021-2022
4	Partial Differential Equations	S. G. Venkatachalapathy	Margham Publications	

### c) Online books:

Suggested Digital	https://old.mu.ac.in/wp-content/uploads/2020/12/Paper-IV-Ordinary-
Platforms Web	Diffrential-Equation.pdf
links:	
Suggested	https://onlinecourses.nptel.ac.in/noc24_ma37/preview
<b>Equivalent online</b>	
courses:	

### **Curriculum Development Team:**

- 1. 1. Dr. Sudha Agrawal, HOD, Department of Mathematics.
- 2. Dr.Ekta Shrivastava , Assistant Professor, Department of Mathematics.
- 3. Mr. Neelkanth Napit, Assistant Professor, Department of Mathematics.
- 4. Mrs. Vandana Soni, Assistant Professor, Department of Mathematics.



- 5. Mr.Radhakrishna Shukla, Assistant Professor, Department of Mathematics.
- 6. Mr.Ghanhyam sen, Assistant Professor, Department of Mathematics.
- 7. Ms. Pushpa Kushwaha, Assistant Professor, Department of Mathematics.
- 8. Ms. Arpana Tripathi, Assistant Professor, Department of Mathematics

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### **Cos, POs and PSOs Mapping**

**Course Title: M.Sc. Mathematics** 

Course Code: 78MS204

**Course Title: Ordinary and Partial Differential Equations** 

	РО	Р	PO3	РО	PO5	РО	PO7	PO8	PO9	PO10	РО	PO12	PSO 1	PS	PSO 3	PS
Course	1	0	'	4	·	6	·	<u>'</u>	·		11	<u>'</u>	ĺ '	02		04
Outcome	<u> </u>	2			'	<u> </u>	'	<u> </u>	'			<u> </u>		<u> </u>		
	Adv	Pr	Resear	Qu	Teac	The	Com	Oper	Appli	Engi	Go	Cons	Under	На	Develo	Cre
	anc	О	ch	ant	hing	ore	muni	ation	catio	neeri	ver	ultin	stand	ndl	р	ate
	ed	bl	Abiliti	itat	and	tica	catio	S	n in	ng	nm	g	the	е	necess	S



### **AKS University**

### Faculty of Basic Science Department of Mathematics

### Curriculum & Syllabus of M.Sc. Mathematics program <u>Department of Mathematics</u>

	Ma the ma tica I Kn owl edg e	e m - so lvi n g Sk ill s	es	ive An alys is	Acad emia	Un der sta ndi ng	n Skills	Rese arch	Indu stry	and Tech nolo gy	ent and Pub lic Sec tor		mathe matica I conce pts and applic ations in the field of algebr a	the adv anc ed tec hni que s	ary skills and expert ise in the field of resear ch	Ma the ma tic al Mo del s
CO1- 78MS204. 1 Solve first- order non- linear differential equations and linear differential equations.	2	3	1	2	1	2	2	2	1	1	1	1	2	1	1	2
CO2- 78MS204. 2. Formulate mathemat ical models using ODEs to represent real-world problems.	1	3	2	1	1	1	1	1	1	2	3	1	<u>3</u>	1	1	1
CO3- 78MS204.3 . Formulate	1	3	2	2	1	1	3	2	1	1	3	1	<u>2</u>	<u>1</u>	<u>2</u>	



differential equations for various mathemati cal models.																
78MS204.4 Study techniques for handling linear PDEs and understand their behavior and applies partial derivative equation techniques to predict the behavior of certain phenomen a.	2	3	2	2	1	1	3	2	1	1	3	1	2	1	2	2
CO5- 78MS204.5 Apply numerical methods (e.g., Euler's method, Runge- Kutta	2	3	2	2	1	1	3	2	1	1	3	1	<u>2</u>	1	<u>2</u>	2



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methods)								
to								
approximat e solutions of ODEs.								

Legend: 1 – Low, 2 – Medium, 3 – High

### **Course Curriculum Map:**

POs & PSOs	COs No.& Titles	SOs No.	Laborat	Classroom Instruction	Self Learning (SL)
No.			ory	(CI)	
			Instructi		
			on(LI)		
PO	CO1- 78MS204.1	SO1.1		Unit-1.0 Group	SL1.1
1,2,3,4,5,6	Solve first-order non-linear	SO1.2		1.1,1.2,1.3,1.4,1.5,1.6,1.	SL1.2
7,8,9,10,11,	differential equations and	SO1.3		7,1.8,1.9,1.10,1.11,1.12	
12	linear differential equations.	SO1.4			
PSO 1,2, 3, 4	·	SO1.5			
PO	CO2- 78MS204.2.	SO1.1		Unit-2 Ring	SL2.1
1,2,3,4,5,6	Formulate mathematical	SO1.2		2.1, 2.2, 2.3, 2.4, 2.5, 2.6,	SL2.2
7,8,9,10,11,	models using ODEs to	SO1.3		2.7, 2.8,2.9,2.10	



### Faculty of Basic Science Department of Mathematics

### Curriculum & Syllabus of M.Sc. Mathematics program <u>Department of Mathematics</u>

12		CO1 1	2 11 2 12	
12	represent real-world	SO1.4	2.11,2.12	
PSO 1,2, 3, 4	problems.	SO1.5		
PO	CO3- 78MS204.3. Formulate	SO1.1	Unit-3	SL3.1
1,2,3,4,5,6	differential equations for	SO1.2	2.1, 2.2, 2.3, 2.4, 2.5, 2.6,	SL3.2
7,8,9,10,11,	various mathematical	SO1.3	2.7,	
12	models.	SO1.4	2.8,2.9,2.10,3.11,3.12	
PSO 1,2, 3, 4		SO1.5		
PO	CO4-	SO1.1	Unit-4	SL4.1
1,2,3,4,5,6	78MS204.4 Study	SO1.2	2.1, 2.2, 2.3, 2.4, 2.5, 2.6,	
7,8,9,10,11,	techniques for handling	SO1.3	2.7,	
12	linear PDEs and understands	SO1.4	2.8,2.9,2.10,4.11,4.12	
PSO 1,2, 3, 4	their behavior and applies	SO1.5		
	partial derivative equation			
	techniques to predict the			
	behavior of certain			
	phenomena.			
PO	CO5- 78MS204.5 Apply	SO1.1	Unit-5	SL5.1
1,2,3,4,5,6	numerical methods (e.g.,	SO1.2	2.1, 2.2, 2.3, 2.4, 2.5, 2.6,	SL5.2
7,8,9,10,11,	Euler's method, Runge-Kutta	SO1.3	2.7, 2.8,2.9,2.10,	
12	methods) to approximate	SO1.4	5.11,5.12	
PSO 1,2, 3, 4	solutions of ODEs.	SO1.5		

\*



### Semester-I

Course Code:	78MS205
Course Title :	[Advanced Discrete Mathematics]
Pre- requisite:	Among then of great importance are first, the actuality
	of the theme of the research; second-the choice of
	adequate research instruments and taxonomy to the
	chosen object field.
Rationale:	Think of a research rationale as a set of reasons that
	explain why a study is necessary and important based
	on its background.

### **Course Outcome:**

- **CO1-** 78MS205.1 Learn the structure of graphs and familiarize the basic concepts used to analyses different problems in different branches such as chemistry, computer science etc.
- CO2- 78MS205.2. Analyze characterization of special graphs.
- **CO3-** 78MS205.**3**. Understand the importance of algebraic properties with regard to working within various number systems.
- **CO4-** 78MS205.4 Acquire knowledge of Boolean algebras and Boolean function and understand how these concepts arise in certain real life problems.
- **CO5-** 78MS205.5 Learn the equivalence of deterministic and non deterministic finite accepters.

### **Scheme of Studies:**

Board of	Course Code	Course Title	Scheme of studies (Hours/Week)					
Study	Code		Cl	LI	SW	SL	Total Study Hours (CI+LI+SW+SL)	ts (C)



Progra	78MS205	Advanced	4[3+1]	0	1	1	6	4
m Core		Discrete						
(PCC)		Mathematic						
		S						

### Legend:

**CI:** Classroom Instruction (Includes different instructional strategies i.e. Lecture (L) and Tutorial (T) and others),

**LI:** Laboratory Instruction (Includes Practical performances in laboratory workshop, field or other locations using different instructional strategies)

**SW:** Sessional Work (includes assignment, seminar, mini project etc.),

SL: Self Learning,

C:Credits.

**Note:** SW & SL has to be planned and performed under the continuous guidance and feedback of teacher to ensure outcome of Learning.

### **Scheme of Assessment:**

### Theory

Board	Couse	Course Title		Schem	e of Assess	ment ( M	arks )			
of Study	Code		Progi						End Semester Assessm ent (ESA)	Total Marks (PRA+ ESA)
			Class/Ho me Assignme nt 5 number 3 marks each ( CA)	Class Test 2 (2 best out of 3) 10 marks each (CT)	Seminar one ( SA)	Class Activit y any one (CAT)	Class Attend ance (AT)	Total Marks (CA+CT+ SA +CAT+A T)		
PCC	78MS205	Advanced Discrete Mathematics	15	20	5	5	5	50	50	100



### **Course-Curriculum Detailing:**

This course syllabus illustrates the expected learning achievements, both at the course and session levels, which students are anticipated to accomplish through various modes of instruction including Classroom Instruction (CI), Laboratory Instruction (LI), Sessional Work (SW), and Self Learning (SL). As the course progresses, students should showcase their mastery of Session Outcomes (SOs), culminating in the overall achievement of Course Outcomes (COs) upon the course's conclusion.

**CO1-** 78MS205.1 Learn the structure of graphs and familiarize the basic concepts used to analyses different problems in different branches such as chemistry, computer science etc.

Item	AppX Hrs
Cl	13
LI	0
SW	1
SL	1
Total	15

Session Outcomes	Laboratory Instruction	Class room Instruction	Self Learning
(SOs)	(LI)	(CI)	(SL)
SO1.1		Unit-1.0	SL.1
Understand the		1.1 Formal Logic statements	Understand the
concept of Group.		1.2 Symbolic representation	concept of Symbolic
		1.3 Tautologies	representation
SO1.2		1.4 Quantifiers	
Understand the		1.5 Proposition logic	SL.2
Proposition logic		1.6 . Graph Theory	Decide whether a
SO1.3		1.7 Definition of	Connectivity
Understand the		(undirected)graph,	SL.3
relation between		1.8 Sub graph, Paths,	Express a given simple
Circuits & cycles		1.9 Circuits & cycles.	graph ,Weight Graph ,



1.10 simple graph ,Weight Graph ,	
1.11 Degree of vertices, 1.12 Connectivity. 1.13 Planer graph their properties.	

### SW-1 Suggested Sessional Work (SW):

### a. Assignments:

i. simple graph ,Weight Graph ,

ii Explain the Symbolic representation

**CO2-** 78MS205.2. Analyze characterization of special graphs.

Item	AppX Hrs
Cl	12
LI	0
SW	1
SL	1
Total	14

Session Outcomes	Laboratory Instruction	Class room Instruction	Self Learning
(SOs)	(LI)	(CI)	(SL)
SO2.1		Unit-2.0	SL.1
Understand the		2.1Euler's formula	Verify complete
Kuratowski's Theorem		2.2connected planar	Bipartite graphs
		graphs.	
SO2.2		2.3 Complete graph 2.4	SL.2
Learn about Matrix		complete Bipartite	Present concepts of the
representation of		graphs.	incidence matrices of a
Graphs.		<b>2.5</b> Kuratowski's	Graph
SO2.3		Theorem (statement	SL.3
Understand the		only) and its use.	Knowledge of



concept of connected	2.6 Matrix	Homomorphism Graph
planar graphs.	representation of	
	Graphs.	
	2.7Tutorial-1	
	2.8Adjacency matrices	
	of a Graph	
	2.9 incidence matrices	
	of a Graph. 2.10	
	Isomorphic Graph	
	2.11 Homomorphism	
	Graph	
	2.12 Tutorial-2	

### SW-2 Suggested Sessional Work (SW):

### a. Assignments:

- i. Write the Adjacency matrices of a Graph.
- ii.Write the Kuratowski's Theorem

**CO3-** 78MS205.**3**. Understand the importance of algebraic properties with regard to working within various number systems.

Item	AppX Hrs	
Cl	11	
LI	0	
SW	1	
SL	1	
Total	13	

Session Outcomes (SOs)	Laboratory Instruction (LI)	Class room Instruction (CI)	Self Learning (SL)
SO3.1		Unit-3.0	SL.1 Direct
Understand the partially		3.1 introduction of Lattices	products.



ordered set		
SO3.2 Explain Some	3.2 partially ordered set	<b>SL.2</b> Complemented Lattices
Special Lattices	<ul><li>3.3partially ordered set and their properties.</li><li>3.4 Tutorial-1</li></ul>	<b>SL.3</b> Distributive Lattices
SO3.3 Distributive	3.5 Sublattices	
Lattices	3. 6Tutorial-2	
	3.7 Direct products.	
	3.8Explain Some Special Lattices	
	3.9 Complete Lattices	
	3.10 Complemented Lattices	
	3.11 Distributive Lattices	

### **SW-3 Suggested Sessional Work (SW):**

### a. Assignments:

- i. Relationships between partially ordered set and their properties
- ii. Explain the Distributive Lattices
- iii Lattices as algebraic systems.

**CO4-** 78MS205.4 Acquire knowledge of Boolean algebras and Boolean function and understand how these concepts arise in certain real life problems.

AppX Hrs
13
0
1
1
15



Session Outcomes	Laboratory Instruction (LI)	Class room Instruction	Self Learning
(SOs)		(CI)	(SL)
SO4.1 understand the Switching Algebra SO4.2Using AND,OR & NOT gates.		Unit-4.0  4.1 Boolean Algebras as Lattices.  4.2 Various Boolean identities,  4.3 Sub Algebra.  4.4Booleanforms  4.5equivalence,  4.6Minterms Boolean forms,  4.7Sum of products 4.8 canonical forms.  4.9Switching Algebra  4.10examples.  4.11Apllication of BooleanAlgebra  4.12Boolean Algebra to Switching Theory  4.13 Using AND,OR & NOT gates.	SL.1 Verify the Various Boolean identities, SL.2 Equivalence, SL.3 canonical forms.

### **SW-4 Suggested Sessional Work (SW):**

### a. Assignments:

- i. Boolean Algebras as Lattices.
- ii. Boolean forms
- iii. Switching Theory

### **b.** Other Activities (Specify):

Quiz, Class Test.

**CO5-** 78MS205.**5** Learn the equivalence of deterministic and non deterministic finite accepters.



Item	AppX Hrs	
Cl	11	
LI	0	
SW	1	
SL	1	
Total	13	

Session Outcomes	Laboratory Instruction (LI)	Class room Instruction	Self Learning
(SOs)		(CI)	(SL)
SO5.1 Understand Minimal Spanning tree SO5.2 Understand Finite state machines		Unit-5.0 5.1Definition of tree 5.2 types of tree 5.3networks, 5.4 Spanning Tree, cut- sets. 5.5Minimal Spanning tree 5.6Kruskal'sAlgorithm 5.7 Finite state machines 5.8 types of Finite state machines 5.8 transition table diagrams. 5.9Equivalence of finite state machines. 5.10 Reduced Machines 5.11 Tutorial	SL.1Verify the types of Finite state machines SL.2 Equivalence of finite state machines

### SW-5 Suggested Sessional Work (SW):

- a. Assignments:
- i. Equivalence of finite state machines
- ii. Spanning Tree
- iii. Finite state machines
- **b.** Other Activities (Specify): Class Test.

**Brief of Hours suggested for the Course Outcome** 



Course Outcomes	Class Lecture (CI)	Sessional Work (SW)	Self Learning (SI)	Total hour (CI+SW+SI)
co1- 78MS205.1 Learn the structure of graphs and familarize the basic concepts used to analyses different problems in different branches such as chemistry, computer science etc.	13	1	1	12
CO2- 78MS205.2. Analyze characterization of special graphs.	12	1	1	14
CO3- 78MS205.3. Understand the importance of algebraic properties with regard to working within various number systems.	11	1	1	13
co4- 78MS205.4 Acquire knowledge of Boolean algebras and Boolean function and understand how these concepts arise in certain real life problems.	13	1	1	12



<b>CO5</b> - 78MS205. <b>5</b> Learn the	11	1	1	11
equivalence of				
deterministic and non				
deterministic finite				
accepters.				
Total Hours	60	5	5	70
1000.1100.0				' "

### **Suggestion for End Semester Assessment**

### Suggested Specification Table (For ESA)

CO Unit Titles		Marks Distribution			Total Marks	
		R	U	Α		
CO-1	Learn the structure of graphs and familarize the basic concepts used to analyses different problems indifferent branches such as chemistry, computer science etc.	03	01	01		05
CO-2	Analyze characterization of special graphs.	02	06	02		10
CO-3	Understand the importance of algebraic properties with regard to working within various number systems.	03	07	05		15
CO-4	Acquire knowledge of Boolean algebras and Boolean function and understand how these	-	10	05		15



	concepts arise in certain real life problems.				
CO-5	Learn the equivalence of deterministic and non deterministic finite accepters.	03	02	-	05
Total		11	26	13	50

Legend: R: Remember, U: Understand, A: Apply

The end of semester assessment for Introduction to Portland cement will be held with written examination of 50 marks

**Note**. Detailed Assessment rubric need to be prepared by the course wise teachers for above tasks. Teachers can also design different tasks as per requirement, for end semester assessment.

### **Suggested Instructional/Implementation Strategies**

- 1. Improved Lecture
- 2. Tutorial
- 3. Presentation
- 4. Group Discussion
- 5. Online sources
- 6 .Seminar
- 7. Workshop



### **Suggested Learning Resources:**

### a) Books:

S.	Title	Author	Publisher	Edition & Year
No.				
1	Discrete	J.P.Tremblay & R.		
	Mathematical	Manohar		
	Structure with			
	Applications to			
	computer science			
2	Finite mathematics	Seymour Lepschutz		
		C.L.Liu		
3	Elements of Discrete			
	Mathematics			
		Kenneth H. Rosen		
	Discrete mathematics			
4	and its applications			
	Discrete and	R.P. Grimaldi		
	combinatorial			
_	mathematics An			
5	applied introduction			

### **Curriculum Development Team:**

- 1. 1. Dr. Sudha Agrawal, HOD, Department of Mathematics.
- 2. Dr.Ekta Shrivastava, Assistant Professor, Department of Mathematics.
- 3. Mr. Neelkanth Napit, Assistant Professor, Department of Mathematics.
- 4. Mrs. Vandana Soni, Assistant Professor, Department of Mathematics.
- 5. Mr.Radhakrishna Shukla, Assistant Professor, Department of Mathematics.
- 6. Mr.Ghanhyam sen, Assistant Professor, Department of Mathematics.
- 7. Ms. Pushpa Kushwaha, Assistant Professor, Department of Mathematics.
- 8. Ms. Arpana Tripathi, Assistant Professor, Department of Mathematics

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### **Cos, POs and PSOs Mapping**

**Course Title: M.Sc. Mathematics** 

Course Code: 78MS205

**Course Title: Advanced Discrete Mathematics** 

	PO 1	PO2	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10	PO1	PO12	PSO 1	PSO 2	PSO 3	PSO 4
	Ad	Proble	Res	Qua	Teachi	Theo	Comm	Operat	Applic	Engine	Gov	Consul	Understa	Handl	Develop	Crea
Course	van	m-	earc	ntita	ng and	retic	unicati	ions	ation	ering	ern	ting	nd the	e the	necessar	tes
Outcome	ced	solvin	h	tive	Acade	al	on	Resear	in	and	men		mathem	advan	y skills	Mat
	Ma	g	Abili	Anal	mia	Und	Skills	ch	Industr	Techn	t		atical	ced	and	hem
	the	Skills	ties	ysis		ersta			У	ology	and		concepts	techni	expertise	atica
	ma					ndin					Publi		and	ques	in the field of	   N4 = =
	tica					g					c Sect		applicati ons in		research	Mod els
	Kn										or		the field		research	CIS
	owl										0.		of			
	edg												algebra			
	е															
						_										
CO1-	2	3	1	2	1	2	2	2	1	1	1	1	2	1	<u>1</u>	<u>3</u>
78MS205.1																
Learn the																
structure of																
graphs and																
familiarize																
the basic																
concepts																
used to																
analyses																
different																
problems in																
different																
branches																
such as																
chemistry,								1		[						
chemistry,													1			



computer																
computer science etc.																
CO2- 78MS205.2. Analyze characterizat ion of special graphs.	1	3	2	1	1	1	1	1	1	2	3	1	3	1	1	2
CO3- 78MS205.3. Understand the importance of algebraic properties with regard to working within various number systems.		3	2	2	1	1	3	2	1	1	3	1	2	1	2	2
CO4- 78MS205.4 Acquire knowledge of Boolean algebras and Boolean function and understand how these concepts arise in certain real life problems.	2	3	2	2	1	1	3	2	1	1	3	1	2	1	2	2



CO5-	2	3	2	2	1	1	3	2	1	1	3	1	<u>2</u>	1	<u>2</u>	3
78MS205.5																
Learn the																
equivalence																
of																
deterministi																
c and non																
deterministi																
c finite																
accepters.																

Legend: 1 – Low, 2 – Medium, 3 – High

### **Course Curriculum Map:**

POs & PSOs No.	COs No.& Titles	SOs No.	Laboratory Instruction(LI)	Classroom Instruction (CI)	Self Learning (SL)
PO 1,2,3,4,5,6 7,8,9,10,11,1 2 PSO 1,2, 3, 4	CO1- 78MS205.1 Learn the structure of graphs and familiarize the basic concepts used to analyses different problems in different branches such as chemistry, computer science etc.	S01.1 S01.2 S01.3 S01.4 S01.5		Unit-1.0 Group 1.1,1.2,1.3,1.4,1.5,1.6,1. 7,1.8,1.9,1.10	SL1.1 SL1.2 SL1.3
PO 1,2,3,4,5,6 7,8,9,10,11,1 2	CO2- 78MS205.2. Analyze characterization of special graphs.	SO1.1 SO1.2 SO1.3 SO1.4 SO1.5		Unit-2 Ring 2.1, 2.2, 2.3, 2.4, 2.5, 2.6, 2.7, 2.8,2.9,2.10	SL2.1 SL2.2



PSO 1,2, 3, 4				
PO 1,2,3,4,5,6 7,8,9,10,11,1 2 PSO 1,2, 3, 4	CO3- 78MS205.3.  Understand the importance of algebraic properties with regard to working within various number systems.	SO1.1 SO1.2 SO1.3 SO1.4 SO1.5	Unit-3 2.1, 2.2, 2.3, 2.4, 2.5, 2.6, 2.7, 2.8,2.9,2.10	SL3.1 SL3.2
PO 1,2,3,4,5,6 7,8,9,10,11,1 2 PSO 1,2, 3, 4	CO4- 78MS205.4  Acquire knowledge of Boolean algebras and Boolean function and understand how these concepts arise in certain real life problems.	SO1.1 SO1.2 SO1.3	Unit-4 2.1, 2.2, 2.3, 2.4, 2.5, 2.6, 2.7, 2.8,2.9,2.10	SL4.1 SL4.2
PO 1,2,3,4,5,6 7,8,9,10,11,1 2 PSO 1,2, 3, 4	CO5- 78MS205.5  Learn the equivalence of deterministic and non deterministic finite accepters.	SO1.1 SO1.2 SO1.3	Unit-5 2.1, 2.2, 2.3, 2.4, 2.5, 2.6, 2.7, 2.8,2.9,2.10	SL5.1 SL5.2 SL5.3

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### Semester-III

Course Code: 78MS301

Course Title : Operational Research

Pre-requisite: Students should have basic knowledge of

**Operational Research** 

Rationale: The program aims to develop advanced problem-

solving and analytical skills and prepares students for careers in academia, research, industry, or other sectors that require advanced

mathematical expertise.

### **Course Outcome:**

### CO1-78MS301.1

To learn graphical method and the simplex algorithm for solving a linear programming problem.

### CO2-78MS301.2.

To learn more optimization techniques for solving linear programming models transportation problem and integer programming problem.

### CO3-78MS301.3.

Understand optimization techniques for solving some network related problems.

### CO4-78MS301.4

To learn sensitivity analysis and parametric programming, which describes how various changes in the problem affect its solution

### CO5-78MS301.5

Ability to think innovatively to do research in high level in mathematics and interdisciplinary fields.



### AKS University Faculty of Basic Science Department of Mathematics

### Curriculum & Syllabus of M.Sc. Mathematics program

Board of	Course Code	Course Title	Scheme of studies (Hours/Week)						
Study	Code		Cl	LI	SW	SL	Total Study Hours (CI+LI+SW+SL)	ts (C)	
Progra m Core (PCC)	78MS301	Operational Research	4[3+1]	0	1	1	6	4	

### Legend:

CI: Classroom Instruction (Includes different instructional strategies i.e. Lecture (L) and Tutorial (T) and others),

**LI:** Laboratory Instruction (Includes Practical performances in laboratory workshop, field or other locations using different instructional strategies)

**SW:** Sessional Work (includes assignment, seminar, mini project etc.),

SL: Self Learning,

C:Credits.

**Note:** SW & SL has to be planned and performed under the continuous guidance and feedback of teacher to ensure outcome of Learning.

### **Scheme of Assessment:**

### Theory

Board	Couse	Course Title	Scheme of Assessment ( Marks )		
of	Code				
Study			Progressive Assessment ( PRA ) End		Total
Study					Marks
			Semo	ester	
			Asse	ssm	(PRA+
			ent		
					ESA)
			(ESA)	)	



			Class/Ho me Assignme nt 5 number 3 marks each ( CA)	Class Test 2 (2 best out of 3) 10 marks each (CT)	Seminar one (SA)	Class Activit y any one (CAT)	Class Attend ance (AT)	Total Marks (CA+CT+ SA +CAT+A T)		
PCC	78MS3		15	20	5	5	5	50	50	100
100	01	Operational Research.	15	20	,	3	,	30	30	100

### **Course-Curriculum Detailing:**

This course syllabus illustrates the expected learning achievements, both at the course and session levels, which students are anticipated to accomplish through various modes of instruction including Classroom Instruction (CI), Laboratory Instruction (LI), Sessional Work (SW), and Self Learning (SL). As the course progresses, students should showcase their mastery of Session Outcomes (SOs), culminating in the overall achievement of Course Outcomes (COs) upon the course's conclusion.

**CO1-78MS301.1** To learn graphical method and the simplex algorithm for solving a linear programming problem.

Item	AppX Hrs
Cl	12
LI	0
SW	1
SL	1
Total	14



### AKS University Faculty of Basic Science Department of Mathematics

### Curriculum & Syllabus of M.Sc. Mathematics program

Session Outcomes	Laboratory	Class room Instruction	Self Learning
(SOs)	Instruction	(CI)	(SL)
	(LI)		
SO1.1		Unit-1.0 Linear	SL.1
Understand the concept		programming problem.	Understand the definition of
of Linear programming.		1.1 Introduction	general Linear programming.
SO1.2		1.2 The definition of general	<b>SL.2</b> knowledge of the general
Understand the		Linear programming	Linear programming.
relationships between	-	problem.	SL.3
basics feasible solution.		1.3 Formulation of the	Properties of general Linear
SO1.3		Linear programming	programming
Understand the concept		problem.	
of graphical method.		1.4 Solution by graphical	
So1.4		method.	
Understand the		1.5 tutorial 1	
multiplication formula		1.6 graphical solution of	
So1.5		Linear programming.	
Understand the concept		1.7 Relation between basics	
of programming.		feasible solution.	
		1.8 tutorial 2	
		1.9 Simplex method.	
		1.10 understand the Simplex	
		method	
		1.11 question based on	
		linear programming	
		1.12 tutorial 3	

### SW-1 Suggested Sessional Work (SW):

### a. Assignment:

- **i.** Formulation of the Linear programming problem.
- ii. graphical solution of Linear programmingiii. Application of Linear programming.

### b. Mini Project:

Oral presentation, Poster presentation, Power Point Presentation.

**c.** Other Activities (Specify):

Quiz, Class Test.



**CO2-78MS301.2**. To learn more optimization techniques for solving linear programming models transportation problem and integer programming problem.

### **Approximate Hours**

Item	AppX Hrs
Cl	12
LI	0
SW	1
SL	1
Total	14

Session Outcomes	Laborator	Class room Instruction	Self Learning
(SOs)	У	(CI)	(SL)
	Instructio		
	n		
	(LI)		
SO2.1 Understand the		Unit-2.0 Solution of linear	SL.1
concept of linear		programming problem	To understand linear
programming.		2.1 Introduction.	programming problem.
SO2.2 Learn about the		2.2 Understand the Concept linear	
concept oflinear		programming	
programming problem		2.3 linear programming problem by	SL.2
by Big –M method.		Big –M method.	Knowledge of the
SO2.3 Understand the		2.4 To phase method. 2.5 Alternative	Alternative forms of
concept of Duality.		forms of generating functions.	generating functions.
SO2.4		2.6 The concept of duality	
Understand the Uses of		2.7 properties of duality	SL.3
Linear programming.		2.8 tutorial 1	Knowledge of some
SO2.5		2.9 fundamental theorem of duality.	properties of linear
Understand the		2.10 tutorial 2	programming.
concept of duality.		2.11 Dual Simplex methods.	
		2.12 Application of duality.	

### SW-2 Suggested Sessional Work (SW):

### a. Assignments:

- i. Definition and Example of linear programming problem.
- ii. Define Alternative forms of generating functions.
- iii. The concept of duality



iv fundamental theorem of duality.

### b. Mini Project:

Oral presentation, Poster presentation, Power Point Presentation.

c. Other Activities (Specify):

Quiz, Class Test.

**CO3-78MS301.3**. Understand optimization techniques for solving some network related problems.

### **Approximate Hours**

, ipproximate means			
Item	AppX Hrs		
Cl	12		
LI	0		
SW	1		
SL	1		
Total	14		

Session Outcomes (SOs)	Laboratory Instruction (LI)	Class room Instruction (CI)	Self Learning (SL)
SO3.1 Understand the principle of Traveling salesman problem. SO3.2 Understand the assignment problem SO3.3 the concept of sequencing problem.		Unit-3.0 Assignment problem.: 3.1 Introduction. 3.2 solution of assignment problem 3.3 unbalanced assignment problem. 3.4 Crew assignment problem. 3.5 tutorial 1 3.6 Traveling salesman problem 3.7 sequencing problem. 3.8 Processing n jobs on two machines. 3.9 n Jobs on three machines. 3.10 n Jobs on m machines. 3.11 Processing two jobs through m machines. 3.12 tutorial 2	SL.1 Knowledge of the.unbalanced assignment problem. SL.2 Understand an application of solution of assignment problem

### SW-3 Suggested Sessional Work (SW):

### a. Assignment:

- i. solution of assignment problem
- ii. Describe Traveling salesman problem.
- iii. Processing two jobs through m machines.



### b. Mini Project:

Oral presentation, Poster presentation, Power Point Presentation.

### c. Other Activities (Specify):

Quiz, Class Test.

**CO4-78MS301.4** To learn sensitivity analysis and parametric programming, which describes how various changes in the problem affect its solution.

Item	AppX Hrs
Cl	12
LI	0
SW	1
SL	1
Total	14

Session Outcomes	Laboratory	Class room Instruction	Self Learning
(SOs)	Instruction	(CI)	(SL)
	(LI)		
SO4.1 Understand the		Unit -4 Transportation problem.	SL.1
concept of		4.1 Introduction	knowledge of the
transportation		4.2 Initial basics feasible solution.	transportation
problem.		4.3 North- west corner method.	problem
SO4.2 understand		4.3 least- cost method.	
the.North- west corner		4.4 Vogels Approximation method.	SL.2
method.		4.5 tutorial 1	Expansion of
		4.6 Optimally test by MODI method .	Stepping stone
SO4.3 Understand the		4.7 Stepping stone method.	method.
importance of		4.8 some properties of transportation.	
transportation		4.9 Expansion of stepping stone methods	
problem.		4.10 Application of transportation problem.	
		4.11 Degeneracy in transportation problem	
		4.12 tutorial 2	



### **SW-4 Suggested Sessional Work**

- i. To solve Initial basics feasible solution.
- ii. Application of transportation problem.
- iii. The Expansion of Stepping stone method.
- iv. Calculation of Vogel's Approximation method.
- V. Degeneracy in transportation problem.

### b. Mini Project:

Oral presentation, Poster presentation, Power Point Presentation.

**c.** Other Activities (Specify):

Quiz, Class Test.

**CO5-78MS301.5** Ability to think innovatively to do research in high level in mathematics and interdisciplinary fields.

Item	AppX Hrs
Cl	12
LI	0
SW	1
SL	1
Total	14

Session Outcomes (SOs)	Laboratory Instruction (LI)	Class room Instruction (CI)	Self Learning (SL)
<b>O5.1</b> Understand the		Unit-5.0 Network Analysis:	SL.1
concept of network		<b>5.1</b> Introduction .	knowledge of
Techniques.		5.2 Constraints in network.	the network
SO5.2 Construction of		5.3 Construction of network	Techniques.
network		5.4 Definition and Example of networks.	SL.2
		5.5 tutorial 1	knowledge of
SO5.3 Constraints in		5.6 Critical path methods PERT	the
network.		5.7. PERT Calculations Resources.	Construction
		5.8 tutorial 2	of network.
		5.9 Leveling by network Techniques.	
		5.10 Advances of network (PERT/CPM).	
		5.11 Application of network Techniques.	
		5.12 tutorial 3	



### **Brief of Hours suggested for the Course Outcome**

Course Outcomes	Class Lecture (CI)	Sessional Work (SW)	Self Learning (SI)	Total hour (CI+SW+SI)
<b>CO1-78MS301.1</b> To learn graphical method and the simplex algorithm for solving a linear programming problem.	12	1	1	14
CO2-78MS301.2 To learn more optimization techniques for solving linear programming models transportation problem and integer programming problem.	12	1	1	14
<b>CO3-78MS301.3</b> . Understand optimization techniques for solving some network related problems.	12	1	1	14
CO4-78MS301.4 .To learn sensitivity analysis and parametric programming , which describes how various changes in the problem affect its solution.	12	1	1	14
CO5-78MS301.5 Ability to think innovatively to do research in high level in mathematics and interdisciplinary fields.	12	1	1	14
Total Hours	60	5	5	70



### **Suggestion for End Semester Assessment**

Suggested Specification Table For (ESA)

СО	Unit Titles	Marks Distribution		Total Marks	
		R	U	А	
CO1-	UNIT-1 linear programming problem.	03	01	01	05
CO2-	UNIT -2 Solution of linear programming problem.	02	05	03	10
СО3-	Unit-3 Assignment problem.	03	06	06	15
CO4-	Unit-4 . Transportation problem	-	10	05	15
CO5-	Unit 5 Network Analysis	03	02	-	05
Total		11	26	13	50

Legend: R: Remember, U: Understand, A: Apply

The end of semester assessment for Introduction to Portland cement will be held with written examination of 50 marks

**Note**. Detailed Assessment rubric need to be prepared by the course wise teachers for above tasks. Teachers can also design different tasks as per requirement, for end semester assessment.



# **Suggested Instructional/Implementation Strategies**

- 1. Improved Lecture
- 2. Tutorial
- 3. Presentation
- 4. Group Discussion
- 5. Online sources
- 6 .Seminar
- 7. Workshop

# **Suggested Learning Resources:**

## a) Books:

S.No.	Title	Author	Publisher	Edition
1	Operations Research	Dr. H.K. Pathak, Dr. Pradeep k.joshi	Shiksha Sahitya prakashan new delhi	2nd edition, 2000
2	Operations Research with applications.	S.D.sharma	Shiksha Sahitya prakashan	CO 2002
3	Operations Research - An introduction,	Prem Kumar Gupta and D.S. Hira	S. Chand & Company Ltd. New Delhi	
4	Operations Research - An introduction,	H.A. Tha	Macmillan Publishing co. Inc. New York.	
5	Operations Research	PK Gupta and Manmohan	Pragti prakashan New Delhi	2003

# b) Reference Book:

S.	Title	Author	Publisher	Edition & Year
No.				
1	Industrial Engineering	F.S, Hiller and G.J.	(This book comes	1995
	Series,	Lieberman	with a CD containing	
			software)	



2	Linear Programming	G. Hadley	Narosa Publishing House. 1995	
3	Linear and Dynamic	G. Hadley	Wesley Reading	
	programming		Mass	

### c) Suggetsed Digital Platform Web links:

Suggested Digital Platforms Web links:	https://www.bbau.ac.in/dept/UIET/EME-601%20Operation%20Research.pdf
Suggested Equivalent online courses:	https://www.amirajcollege.in/wp-content/uploads/2020/10/3151910- operations-research-theory-and-applications-by-jksharma-z-lib.org .pdf

# **Curriculum Development Team**

- 1. Dr.Sudha Agrawal, HOD, Department of Mathematics.
- 2. Dr.Ekta Shrivastava , Assistant Professor, Department of Mathematics.
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- 8. Ms. Arpana Tripathi, Assistant Professor, Department of Mathematics.

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# **Cos, POs and PSOs Mapping**

**Course Title: M.Sc. Mathematics** 

Course Code: 78MS301

**Course Title: Operational Research** 

	PO1	PO 2	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10	PO11	PO 12	PSO 1	P S	PSO 3	PS O 4
Course		_												0		
Outcome														2		
	Adva nced Mat hem atical Kno wled ge	Pr obl em - sol vin g Ski Ils	Rese arch Abili ties	Qua ntita tive Anal ysis	Teaching and Academi a	Theor etical Under standi ng	Com mun icati on Skills	Ope ratio ns Rese arch	Applic ation in Indust ry	Engin eering and Techn ology	Gover nmen t and Public Secto r	C o n s ul ti n g	Unders tand the mathe matical concep ts and applica tions in the field of algebra	Han dle the adva nced tech niqu es	Develo p necess ary skills and experti se in the field of researc h	Cre ate s Ma the ma tic al Mo del s
78MS301.1 to learn graphical method and the simplex algorithm for solving a linear programmin g problem.	2	1	3	2	1	2	3	3	1	1	2	1	1	2	1	2



	2	1	3	2	1	2	3	3	1	2	2	1	<u>3</u>	<u>2</u>	<u>1</u>	1
CO2-	2	1	3	2	1	2	3	3	1	2	2	1	<u> </u>	_	_	<u>1</u>
.78MS301.2.																
To learn																
more																
optimization																
techniques																
for solving																
linear																
programmin																
g models																
transportati																
on problem																
and integer																
programmin																
g problem.																
CO3-	2	1	2	2	1	3	3	2	2	2	1	1	2	2	1	<u>1</u>
.78MS301.3																
Understand																
optimization																
techniques																
for solving																
some																
network																
related																
problems.																



# AKS University Faculty of Basic Science Department of Mathematics

# Curriculum & Syllabus of M.Sc. Mathematics program

CO4-	2	1	2	2	2	2	3	2	3	2	2	2	1 2	1	1	1
78MS301.4	2	1	2	2	2	2	3	2	3	2	2		<u>2</u>	1	1	1
To learn																
sensitivity																
analysis and																
parametric																
programming																
, which																
describes																
how various																
changes in																
the problem																
affect its																
solution.																
CO5-	2	2	2	2	3	3	2	2	2	1	1	3	<u>1</u>	1	<u>2</u>	<u>1</u>
78MS301.5																
Ability to																
think																
innovatively																
to do																
research in																
high level in																
mathematics																
and																
interdisciplin																
ary fields.																
ary neius.																

Legend: 1 – Low, 2 – Medium, 3 – High



# **Course Curriculum Map:**

POs & PSOs No.	COs No.& Titles	SOs No.	Laborator Y Instructio n(LI)	Classroom Instruction (CI)	Self Learning (SL)
PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2, 3, 4	CO1- <b>78MS301.1</b> to learn graphical method and the simplex algorithm for solving a linear programming problem.	SO1.1 SO1.2 SO1.3		Unit-1.0 linear programming problem. 1.1,1.2,1.3,1.4,1.5,1.6,1.7,1	SL1.1 SL1.2
	or or had a ghara	SO1.4 SO1.5		.8,1.9,1.10 1.11 1.12	
PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2, 3, 4	CO2 <b>78MS301.2</b> . To learn more optimization techniques for solving linear programming models transportation problem and integer programming problem.	SO1.1 SO1.2 SO1.3 SO1.4 SO1.5		Unit-2 solution of linear programming problem. 2.1, 2.2, 2.3, 2.4, 2.5, 2.6, 2.7, 2.8,2.9,2.10 2.11 2.12	SL2.1 SL2.2
PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2, 3, 4	CO3- <b>78MS301.3</b> Understand optimization techniques for solving some network related problems.	SO1.1 SO1.2 SO1.3 SO1.4 SO1.5		Unit-3 . Assignment problem:  3.1, 3.2, 3.3, 3.4, 3.5, 3.6, 3.7, 3.8,3.9,3.10,3.11 3.12	SL3.1 SL3.2
PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2, 3, 4	CO4- <b>78MS301.4</b> To learn sensitivity analysis and parametric programming, which describes how various changes in the problem affect its solution.	SO1.1 SO1.2 SO1.3 SO1.4 SO1.5		Unit-4 Transportation problem: 4.1, 4.2, 4.3, 4.4, 4.5, 4.6, 4.7, 4.8,4.9,4.10. 4.11 4.12	SL4.1 SL4.2
PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2, 3, 4	CO5- <b>78MS301.5</b> Ability to think innovatively to do research in high level in mathematics and interdisciplinary fields.	SO1.1 SO1.2 SO1.3 SO1.4 SO1.5		Unit-5 <b>Network Analysis:</b> 5.1, 5.2, 5.3, 5.4, 5 .5, 5.6, 5.7, 5.8,5.9 5.10 5.11 5.12	SL5.1 SL5.2

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#### Semester-III

Course Title: Integral Equation

Course Code: - 78MS302

Prerequisite: Students should review the fundamentals of

Laplace transform and differential equation.

Rationale: The program aims to develop advanced problem-

solving in initial value problem and boundary value problem and analytical skills and prepares students for careers in academia, research, industry, or other sectors that require advanced

mathematical expertise.

### **Course Outcomes (CO):**

#### CO1-- 78MS302.1

Define and understand the concept of laplace transform and differential equation and their classification, definition of integral transform .fredholm and Volterra integral equation.

#### CO2-- 78MS302.2

Define and understand the basic concepts of integral transform method, laplacetransform, convolution integral. Application of Volterra with convolution type kernels.solution of the Cauchy type singular integral equation. And the hilbert kernel.

#### CO3-- 78MS302.3

Define and compute, symmetric kernels, orthonormal system of functions. Fundamental properties of eigenvalues and eigen functions for symmetric kernels. Solution of integral equations with symmetric kernels.

#### CO4-- 78MS302.4

Understand and definition of a boundary value problem for an ordinary equation of a second order and reduction to a fredholm integral equation of the second kind. Dirac delta function. Green function approach to reduce the boundary value problem of a self adjoint differential equation with homogenous boundary condition to integral equation form.

#### CO5- - 78MS302.5

Understand the integral representation formulae for the solution of the laplace and Poisson equations. Newtonian single layer and double layer potentials. Integral equation formulation of boundary value problem for laplace equations.



# Curriculum & Syllabus of M.Sc. Mathematics program

#### **Scheme of Studies:**

Board of Study	Course Code	Course Title	Scheme of studies (Hours/Week)						
Study	Code	Title	CI	Total Study Hours (CI+LI+SW+SL)	Credit s (C)				
PCC	78MS302	Integral equation	4[3+1]	0	1	1	6	4	

## Legend:

CI: Classroom Instruction (Includes different instructional strategies i.e. Lecture (L) and Tutorial (T) and others)

LI: Laboratory Instruction (Includes Practical performances in laboratory workshop, field or other locations using different instructional strategies)

**SW:** Sessional Work (includes assignment, seminar, mini project etc.)

SL: Self Learning,

**C:**Credits

**Note:** SW & SL has to be planned and performed under the continuous guidance and feedback of teacher to ensure outcome of Learning.

## **Scheme of Assessment:**

Theory

Board of	Couse	Course Title	Scheme of	Assessme	nt ( Marks )	)				
Study	Code		Progr	essive As	sessment (	PRA )			End	Total
									Semester	Marks
									Assessm	(PRA+
									ent	ESA)
									(ESA)	
			Class/Ho	Class	Seminar	Class	Class	Total		
			me	Test 2	one	Activit	Attend	Marks		
			Assignme	(2 best	( SA)	y any	ance	(CA+CT+		
			nt 5	out of		one	(AT)	SA		
			number	3)		(CAT)		+CAT+A		
			3 marks	10				T)		
			each	marks						
			( CA)	each						



# **Curriculum & Syllabus of M.Sc. Mathematics program**

				(CT)						
PCC	78MS302	Integral	15	20	5	5	5	50	50	100
		equation								

### **Course-Curriculum Detailing:**

This course syllabus illustrates the expected learning achievements, both at the course and session levels, which students are anticipated to accomplish through various modes of instruction including Classroom Instruction (CI), Laboratory Instruction (LI), Sessional Work (SW), and Self Learning (SL). As the course progresses, students should showcase their mastery of Session Outcomes (SOs), culminating in the overall achievement of Course Outcomes (COs) upon the course's conclusion.

### CO1-- 78MS302.1

Define and understand the concept of laplace transform and differential equation and their classification, definition of integral transform .fredholm and Volterra integral equation.

Item	AppXHrs
Cl	12
LI	0
SW	1
SL	1
Total	14

Session Outcomes (SOs)	Laboratory Instruction (LI)	Class room Instruction (CI)	Self Learning (SL)
SO1.1		Unit-1.0	SL.1
Understand the			Define the integral
basic concept of		1.1.define of integral	equation and their
integral equation		equation and her	types with their
and their types.		classification.	examples.
SO1.2	-	1.2. eigenvalues and eigen	
Understand the		functions.	SL.2
how to find		1.3. fredholm integral	Apply fredholm and
eigenvalues and		equation of kind with	Volterra integral



# Curriculum & Syllabus of M.Sc. Mathematics program

eigen functions in	seperable kernels.	equation to find the
integral equation.	1.4.reduction to a system of	eigen values and
SO1.3	algebraic equation.	eigenfunctions.
Apply reduction to	1.5.an approximation	SL.3
a system of	method.	Apply fredholm and
algebraic equation	1.6 Tutorial-1	Volterra integral
in integral	1.7. method of successive	equation to solve
equation of	approximation.	method of successive
Volterra and	1.8. iterative scheme for	approximation and
fredholm	fredholm integral equation	iterative scheme for all
equation.	of second kind	kinds.
	1.9 condition of uniform	
So1.4	convergence and	
Understand the	uniqueness series solution	
Condition of	1.10resolvent kernel and its	
uniform	results.	
convergence and	1.11application of iterative	
uniqueness series	scheme to Volterra integral	
solution.	equation of the second kind.	
So1.5	1.12 Tutorial- 2	
Understand		
theapplication of		
iterative scheme		
of Volterra		
integral equation		
of the second		
kind.		

# SW-1 Suggested Sessional Work (SW):

# a. Assignments:

- i. Analyze and define the concept of integral equation with their types and cases with example.
- ii. Volterra integral equation to find the eigen values and eigenfunctions
- iii. Find the application of iterative scheme to Volterra integral equation of the second kind



# b. Mini Project:

Oral presentation, Poster presentation, Power Point Presentation.

**c.** Other Activities (Specify): Quiz, Class Test.

### CO2-78MS302.2

Define and understand the basic concepts of integral transform method, laplacetransform , convolution integral. Application of Volterra with convolution type kernels.solution of the Cauchy type singular integral equation. And the hilbert kernel.

Item	AppXHrs
Cl	12
LI	0
SW	1
SL	1
Total	14

Session Outcomes	Laboratory Instruction	Class room Instruction	Self Learning
(SOs)	(LI)	(CI)	(SL)
SO2.1		Unit-2.0	SL.1
Define and		2.1.integral transform	Explore laplace
understand		method	transform and fourier
integral transform.		2.2. fourier transform	transform with their
SO2.2		2.3.laplace transform	relation .
Perform basic	-	2.4-convolution integral	SL.2
Convolution tofind		2.5. application of Volterra	Understand the concept
the application of		integral equation with	of Volterra integral
Volterra integral		convolution type kernels.	equation with
equation with		2.6.solution of the Cauchy	convolution type
kernels.		type singular integral	kernels.
SO2.3		equation.	SL.3
Understand the		2.7.the Hilbert kernel.	Apply Hilbert type and



# Curriculum & Syllabus of M.Sc. Mathematics program

concept of singular integral	2.8. convolution kernels.	type	Cauchy type to find the solution of singular
equation	2.9. solution of the H	Hilbert	integral equations.
SO2.4	type singular in	itegral	
Define and	equation.		
compute the	2.10. singular in	tegral	
Cauchy type and	equation.		
Hilbert type	2.11 solution of Cauchy	y type	
kernels.	and Hilbert type sintegral equation.	ngular	
SO2.5	2.12 Tutorial-1		
Understand the			
solution of Cauchy			
type and Hilbert			
type singular			
integral equation.			

## SW-2 Suggested Sessional Work (SW):

### a. Assignments:

- i. Write the integral transform with their types.
- ii. Write the Volterra integral equation with convolution type kernels.
- iii. Write a short note on Hilbert type and Cauchy type to find the solution of singular integral equations.
- iv. Describe the method singular integral equation and use in caychy type and hibert type kernels.

## b. Mini Project:

Oral presentation, Poster presentation, Power Point Presentation.

**c.** Other Activities (Specify):

Quiz, Class Test.



### CO3-78MS302.3

Define and compute, symmetric kernels, orthonormal system of functions. Fundamental properties of eigenvalues and eigen functions for symmetric kernels. Solution of integral equations with symmetric kernels.

Item	AppXHrs
Cl	12
LI	0
SW	1
SL	1
Total	14

Session Outcomes	<b>Laboratory Instruction</b>	Class room Instruction	Self Learning
(SOs)	(LI)	(CI)	(SL)
SO3.1		Unit-3.0	SL.1
Define and			Apply symmetric
compute		3.1. symmetric kernels	kernels and
Symmetric kernels		3.2. orthonormal system of	orthonormal system of
SO3.2		functions	functions.
Understand the	-	3.3. fundamental properties	SL.2
eigen values and		of eigenvalues	Apply the fundamental
eigen functions for		3.4. and eigen functions for	properties to find the
symmetric		symmetric kernels	eigen values and eigen
kernels. SO3.3		3.5. solution of integral	functions of integral
Apply and		equations with symmetric	equations
computesolution		kernels.	SL.3
of integral		3.6.eigenvalues and eigen	Solve the integral
equations with		functions	equation with
symmetric		3.7. system of functions	symmetric kernels.
kernels.		3.8properties of eigen	
SO3.4		values	
Understand		3.9. properties of eigen	
The properties of		functions	
eigen values and		3.10. integral equations with	
eigen functions		symmetric kernels	



# AKS University Faculty of Basic Science

# **Department of Mathematics**

# **Curriculum & Syllabus of M.Sc. Mathematics program**

SO3.5	3.11 Questions of symmetric
Identify the	kernels
integral equation	3.12 Tutorial-1
with symmetric	
kernels.	

### SW-2 Suggested Sessional Work (SW):

### a. Assignments:

- i. Write the symmetric kernels and orthonormal system of functions.
- ii. Explain the fundamental properties of eigen values and eigen functions.
- iii. Write the solution of integral equation with symmetric kernels.

### b. Mini Project:

Oral presentation, c. Other Activities (Specify): Quiz, Class Test.

### CO4-78MS302.4

Understand and definition of a boundary value problem for an ordinary equation of a second order and reduction to a fredholm integral equation of the second kind. Dirac delta function. Green function approach to reduce the boundary value problem of a self adjoint differential equation with homogenous boundary condition to integral equation form.

Tip protition to the arre			
Item	AppXHrs		
Cl	12		
LI	0		
SW	1		
SL	1		
Total	14		



# **AKS University**

# Faculty of Basic Science Department of Mathematics

# **Curriculum & Syllabus of M.Sc. Mathematics program**

Session Outcomes (SOs)	Laboratory Instruction (LI)	Class room Instruction (CI)	Self Learning (SL)
SO4.1 Understand the definition of boundary value problem. SO4.2 Analyze theboundary value problem for an ordinary equation of the second order.  SO4.3 Identify the dirac delta function with their properties. SO4.4 Identify green function approach to reduce boundary value problem of a self adjoint differential equations.  SO4.5 Recognize with homogenous boundary condition to		Unit-4.0  4.1.definition of boundary value problem for an ordinary equation of the second order.  4.2 and its reduction to a fredholm integral equations of the second kind.  4.3.dirac delta function  4.4. green functions  4.5 Tutorial-1  4.6.green function approach to reduce boundary value problem of a self adjoint differential equations.  4.7. with homogenous boundary condition to integral equations.  4.8.construction of green functions.  4.9.reduction of boundary value problem into integral equations.  4.10. properties of dirac delta functions.  4.11problem based on boundary value problem.  4.12 Tutorial-2	SL.1 Apply boundary value problem for an ordinary equation of the second kind. SL.2 Apply Boundary value problem to reduce in a fredholm integral equation of the second kind. SL.3 Analyze and interpret green functions to reduce boundary value problem of a self adjoint differential equations with homogenous boundary conditions to integral equations.
integral equations.			



### SW-2 Suggested Sessional Work (SW):

### a. Assignments:

- Explain green functions to reduce boundary value problem of a self adjoint differential equations with homogenous boundary conditions to integral equations.
- **b.** Other Activities (Specify): Quiz, Class Test.

### CO5-78MS302.5

Understand the integral representation formulae for the solution of the laplace and Poisson equations. Newtonian single layer and double layer potentials. Integral equation formulation of boundary value problem for laplace equations.

Item	AppXHrs
Cl	12
LI	0
SW	1
SL	1
Total	14

Session Outcomes	Laboratory Instruction	Class room Instruction	Self Learning
(SOs)	(LI)	(CI)	(SL)
SO4.1		Unit-5.0	SL.1
Understand			Apply integral
laplace equation		5.1.integral representation	representation formulas
and poisons		formulas for the laplace	for the laplace
equations.		equation.	equation. And poisons
SO4.2	-	5.2. integral representation	equations.
Understand single		formulas for the poisons	SL.2
and double layer		equation.	Use Newtonian single
of Newtonian		5.3. Newtonian single layer	and double layer
potential in		potential	potential in integral



# Curriculum & Syllabus of M.Sc. Mathematics program

integral equations.	5.4 Newtonian double layer	equations.
SO4.3	potential	SL.3
Understand the	5.5. integral equation	Apply integral equation
concept of	formulation of boundary	formulation of
formulation of	value problem for laplace	boundary value
boundary value	equation.	problem for laplace
problem for	5.6 laplace equation	equation.
laplace equation.	5.7. poisons equations	
SO4.4	5.8 problems on laplace	
Interpret poisons	equations	
equations.	5.9. problems on poisons	
	equations	
SO4.5	5.10. boundary value	
Understand	problem forlaplace	
boundary value	equation	
problem for	5.11boundary value	
laplace and	problem for poisons	
poisson equations.	equation.	
	5.12 Tutorial-1	

# SW-2 Suggested Sessional Work (SW):

# a. Assignments:

- i. Write the integral representation formulas for the laplace equation. And poisons equations.
- ii. Write integral equation formulation of boundary value problem for laplace equation

## b. Mini Project:

Power Point Presentation.

**c.** Other Activities (Specify): Quiz, Class Test.

**Brief of Hours suggested for the Course Outcome** 



# **Curriculum & Syllabus of M.Sc. Mathematics program**

Course Outcomes	Class Lecture (CI)	Sessional Work (SW)	Self Learning (SI)	Total hour (CI+SW+SI)
CO1-78MS302.1  Define and understand the concept of laplace transform and differential equation and their classification, definition of integral transform .fredholm and Volterra integral equation.	12	1	1	14
CO2-78MS302.2  Define and understand the basic concepts of integral transform method, laplacetransform, convolution integral. Application of Volterra with convolution type kernels.solution of the Cauchy type singular integral equation. And the hilbert kernel	12	1	1	14
CO3-78MS302.3  Define and compute, symmetric kernels, orthonormal system of functions. Fundamental properties of eigenvalues and eigen functions for symmetric kernels. Solution of integral equations with symmetric kernels	12	1	1	14
CO4-78MS302.4  Understand and definition of a boundary value problem for an ordinary equation of a second order and reduction to a fredholm integral equation of the second kind. Dirac delta function. Green function approach to reduce the boundary value problem of a self adjoint differential equation with homogenous boundary condition to integral equation form.	12	1	1	14



CO5-78MS302.5 Understand the integral representation formulae for the solution of the laplace and Poisson equations. Newtonian single layer and double layer potentials. Integral equation formulation of boundary value problem for laplace equations.	12	1	1	14
Total Hours	60	5	5	70

# **Suggestion for End Semester Assessment**

Suggested Specification Table (For ESA)

СО	Unit Titles	Marl	ks Distrib	Total Marks		
		R	U	Α		
CO-1		02	04	05		07
	Integral equation					
CO-2	Integral transform	03	07	04		14
CO-3	Symmetric kernels	02	06	02		10
CO-4	Boundary value problem and green functions	03	03	02		11
CO-5	Integral representation	03	02	02		08
Total		13	22	15		50

Legend: R: Remember, U: Understand, A: Apply

The end of semester assessment for Introduction to Portland cement will be held with written examination of 50 marks



# Curriculum & Syllabus of M.Sc. Mathematics program

**Note**. Detailed Assessment rubric need to be prepared by the course wise teachers for above tasks. Teachers can also design different tasks as per requirement, for end semester assessment.

## **Suggested Instructional/Implementation Strategies**

- 1. Improved Lecture
- 2. Tutorial
- 3. Presentation
- 4. Group Discussion
- 5. Online sources
- 6 .Seminar
- 7. Workshop

### **Suggested Learning Resources:**

a) Books:

S. N	Title	Author	Publisher	Edition & Year
0.				
1	Linear integral equation	R.P. kanwal	Academic press	New York , 1971
2	Integral equation and calculus of variation	Dr. jagbirsingh	Maharshi Dayanand university	2021

#### **Curriculum Development Team**

- 1. Dr.Sudha Agrawal, HOD, Department of Mathematics.
- 2. Dr. Ekta Shrivastava, Assistant Professor, Department of Mathematics.
- 3. Mr. Neelkanth Napit, Assistant Professor, Department of Mathematics.
- 4. Mrs. Vandana Soni, Assistant Professor, Department of Mathematics.
- 5. Mr.Radhakrishna Shukla, Assistant Professor, Department of Mathematics.
- 6. Mr.Ghanhyam sen, Assistant Professor, Department of Mathematics.
- 7. Ms. Pushpa Kushwaha, Assistant Professor, Department of Mathematics.
- 8. Ms. Arpana Tripathi, Assistant Professor, Department of Mathematics.

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# **Cos, POs and PSOs Mapping**

**Course Title: M.Sc. Mathematics** 

Course Code: 78MS302

**Course Title: Integral Equation** 

Course				•												
		1			ı	П	1	1	Г	ı	1	1				T
Course	PO1	PO 2	P O	PO4	PO5	PO6	PO7	PO8	PO9	PO10	PO11	PO12	PSO 1	PS O	PSO 3	PSO 4
Outcome	Adv ance d Mat hem atica I Kno wled ge	Pro ble m- sol vin g Skil ls	Re se ar ch A bil iti es	Qua ntita tive Anal ysis	Teachi ng and Acade mia	Theo retic al Und ersta ndin g	Comm unicati on Skills	Operat ions Resear ch	Appl icati on in Indu stry	Engine ering and Techno logy	Gove rnme nt and Publi c Sect or	Cons ultin g	Understa nd the mathema tical concepts and applicati ons in the field of algebra	Ha ndl e th e ad va nc ed tec hni qu es	Dev elop nece ssar y skills a nd expe rtise in the field of rese arch	Creates Mathem atical Models
CO1- 78MS302 Define and understand the concept of laplace transform and differential equation and their classification, definition of integral transform .fredholm and Volterra integral equation.	2	3	1	2	1	2	1	1	1	1	1	1	2	2	1	
CO1-78MS302.2 Define and understand the	2	3	1	1	1	1	1	1	1	1	1	1	1	<u>2</u>	<u>2</u>	
basic concepts																



# **Curriculum & Syllabus of M.Sc. Mathematics program**

of integral																
transform																
method,																
laplacetransfor																
m , convolution																
integral.																
Application of																
Volterra with																
convolution																
type																
kernels.solution																
of the Cauchy																
type singular																
integral																
equation. And																
the hilbert																
kernel																
CO1-78MS302.3	3	3	1	2	1	1	3	2	2	1	2	2	1	<u>2</u>	<u>3</u>	
Define and													_		_	
compute,																
symmetric																
kernels,																
orthonormal																
system of																
functions.																
Fundamental																
properties of																
eigenvalues and																
eigen functions																
for symmetric																
kernels. Solution																
of integral																
equations with																
1																
symmetric kernels.																
CO1-	2	3	1	2	3	2	3	1	1	1	1	2	2	1	1	
78MS302.4		3	1	~	3	4	٥	1	1			2	2	<u>1</u>	<u>1</u>	
Understand and																
definition of a																
definition of a	<u> </u>					l			]							



# **Curriculum & Syllabus of M.Sc. Mathematics program**

boundary value	
problem for an	
ordinary	
equation of a	
second order	
and reduction to	
a fredholm	
integral	
equation of the	
second kind.	
Dirac delta	
function. Green	
function	
approach to	
reduce the line line line line line line line lin	
boundary value	
problem of a	
self adjoint	
differential	
equation with	
homogenous	
boundary	
condition to	
integral	
equation form.	
CO1-78MS302.5 3 2 3 1 2 1 2 3 1 1 1 1 <u>1</u> <u>1</u>	1
Understand the Understand the	
integral	
representation	
formulae for the	
solution of the	
laplace and	
Poisson	
equations.	
Newtonian	
single layer and	
double layer	
potentials.	
Integral	



# Curriculum & Syllabus of M.Sc. Mathematics program

_	1	1							
equation									
equation formulation of									
boundary value									
problem for laplace equations.									
laplace									
equations.									

Legend: 1 – Low, 2 – Medium, 3 – High



# **Course Curriculum Map:**

POs & PSOs No.	COs No.& Titles	SOs No.	Laboratory Instruction(L	Classroom Instruction (CI)	Self Learning (SL)
NO.			I)		(3L)
PO 1,2,3,4,5,6	<b>CO1-78MS302.1</b> 78MS302	SO1.1	,	Unit-1.0	SL1.1
7,8,9,10,11,12	Define and understand the	SO1.2		Approximation1.1,1.2,1.3,1.4,	SL1.2
PSO 1,2, 3, 4	concept of laplace transform	SO1.3		1.5,1.6,1.7,1.8,1.9,1.10,1.11,1.	
	and differential equation and	SO1.4		12,1.13,1.14,	
	their classification, definition				
	of integral transform .fredholm and Volterra				
	integral equation.				
PO 1,2,3,4,5,6	CO1-78MS302.2 Define and	SO2.1		Unit-2 System of linear	SL2.1
7,8,9,10,11,12	understand the basic	SO2.2		equations :2.1, 2.2, 2.3,	322.1
PSO 1,2, 3, 4	concepts of integral	SO2.3		2.4,2.5,2.6,2.7,2.8,2.9,2.10,2.1	
	transform method,	So2.4		1,2.12,2.13,2.14,2.15.	
	laplacetransform ,				
	convolution integral.				
	Application of Volterra with				
	convolution type				
	kernels.solution of the				
	Cauchy type singular integral equation. And the hilbert				
	kernel.				
PO 1,2,3,4,5,6	CO3-78MS302.3 Define and	SO3.1		Unit-3 Iteratives method	SL3.1
7,8,9,10,11,12	compute, symmetric kernels,	SO3.2		Offic-3 iteratives method	323.1
PSO 1,2, 3, 4	orthonormal system of	SO3.3		3.1, 3.2, 3.3, 3.4, 3.5,3.6,3.7	
	functions. Fundamental				
	properties of eigenvalues				
	and eigen functions for				
	symmetric kernels. Solution				
	of integral equations with				
20122156	symmetric kernels.	6044			61.4.4
PO 1,2,3,4,5,6	CO4-78MS302.4 Understand	SO4.1 SO4.2		Unit-4 Eigen value problem	SL4.1
7,8,9,10,11,12 PSO 1,2, 3, 4	and definition of a boundary value problem for an	SO4.2 SO4.3		41 42 42 44 45 46 47	
1 30 1,2, 3, 4	ordinary equation of a	SO4.3		4.1, 4.2, 4.3, 4.4, 4.5, 4.6, 4.7, 4.8,4.9,4.10,4.11,4.12	
	second order and reduction	JO 1T		+.O,+.J,4.1U,4.11,4.12	



# AKS University

# Faculty of Basic Science Department of Mathematics

# **Curriculum & Syllabus of M.Sc. Mathematics program**

	to a fredholm integral equation of the second kind. Dirac delta function. Green function approach to reduce the boundary value problem of a self adjoint differential equation with homogenous boundary condition to integral equation form.			
PO 1,2,3,4,5,6	CO5-78MS302.5	SO5.1	Unit-5Numerical Integration	SL.5.1
7,8,9,10,11,12	Understand the integral	SO5.2	5.1, 5.2, 5.3, 5.4, 5.5, 5.6	
PSO 1,2, 3, 4	representation formulae for	SO5.3	,5.7,5.8,5.9,5.10,5.11,5.12	
	the solution of the laplace	SO5.4		
	and Poisson equations.			
	Newtonian single layer and			
	double layer potentials.			
	Integral equation			
	formulation of boundary			
	value problem for laplace			
	equations.			



#### Semester-III

Course Code: 78MS303

Course Title : Advanced Numerical Techniques

Pre-requisite: Students should have basic knowledge of and

deep understanding of the theory of the

advanced numerical techniques.

Rationale: The program aims to develop advanced problem-

solving and analytical skills and prepares students for careers in academia, research, industry, or other sectors that require advanced

mathematical expertise.

**CO1-78MS303.1** Understand the importance of Uniform approximation by polynomials, Errors and their computations.

CO2-78MS303.2 Determine the Systems of Linear Equations

CO3-78MS303.3 Demonstrate an understanding of the theory of Iteratives method

CO4-78MS303.4 Define and recognize the Eigen value problem

**CO5-78MS303.5** Students will create the concept of a Numerical Integrationand methodbased on Interpolation

### **Scheme of Studies:**

Board of	Course	Course Title	Scheme of studies (Hours/Week)							
Study	Code	Title	CI	LI	sw	SL	Total Study Hours (CI+LI+SW+SL)	ts (C)		
Program Core (PCC)	78MS303	Advance d Numeric al Techniqu es	4[3+1]	0	1	1	6	4		

### Legend:

**CI:** Classroom Instruction (Includes different instructional strategies i.e. Lecture (L) and Tutorial (T) and others),



**LI:** Laboratory Instruction (Includes Practical performances in laboratory workshop, field or other locations using different instructional strategies)

**SW:** Sessional Work (includes assignment, seminar, mini project etc.),

SL: Self Learning,

C:Credits.

**Note:** SW & SL has to be planned and performed under the continuous guidance and feedback of teacher to ensure outcome of Learning.

#### **Scheme of Assessment:**

#### Theory

Board of	Couse	Course Title	Scheme of	Assessme	nt ( Marks	)				
Study	Code					End Semester Assessm ent (ESA)	Total Marks (PRA+ ESA)			
			Class/Ho me Assignme nt 5 number 3 marks each ( CA)	Class Test 2 (2 best out of 3) 10 marks each (CT)	Seminar one ( SA)	Class Activit y any one (CAT)	Class Attend ance (AT)	Total Marks (CA+CT+ SA +CAT+A T)		
PCC	78MS303	Advanced Numerical Techniques	15	20	5	5	5	50	50	100

#### **Course-Curriculum Detailing:**

This course syllabus illustrates the expected learning achievements, both at the course and session levels, which students are anticipated to accomplish through various modes of instruction including Classroom Instruction (CI), Laboratory Instruction (LI), Sessional Work (SW), and Self Learning (SL). As the course progresses, students should showcase their mastery of Session Outcomes (SOs), culminating in the overall achievement of Course Outcomes (COs) upon the course's conclusion.



**CO1-78MS303.1** Understand the importance of Uniform approximation by polynomials, Errors and their computations.

Item	AppXHrs
Cl	14
LI	0
SW	1
SL	1
Total	16

Session Outcomes (SOs)	Laboratory Instruction (LI)	Class room Instruction (CI)	Self Learning (SL)
SO1.1 Understand the concept of Uniform approximation SO1.2 Understand the Principles of floating point,  SO1.3 Understand the Errors and their computations. SO1.4 Understand the data fitting		Unit-1.0  1.1 Uniform approximation by polynomials  1.2 least squares approximation  1.3 Rational approximation  1.4 Weighted least square approximation  1.5 Approximation of function-chebyshev polynomials  1.6 Tutorial 1  1.7 Principles of floating point  1.8 Errors and their computations.  1.9 Error in series approximation  1.10 Tutorial 2  1.11 Multiple linear least square  1.12 Curve fitting by a polynomial  1.13 data fitting  1.14 Fitting a straight line	SL1.1 Orthogonal polynomial



# SW-1 Suggested Sessional Work (SW):

### a. Assignments:

- (i) Obtain a linear polynomial approximation to the function  $f(x) = x^3$  on the interval [0,1] using the least square approximation with W(x)=1
- (ii) Certain experimental values of x and given below (0,-1) (2,5) (5,12) (7,20) in the straight lines  $y=a_0+a_1x$  is fitted to the above data find the approximate value of  $a_0$  and  $a_1$ .
- (iii)find the approximate value of  $a_0$  and  $a_0$  and  $a_1$  so that the function  $z=a_0+a_1x+a_2y$  is fitted to the data given below (0,0,2) (1,1,4) (2,3,3) (4,2,16) (6,8,6)
- (iv)Define Errors and their computations

## b. Mini Project:

Oral presentation, Poster presentation, Power Point Presentation.

**c.** Other Activities (Specify): Quiz, Class Test.

## CO2-78MS303.2 Determine the Systems of Linear Equations

Item	AppXHrs
Cl	15
LI	0
SW	1
SL	1
Total	17

Session Outcomes	Laboratory Instruction	Class room Instruction	Self Learning
(SOs)	(LI)	(CI)	(SL)
SO2.1		Unit2.0	SL.1 computational
Understand the		2.1 Introduction of	procedure for LU
concept Systems of		Systems of Linear	Decomposition method
Linear Equations		Equations	
SO2.2 Understand the		2.2 Bisection method	
Partial Pivoting		2.3 Newton Raphson	
And Complete Pivoting		method	
SO2.3 Understand the		2.4 Regula falsi	



Factorization method,	method
	2.5 Secant method
SO2.4 Understand the 3	2.6 Tutorial 1
Gauss-elimination	2.7 Factorization
	method
	2.8 Gauss-elimination
	method
	2.9 Gauss -Jordan
	method
	2.10 Tutorial 2
	2.11 Partial Pivoting
	2.12 Necessity for
	pivoting
	2.13 Complete
	Pivoting
	2.14 Tutorial 3
	2.15 Residual error
	correction method

## SW-2 Suggested Sessional Work (SW):

#### a. Assignments:

(I) Solve the System of Equation by Factorization Method

$$3x + 2y + 7z = 4$$
  
 $2x + 3y + z = 5$   
 $3x + 4y + z = 7$ 

(ii) Solve the system of Equation by Gauss Elimination method with partial pivoting

$$10x - y + 2z = 4$$
  
  $x + 10y - z = 3$   
  $2x + 3y + 20z = 7$ 

(iii) Solve the System of Equation by Triangularization Method

$$x + 5y + z = 14$$
  
 $2x + y + 3z = 13$   
 $3x + y + 4z = 17$ 

# b. Mini Project:

Oral presentation, Poster presentation, Power Point Presentation.

c. Other Activities (Specify): Quiz, Class Test.



O3-78MS303.3 Demonstrate an understanding of the theory of Iteratives method

## **Approximate Hours**

• •	
Item	AppXHrs
Cl	7
LI	0
SW	1
SL	1
Total	9

Session Outcomes (SOs)	Laboratory Instruction (LI)	Class room Instruction (CI)	Self Learning (SL)
SO3.1 Understand the theJacobi method		Unit-3.0	SL.1 Solve the
SO3.2 Understand the conjugate gradient		3.1 Introduction of Iterative methods	many problems system of
methods		3.2 Tutorial 1	Equation by Gauss
SO3.3 Understand the		3.3 Jacobi method	Seidel method in
Gauss-Seidel methods with convergence		3.4 Gauss-Seidel methods	third iterations
analysis		3.5 Gauss-Seidel methods with convergence analysis	
		3.6 Tutorial 2	
		3.7 conjugate gradient methods.	

# SW-3 Suggested Sessional Work (SW):

# a. Assignments:

1. Solve the Equation by Jacobi Method

$$6x + 3y + 12z = 35$$
  
 $8x - 3y + 2z = 20$   
 $4x + 11y - z = 33$ 



# 2. Solve the Equation by Jacobi Method

$$20x + y - 2z = 17$$
  
 $3x + 20y - z = -18$   
 $2x - 3y + 20z = 25$ 

3. Solve the system of Equation by Gauss Seidel method

$$x + 2y + z = 3$$
  
 $2x + 3y + 3z = 10$   
 $3x - y + 2z = 13$ 

4. Solve the system of Equation by Gauss Seidel method

$$10x + y + z = 12$$
  
2x + 10y + z = 13  
x + y + 5z = 7

5. Solve the system of Equation by Gauss Seidel method

$$8x - 3y + 2z = 20$$
$$4x + 11y - z = 33$$
$$6x + 3y + 12z = 35$$

### b. Mini Project:

Oral presentation, Poster presentation, Power Point Presentation.

**c.** Other Activities (Specify):

Quiz, Class Test.

CO4-78MS303.4 Define and recognize the Eigen value problem

• •	
Item	AppXHrs
Cl	12
LI	0
SW	1
SL	1
Total	14

Session Outcomes (SOs)	Laboratory Instruction (LI)	Class room Instruction (CI)	Self Learning (SL)



SO4.1 Understand	Unit-4.0	SL.1
Eigen value and Eigen		Some problems on
vectors	4.1 Eigen value	Eigen value and eigen vectors
SO4.2 Understand the	4.2 Eigen vectors of	
Householder's method	matrix .	
SO4.3Understand Eigen values of a symmetric	4.3 Tutorial 1	
tridiagonal matrix,	4.4 Householder's method	
SO4.4 understand and		
problems solving on Interpolation	4.5 Eigen values of a symmetric tridiagonal matrix	
	4.6 Tutorial 2	
	4.7 Singular value decomposition	
	4.8 Interpolation - Introduction	
	4.9 review of Lagrange interpolation techniques.	
	4.10 Tutorial 3	
	4.11 Error in Lagrange 's interpolation techniques.	
	4.12 Tutorial 4	

# SW-4 Suggested Sessional Work (SW):

# a. Assignments:

(i) Determine the Eigen values and Eigen vectors of the following matrix:



$$\begin{bmatrix} 5 & 0 & 1 \\ 0 & -2 & 0 \\ 1 & 0 & 5 \end{bmatrix}$$

(ii) Evaluate  $\log_{10} 301$  by using Lagrange's interpolation formula given

log <sub>10</sub> 300	log <sub>10</sub> 304	log <sub>10</sub> 305	log <sub>10</sub> 307
2.4771	2.4829	2.4843	2.4871

(iii) Obtain the singular value decomposition of the following matrix:

$$\begin{bmatrix} 1 & 2 \\ 1 & 1 \\ 1 & 3 \end{bmatrix}$$

(iv) Evaluate  $\log_{10}656\,$  by using Lagrange's interpolation formula given

log <sub>10</sub> 654	log <sub>10</sub> 658	log <sub>10</sub> 659	log <sub>10</sub> 661
2.8156	2.8182	2.8189	2.8202

## b. Mini Project:

Oral presentation, Poster presentation, Power Point Presentation.

c. Other Activities (Specify):

Quiz, Class Test.

**CO5-78MS303.5** Students will create the concept of a Numerical Integration and method based on Interpolation.

ipproximate mours			
Item	Appx Hrs		
Cl	12		
LI	0		
SW	1		
SL	1		
Total	14		



# AKS University Faculty of Basic Science Department of Mathematics

# Curriculum & Syllabus of M.Sc. Mathematics program

Session Outcomes (SOs)	Laboratory Instruction (LI)	Class room Instruction (CI)	Self Learning (SL)
SO5.1 Understand the concept Method based on Interpolation SO5.2 Understand the Gauss quadrature method SO5.3 Understand Initial Value Problems for Ordinary Differential Equations SO5.4 Understand Predictor and Corrector scheme		Unit-5.0 5.1Method based on Integration 5.2 Simpson's rule 5.3 Trapezoidal rule 5.4 Tutorial 1 5.5 Newton's- Cotes method 5.6 Gauss quadrature method. 5.7 Tutorial 2 5.8 Initial Value Problems for Ordinary Differential Equations 5.9Runge-Kutta method, 5.10 Predictor 5.11 Corrector scheme 5.12 Stability and Convergence analysis.	SL.1 Problems on Euler method

# SW-3 Suggested Sessional Work (SW):

# a. Assignments

(i) Use Runge - Kutta method to obtain

y when 
$$x=1.1$$
 given that  $1.2$  when  $x=1$  and y satisfies the equations  $\frac{dy}{dx}=3x+y^2$ 

(ii) Use Runge - Kutta method to find

y when x = 1.2 in step of 0.1 given that satisfies the equations

$$\frac{dy}{dx} = x^2 + y^2$$
, y(1) = 1.5



- (iii) Show that the sum of cotes number is unity
- (iv) Find  $\int_0^1 \frac{1}{1+x^2} dx$  by using Trapezoidal rule where the interval is divided into 6 equal parts.
- (v) Apply Milne' Simpson method to find a solution of the differential equation  $\frac{dy}{dx} = 1+x$  y² with initial condition y(0)=1 for x=0.4, 0.5 given that

X	0.1	0.2	0.3
Υ	1.101	1.223	1.355

#### b. Mini Project:

Oral presentation, Poster presentation, Power Point Presentation.

c. Other Activities (Specify):

Quiz, Class Test.

#### **Brief of Hours suggested for the Course Outcome**

Course Outcomes	Class Lecture (CI)	Sessional Work (SW)	Self Learning (SI)	Total hour (Cl+SW+SI)
CO1-78MS303.1 Understand the importance of Uniform approximation by polynomials, Errors and their computations.	14	1	1	16
CO2-78MS303.2 Determine the Systems of Linear Equations	15	1	1	17
CO3-78MS303.3 Demonstrate an understanding of the theory of Iteratives method	7	1	1	10
CO4-78MS303.4 Define and recognize the Eigen value problem	12	1	1	14



CO5-78MS303.5 Students will create the concept of a Numerical Integrationand method based on Interpolation	12	1	1	14
Total Hours	60	5	5	70

#### **Suggestion for End Semester Assessment**

Suggested Specification Table (For ESA)

СО	Unit Titles	Mark	s Distribu	ution		Total Marks
		R	U	Α		
CO-1	Understand the importance of Uniform approximation by polynomials, Errors and their computations.	03	01	01		05
CO-2	Determine the Systems of Linear Equations	02	06	02		10
CO-3	Demonstrate an understanding of the theory of Iteratives method	03	07	05		15
CO-4	Define and recognize the Eigen value problem	-	10	05		15
CO-5	Students will create the concept of a Numerical Integrationand method based on Integration	03	02		-	05
Total	•	11	26		13	50

Legend: R: Remember, U: Understand, A: Apply



The end of semester assessment for Introduction to Portland cement will be held with written examination of 50 marks

**Note**. Detailed Assessment rubric need to be prepared by the course wise teachers for above tasks. Teachers can also design different tasks as per requirement, for end semester assessment.

#### **Suggested Instructional/Implementation Strategies**

- 1. Improved Lecture
- 2. Tutorial
- 3. Presentation
- 4. Group Discussion
- 5. Online sources
- 6 .Seminar
- 7. Workshop

#### **Suggested Learning Resources:**

a) Books:

S. N o.	Title	Author	Publisher	Edition & Year
1	Numerical Analysis	S.S.Sastry	Prentice hall India.	2015
2	Numerical methods fore scientific and engineering computations	M.K.Jain,S.R.K. Iyenger.		
3	Numerical Analysis	G.Shankar Rao	New age international publishers ,new- Hydrabad.	2006



#### **Curriculum Development Team**

- 1. Dr.Sudha Agrawal, HOD, Department of Mathematics.
- 2. Dr.Ekta Shrivastava, Assistant Professor, Department of Mathematics.
- 3. Mr. Neelkanth Napit, Assistant Professor, Department of Mathematics.
- 4. Mrs. Vandana Soni, Assistant Professor, Department of Mathematics.
- 5. Mr.Radhakrishna Shukla, Assistant Professor, Department of Mathematics.
- 6. Mr.Ghanhyam sen, Assistant Professor, Department of Mathematics.
- 7. Ms. Pushpa Kushwaha, Assistant Professor, Department of Mathematics.
- 8. Ms. Arpana Tripathi, Assistant Professor, Department of Mathematics.

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### **Cos, POs and PSOs Mapping**

**Course Title: M.Sc. Mathematics** 

Course Code: 78MS303

**Course Title: Advanced Numerical Techniques** 

Co	urse i	itie: /	Advanced	ı Num	ericai i e	cnniq	ues						ı			
Course	PO1	PO 2	PO3	PO4	PO5	PO6	P07	PO8	PO9	PO10	PO11	PO12	PSO 1	PS O 2	PSO 3	PSO 4
Outcome	Adva nced Mat hem atica I Kno wled ge	Pr ob le m- sol vin g Ski Ils	Research Abilities	Qua ntita tive Anal ysis	Teachi ng and Acade mia	Theo retic al Und ersta ndin g	Comm unicati on Skills	Operat ions Resear ch	Appl icati on in Indu stry	Engine ering and Techno logy	Gove rnme nt and Publi c Sect or	Cons ultin g	Understa nd the mathema tical concepts and applicati ons in the field of algebra	Ha ndl e th e ad va nc ed tec hni qu es	Dev elop nece ssar y skills a nd expe rtise in the field of rese arch	Creates Mathem atical Models
rand the importance of Uniform approximat ion by polynomial s, Errors and their computations.	2	3	1	2	1	2	1	1	1	1	1	1	2	2	1	
CO1- 78MS303. 2 Determine the Systems of Linear Equations	2	3	1	1	1	1	1	1	1	1	1	1	1	<u>2</u>	2	
CO1- 78MS30	3	3	1	2	1	1	3	2	2	1	2	2	1	<u>2</u>	<u>3</u>	



# AKS University Faculty of Basic Science Department of Mathematics

### Curriculum & Syllabus of M.Sc. Mathematics program

3.3 Demons trate an underst anding of the theory of Iterative s method																
CO1- 78MS30 3.4 Define and recogniz e the Eigen value problem	2	3	1	2	3	2	3	1	1	1	1	2	2	1	1	
CO1- 78MS30 3.5Stud ents will create the concept of a Numeric al Integrati onand method based on Interpol ation	3	2	3	1	2	1	2	3	1	1	1	1	1	1	1	

Legend: 1 – Low, 2 – Medium, 3 – High



### **Course Curriculum Map:**

POs & PSOs No.	COs No.& Titles	SOs No.	Laborato Instructi LI)	•	Classroom Instruction (CI)	Self Learning (SL)
PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2, 3, 4	CO1-78MS303.1 Understand the importance of Uniform approximation by polynomials, Errors and their computations.	SO1.1 SO1.2 SO1.3 SO1.4		App 1.5	it-1.0 proximation1.1,1.2,1.3,1.4, ,1.6,1.7,1.8,1.9,1.10,1.11,1 ,1.13,1.14,	SL1.1 SL1.2
PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2, 3, 4	CO2-78MS303.2 Determine the Systems of Linear Equations	SO2.1 SO2.2 SO2.3 So2.4		equ 2.4	it-2 System of linear uations :2.1, 2.2, 2.3, ,2.5,2.6,2.7,2.8,2.9,2.10,2. 2.12,2.13,2.14,2.15.	SL2.1
PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2, 3, 4	CO3-78MS303.3  Demonstrate an understanding of the theory of Iteratives method	SO3.1 SO3.2 SO3.3			it-3 Iteratives method , 3.2, 3.3, 3.4, 3.5,3.6,3.7	SL3.1
PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2, 3, 4	CO4-78MS303.4  Define and recognize the Eigen value problem	SO4.1 SO4.2 SO4.3 SO4.4		4.1	it-4 Eigen value iblem , 4.2, 4.3, 4.4, 4.5, 4.6, 4.7, ,4.9,4.10,4.11,4.12	SL4.1
PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2, 3, 4	CO5-78MS303.5 Students will create the concept of a Numerical Integration	SO5.1 SO5.2 SO5.3 SO5.4		5.1	it-5Numerical Integration , 5.2, 5.3, 5.4, 5.5, 5.6 7,5.8,5.9,5.10,5.11,5.12	SL.5.1

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#### Semester-III

Course Code: 78MS304
Course Title : Special function

Perquisite: Students should have basic knowledge of

complex numbers

Rationale: The program aims to develop advanced problem-

solving and analytical skills and prepares students for careers in academia, research, industry, or other sectors that require advanced

mathematical expertise.

#### **Course Outcome:**

**CO1-78MS304.1** understand the property of special function like Gaus hypergeometric legendra function with their integral representations.

**CO2-78MS304.2**. Understand the concept of bessel's function hermit function etc with its properties like recurrence relation orthogonal properties generating function etc.

**CO3-78MS304.3**. Understand how special function is useful in differential equation.

CO4-78MS304.4 explain the application and the usefulness of these special function

**CO5-78MS304.5** classify and explain the function different types of differential equation.

### Curriculum & Syllabus of M.Sc. Mathematics program Scheme of Studies:

Board of Study	Course Code	Course Title	Scheme of s	Scheme of studies (Hours/Week)						
Study		Title	Cl	LI	SW	SL	Total Study Hours (CI+LI+SW+SL)	Credit s (C)		
Program Core (PCC)	78MS304	Special function	4[3+1]	0	1	1	6	4		



#### Legend:

**CI:** Classroom Instruction (Includes different instructional strategies i.e. Lecture (L) and Tutorial (T) and others),

**LI:** Laboratory Instruction (Includes Practical performances in laboratory workshop, field or other locations using different instructional strategies)

**SW:** Sessional Work (includes assignment, seminar, mini project etc.),

SL: Self Learning,

C:Credits.

**Note:** SW & SL has to be planned and performed under the continuous guidance and feedback of teacher to ensure outcome of Learning.

#### **Scheme of Assessment:**

#### Theory

Board of	Couse Code	Course Title	Sc	Scheme of Assessment ( Marks )						
Study			Progressiv	Progressive Assessment ( PRA )						Total Marks (PRA+ ESA)
			Class/Home Assignment 5 number 3 marks each ( CA)	Class Test 2 (2 best out of 3) 10 marks each (CT)	Seminar one ( SA)	Class Activity any one (CAT)	Class Attendanc e (AT)	Total Marks (CA+CT+SA +CAT+AT)		
PCC	78MS304	Special function	15	20	5	5	5	50	50	100

#### **Course-Curriculum Detailing:**

This course syllabus illustrates the expected learning achievements, both at the course and session levels, which students are anticipated to accomplish through various modes of instruction including Classroom Instruction (CI), Laboratory Instruction (LI), Sessional Work (SW), and Self Learning (SL). As the course progresses, students should showcase their mastery of Session Outcomes (SOs), culminating in the overall achievement of Course Outcomes (COs) upon the course's conclusion.

CO1-78MS304.1 understand the properties of special function like Gauss hyper geometric legendra function with their integral representations.

Item	AppX Hrs
Cl	10
LI	0



SW	1
SL	1
Total	12

Session Outcomes	Laboratory Instruction	Class room Instruction	Self Learning
(SOs)	(LI)	(CI)	(SL)
SO1.1		Unit-1.0 Gamma function	SL.1
Understand the		and Beta function:	Understand the
concept of			complex numbers.
Gamma functions.		1.1 Introduction of Gamma	
		function.	<b>SL.2</b> knowledge of the
SO1.2	-		gamma function and
Understand the		1.2 The definition of Gamma	beta function.
relationships		functions.	SL.3
between beta and		1.3 Eulerian Definition.	Properties of Gamma
gamma functions.			functions
SO1.3		1.4 Euler's Products.	
Understand the			
concept of Beta			
function.		1.5 Evaluation of Gamma	
So1.4		functions.	
Understand the		1.6 Beta function:	
multiplication		1.7 Introduction	
formula		1.8 definition of Beta	
So1.5		function.	
Understand the			
concept of		1.9 Multiplication formulas.	
function.		1.10 Related functions.	

#### SW-1 Suggested Sessional Work (SW):

#### a. Assignment:

i. Evaluation of Gamma and beta terms..

- ii. Gauss 's multiplication formula.
- iii. State and prove Beta function.
- iv. Application of Gamma functions.

#### b. Mini Project:

Oral presentation, Poster presentation, Power Point Presentation.



**c.** Other Activities (Specify): Quiz, Class Test.

**CO2-78MS304.2**. Understand the concept of bessel's function hermit function etc with its properties like recurrence relation orthogonal properties generating function etc.

#### **Approximate Hours**

Item	AppX Hrs
Cl	10
LI	0
SW	1
SL	1
Total	12

Session Outcomes (SOs)	Laboratory Instruction (LI)	Class room Instruction (CI)	Self Learning (SL)
SO2.1 Understand the concept of bessel's functions.		Unit-2.0 Bessel Functions.:  2.1 Introduction.	SL.1 Evaluation Bessel's differential equations.
SO2.2 Learn about the		<ul><li>2.2 Definition of Bessel functions.</li><li>2.3 Definition of Jn(x)</li></ul>	SL.2 Knowledge of the Bessel's functions.
concept of Recurrence relation.		<ul><li>2.4 Generating function of Jn(x).</li><li>2.5 Alternative forms of generating functions.</li></ul>	SL.3 Knowledge of some properties of bessel's
Understand the concept of Jn(x)		<ul><li>2.6 Bessel's differential equations.</li><li>2.7 Recurrence relation</li></ul>	functions.
SO2.4 Understand the Uses of Bessel's functions.		for Jn(x).  2.8 Bessel 's Integral.	
SO2.5 Understand the concept of recurrence relation with example.		2.9 tutorial 1 2.10 Application of bessel's functions.	

#### **SW-2 Suggested Sessional Work (SW):**

#### a. Assignments:

- i. Definition and Example of Bessel's functions.
- ii. Define Alternative forms of generating functions.
- iii. The Recurrence relation for Jn(x).
- iv. Bessel's differential equations.



#### b. Mini Project:

Oral presentation, Poster presentation, Power Point Presentation.

**c.** Other Activities (Specify):

Quiz, Class Test.

#### **CO3-78MS304.3**. Understand how special function is useful in differential equations.

#### **Approximate Hours**

Item	AppX Hrs
Cl	11
LI	0
SW	1
SL	1
Total	13

Session Outcomes (SOs)  Class room Instruction (CI)  SO3.1 Understand the principle of legendre polynomials.  SO3.2 Understand the Laplaces first integral form.  SO3.3 the concept of orthogonal properties.  SO3.4 Generating function for legendre polynomials  3.5 tutorial 1  3.6 Rodriguez formula.  3.7 Hypergeometric forms of Pn(x)  3.8 some other generating functions  3.9 Laplaces first integral form,  3.10 Legendre 's differential equations.				10tai 13
SO3.1 Understand the principle of legendre polynomials.  SO3.2 Understand the Laplaces first integral form.  SO3.3 the concept of orthogonal properties.  SO3.4 Generating function for legendre polynomials 3.5 tutorial 1 3.6 Rodriguez formula. 3.7 Hypergeometric forms of Pn(x) 3.8 some other generating functions 3.9 Laplaces first integral form,  3.10 Legendre 's differential equations.		Instruction		
3 11 Orthogonal properties	SO3.1 Understand the principle of legendre polynomials.  SO3.2 Understand the Laplaces first integral form.  SO3.3 the concept of	(LI)	Unit-3.0 Legendre Polynomials. 3.1 Introduction. 3.2 Recurrence relation. 3.3 the concept of legendre polynomials 3.4 Generating function for legendre polynomials 3.5 tutorial 1 3.6 Rodriguez formula. 3.7 Hypergeometric forms of Pn(x) 3.8 some other generating functions 3.9 Laplaces first integral form,  3.10 Legendre 's differential	<ul> <li>Knowledge of the generating functions for legendre polynomials.</li> <li>Understand an application of legendre</li> </ul>

#### SW-3 Suggested Sessional Work (SW):

#### a. Assignment:

- ii. Application of legendre polynomials.
- iii. Evaluation of legendre differential equations.
- iv. State and prove Rodrigues formula.



V. Orthogonal properties.

#### b. Mini Project:

Oral presentation, Poster presentation, Power Point Presentation.

c. Other Activities (Specify):

Quiz, Class Test.

#### CO4-78MS304.4 explain the application and the usefulness of these special function.

Item	AppX Hrs
Cl	10
LI	0
SW	1
SL	1
Total	12

Session Outcomes (SOs)	Laboratory Instruction (LI)	Class room Instruction (CI)	Self Learning (SL)
SO4.1 Understand the concept of harmite 's polynomials. SO4.2 understand the generating functions. SO4.3 Understand the importance of harmite 's polynomials.		Unit -4 Hermite's Polynomials: 4.1 Introduction 4.2 Recurrence relation. 4.3 Evaluation of Rodrigues Formula. 4.3 Generating function. 4.4 Bat'sman generating functions. 4.5 tutorial 1 4.6 Hermite's differential equations. 4.7 Evaluation of orthogonal properties. 4.8 some properties of harmite 's function. 4.9 Expansion of polynomials. 4.10 more generating functions.	st.1 knowledge of the harmite 's polynomials.  St.2 Expansion of polynomials, Recurrence relation.



#### SW-4 Suggested Sessional Work (SW):

#### a. Assignments:

- i. Evaluation of Rodrigues formula for generating functions.
- ii. Application of Hermite 's polynomials.
- iii. The Expansion of polynomials.
- iv. Calculation of Hermite 's differential equations.
- V. More generating functions.

#### b. Mini Project:

Oral presentation, Poster presentation, Power Point Presentation.

c. Other Activities (Specify):

Quiz, Class Test.

**CO5-78MS304.5** The classify and explain the function different types of differential equations.

• •	
Item	AppX Hrs
Cl	9
LI	0
SW	1
SL	1
Total	11

Session Outcomes (SOs)	Laboratory Instruction (LI)	Class room Instruction (CI)	Self Learning (SL)



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SO5.2 Generaliged Laguerre polynomials.  SO5.3 Orthogonal properties.	<ul><li>5.1 Introduction .</li><li>5.2 simple Laguerre polynomials:</li><li>5.3 Introduction the Laguerre polynomials Ln(x)</li></ul>	Recurrence relation and generating functions.  • knowledge of the expansion of polynomials.
	5.4 Definition and Example of Laguerre polynomials. 5.5 Generating function. 5.6 Recurrence relation. 5.7. Laguerre difficult equations. 5.8 Rodrigues Formula.,Orthogonal properties. 5.9 Generaliged Laguerre polynomials: Rodrigues formula,Orthogonal properties, expansion of polynomials.	

**Brief of Hours suggested for the Course Outcome** 



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Course Outcomes	Class Lecture (CI)	Sessional Work (SW)	Self Learning (SI)	Total hour (CI+SW+SI)
CO1-78MS304.1 understand the properties of special function like Gauss hyper geometrc legendra function with their integral representations.	10	1	1	12
CO2-78MS304.2. Understand the concept of bessel's function hermit function etc with its properties like recurrence relation orthogonal properties generating function etc.	10	1	1	12
CO3-78MS304.3. Understand how special function is useful in differential equations.	11	1	1	13
CO4-78MS304.4 Explain the application and the usefulness of these special function.	10	1	1	12
CO5-78MS304.5 The classify and explain the function different types of differential equations.	9	1	1	11
Total Hours	50	5	5	60

### o Suggestion for End Semester Assessment

Suggested Specification Table For( ESA

со	Unit Titles	Marks	Total Marks		
		R	U	Α	
CO-1	UNIT-1: Gamma function and beta function.	03	01	01	05
CO-2.	UNIT 2: Bessel's functions & Bessel's differential equations.	02	05	03	10



CO-3	Unit-3: Legendre Polynomials.	03	06	06	15
CO-4	Unit- 4: Harmite's polynomials. & harmite differential equations.	-	10	05	15
CO-5	Unit 5: Laguerre polynomials. & Generaliged Laguerr polynomials.	03	02	-	05
Total		11	26	13	50

Legend: R: Remember, U: Understand, A: Apply

The end of semester assessment for Introduction to Portland cement will be held with written examination of 50 marks

**Note**. Detailed Assessment rubric need to be prepared by the course wise teachers for above tasks. Teachers can also design different tasks as per requirement, for end semester assessment.

#### **Suggested Instructional/Implementation Strategies**

- 1. Improved Lecture
- 2. Tutorial
- 3. Presentation
- 4. Group Discussion
- 5. Online sources
- 6 .Seminar
- 7. Workshop



### **Suggested Learning Resources:**

### a) Books:

S. No.	Title	Author	Publisher	Edition
1	Special Functions & Their Applications	N. N. Lebedev	New Edition	1972
2.	Differential Equation with Special function	J.N. Sharma & R.K. Gupta	Krishna Prakashan Mandir	-
3.	Integral Calculus	Shanti Narayan and Dr. P.K. Mittal	S. Chand & Company Pvt.Ltd. Ram Nagar New Delhi	-
4.	Differential Equations	Shepley L.Ross	Second Edition , john Willy & sons, New York	Second Edition 1974

#### b) Reference Books:

S. N o.	Title	Author	Publisher	Edition
1	Special function	Rainville E.D	The Macmillan ,New York,	2nd edition, 1971
2	Special function and their applications	Lebdev	Prentice hall Englewood cliffs	New Jersey USA 1995
3	Special function with applications	Saran N. Sharma and trivedi	Pragti prakashan	Edition, 1986



#### **Curriculum Development Team:**

- 1. Dr. Sudha Agrawal, HOD, Department of Mathematics.
- 2. Dr.Ekta Shrivastava, Assistant Professor, Department of Mathematics.
- 3. Mr. Neelkanth Napit, Assistant Professor, Department of Mathematics.
- 4. Mrs. Vandana Soni, Assistant Professor, Department of Mathematics.
- 5. Mr.Radhakrishna Shukla, Assistant Professor, Department of Mathematics.
- 6. Mr. Ghanhyam sen, Assistant Professor, Department of Mathematics.
- 7. Ms. Pushpa Kushwaha, Assistant Professor, Department of Mathematics.
- 8. Ms. Arpana Tripathi, Assistant Professor, Department of Mathematics.

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### **Cos, POs and PSOs Mapping**

**Course Title: M.Sc. Mathematics** 

Course Code: 78MS304 Course Title: Special Function

Course Outcome	PO1	PO2	PO3	PO4	PO5	PO6	P O 7	PO8	PO9	PO1 0	PO11	PO 12	PSO 1	PSO 2	PSO 3	PSO 4
	Adv ance d Mat hem atica I Kno wled ge	Prob lem- solvi ng Skills	Rese arch Abilit ies	Quant itative Analy sis	Teachin g and Academi a	Theor etical Under standi ng	C o m m u ni c at io n S ki lls	Opera tions Resea rch	Appl icati on in Indu stry	Engi neer ing and Tech nolo gy	Gover nmen t and Public Sector	Co nsu Itin g	Unders tand the mathe matical concep ts and applica tions in the field of algebra	Handl e the advan ced techni ques	Develo p necess ary skills and experti se in the field of researc h	Creat es Math emati cal Mod els
CO1-78MS304.1 understand the properties of special function like Gauss hyper geometrc legendra function with their integral representations	2	1	2	2	1	2	3	2	1	1	1	1	<u>1</u>	2	1	2
CO2-78MS304.2. Understand the concept of bessel's function hermit function etc with its properties like recurrence relation orthogonal properties generating function etc	2	1	3	2	1	2	1	1	1	2	1	1	3	2	1	1



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CO378MS304.3. Understand how special function is useful in differential equations.	2	1	2	2	1	3	2	1	2	2	1	1	2	2	1	1
CO4-78MS304.4 explain the application and the usefulness of these special function	2	1	2	2	2	1	2	2	3	2	2	2	2	1	1	1
CO5-78MS304.5 The classify and explain the function different types of differential equations.	2	2	3	2	2	2	2	2	2	1	1	3	1	1	2	1



### **Course Curriculum Map:**

POs & PSOs No.	COs No.& Titles	SOs No.	Laboratory Instruction( LI)	Classroom Instruction (CI)	Self Learning (SL)
PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2, 3, 4	CO1-78MS304.1 understand the properties of special function like Gauss hyper geometrc legendra function with their integral representations	S01.1 S01.2 S01.3 S01.4 S01.5		Unit-1.0 Gamma function and beta function.  1.1,1.2,1.3,1.4,1.5,1.6,1.7,1.8,1.9, 1.10	SL1.1 SL1.2
PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2, 3, 4	CO278MS304.2. Understand the concept of Bessel's function hermit function etc with its properties like recurrence relation orthogonal properties generating function etc	SO1.1 SO1.2 SO1.3 SO1.4 SO1.5		Unit-2 Bessel's functions & Bessel's Differential equations.  2.1, 2.2, 2.3, 2.4, 2.5, 2.6, 2.7, 2.8,2.9,2.10	SL2.1 SL2.2
PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2, 3, 4	CO3-78MS304.3 Understand how special function is useful in differential equations.	SO1.1 SO1.2 SO1.3 SO1.4 SO1.5		Unit-3 Legendre Polynomials.  3.1, 3.2, 3.3, 3.4, 3.5, 3.6, 3.7, 3.8,3.9,3.10,3.11	SL3.1 SL3.2
PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2, 3, 4	CO4-78MS304.4 explain the application and the usefulness of these special function	SO1.1 SO1.2 SO1.3 SO1.4 SO1.5		Unit-4 Harmite 's polynomials. &harmite differential equations 4.1, 4.2, 4.3, 4.4, 4.5, 4.6, 4.7, 4.8,4.9,4.10.	SL4.1 SL4.2
PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2, 3, 4	CO5-78MS304.5 The classify and explain the function different types of differential equations.	SO1.1 SO1.2 SO1.3 SO1.4 SO1.5		Unit-5 Laguerre polynomials.& Generaliged Laguerre polynomials. 5.1, 5.2, 5.3, 5.4, 5 .5, 5.6, 5.7, 5.8,5.9,	SL5.1 SL5.2

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#### Semester-III

Course Code: 78MS305

**Course Title:** Fundamentals of Computers & Programming

Pre-requisite: Student should have basic knowledge of elementary

mathematics.

Rationale: The rationale behind discrete mathematics is grounded in

its practical applications to computer science and related

fields.

#### **Course Outcome:**

**78MS305.1**: Understand and apply the programming concepts of C++ which is important for mathematical investigation and problem solving.

**78MS305.2:** Use mathematical libraries for computational objectives.

**78MS305.3:** Represent the outputs of programs visually in terms of well formatted text and plots.

**78MS305.4**:Apply the knowledgeto solve complex problems and contribute meaningfully to the development of various software and systems.

**78MS305.5**:UnderstandMicrosoft Office is favored in professional settings due to its extensive features, compatibility, and support, while OpenOffice might be more suitable for personal use or organizations looking for a free and basic office suite.

#### SchemeofStudies:

Board	Course				Schem	e of stud	ies(Hours/Week)	TotalCredits
ofStud	Code		Cl	LI	SW	SL	Total	(C)
У		CourseTitle					StudyHours(CI+LI +SW+SL)	
OEC		Fundamentals of Computers & Programming	3	1	2	1	7	4

#### Legend

**CI:** ClassroomInstruction(Includes differentinstructional strategies i.e. Lecture (L) and Tutorial (T) and others),

**LI**:LaboratoryInstruction(IncludesPracticalperformancesinlaboratoryworkshop, field or other locations using different instructional strategies)

**SW:** Sessional Work(includesassignment, seminar, miniprojectetc.),

**SL:**SelfLearning, **C:**Credits.

Note: SW & SL has to be planned and performed under the continuous guidance and

feedback ofteachertoensureoutcomeofLearning.



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### Scheme of Assessment Theory

					;	Scheme	of Assessm	ent (Marks)		
				Pro	ogressiv	e Assess	sment ( PRA	A)	End Semester Assessme	Total
Board of Study	Co use Co de	Course Title	Class/ Home Assig nmen t 5	Class Test 2 (2 best out of	Semi nar one	Class Activ ity any	Class Attendan ce	Total Marks	nt	Marks
			numb er 3 marks each ( CA)	3) 10 marks each (CT)	(SA)	one (CAT	(AT)	( CA+CT+SA+CAT +AT)	(ESA)	(PRA+ ESA)
OEC	78 MS 30 5	Fundament als of Computers & Programmi ng	15	20	5	5	5	50	50	100

#### **Course-CurriculumDetailing:**

This course syllabus illustrates the expected learning achievements, both at the course and session levels, which students are anticipated to accomplish through various modes of instruction including Classroom Instruction (CI), Laboratory Instruction (LI), Sessional Work (SW), and Self Learning (SL). As the course progresses, students should showcase their mastery of Session Outcomes (SOs), culminating in the overall achievement of Course Outcomes (COs) upon the course's conclusion.

78MS305.1: Understand and apply the programming concepts of C++ which is important for mathematical investigation and problem solving.

Approximate mours							
Item	AppX Hrs						
Cl	10						
LI	02						
SW	2						
SL	1						
Total	15						



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SessionOutco	LaboratoryInstruc		ClassroomInstruction		SelfLearni
mes	tion		(CI)		ng
(SOs)	(LI)				(SL)
SO1.1	1.1 Working with	Unit-1	.Computer Fundamental:	1.	Learn about
Understandin	DOS commands	1.1 (	Characteristics of Computer		Computer
g	1.2 Introduction of	1	Fundamental,		Software,
Types and	programming	1.2	Types and components of		Operating
components	language	(	Computer Fundamental		System.
for computer		1.3 I	Input Devices, Output	2.	Google
fundamental		ı	Devices,3D Printing		Bard,
SO1.2 Explain		1.4	Storage Devices. Smart Devices,		Microsoft
computer		DOS	Commands. Introduction to		Bing, ML.
Software		Prog	gramming Languages & Software		
<b>SO1.</b> 3 discuss		1.5	Computer Software,		
Email, chat		1.6	Operating System		
boat and wed		1.7	Mobile App Software,		
Blogs.		1.8	Social Media Software: Instant		
<b>SO1.4</b> define Virtual		Mes	saging, Email, Chat Boat, and		
Reality (VR), and		Web	Blogs.		
Augmented Reality		Intro	oduction to cutting-edge		
(AR).		tech	nologies:		
		1.9	Digital Trust, Blockchain,		
			Internet of Things (IoT), 5G,		
		(	Cyber Security,		
		1.10	Cloud Computing, Quantum		
		(	Computing. Introduction to AI,		
		(	Chat GPT, Google Bard,		
		ı	Microsoft Bing, ML, Virtual		
			Reality (VR), and Augmented		
			Reality (AR)		

#### SW-1 SuggestedSessionalWork(SW):

#### a. Assignments:-

- (1) Characteristics, types and componentsComputer Fundamental.
- (2) Digital Trust, Blockchain, Internet of Things (IoT), 5G, Cyber Security, Cloud Computing, Quantum Computing. Introduction to AI, ChatGPT.
- (3) Computer Software, Operating System, Mobile App Software, Social Media Software.

#### b. MiniProject:

Oral presentation, Poster presentation, Power Point Presentation.

#### **c.**Other Activities (Specify):

Quiz, Class Test.



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#### 78MS305.2: Use mathematical libraries for computational objectives.

•	
Item	AppXHrs
Cl	10
LI	02
SW	2
SL	2
Total	16

SessionOutcomes (SOs)	Laboratory Instruction (LI)	ClassroomInstruction (CI)	SelfLearni ng (SL)
SO2.1 define Programming Language.  SO2.2 discussHistory of C and Types of C Variables.  SO2.3 To learn about Data types.  SO2.4 Explainarithmetic operators and relational operators.	2.1 Programming in C. 2.2 Operators in C.	Unit-2 :Getting Started with C:  2.1 Programming Language, Types, Translators, Flowcharts, what is C,  2.2 History of C, The C Character set  2.3 Types of C, Constants  2.4 Types of C Variables, C keywords  2.5 Identifiers, and literals, Data types  2.6 Basic input & output function – printf and scanf, Math library  2.7 arithmetic operators  2.8 Relational operators  2.9 Assignment operators, logical operators, increment and decrement operators  2.10 conditional operator.	1. Types of C, Constants and Types of C Variables. 2. Basic input & output function.



#### SW-2 SuggestedSessionalWork(SW):

#### a. Assignments:-

- (1) Programming Language, Types, Translators, Flowcharts.
- (2) All topics of c.
- (3) What is operator and types of operator.

#### b. MiniProject:

Oral presentation, Poster presentation, Power Point Presentation.

**c.** Other Activities (Specify):

Quiz, Class Test.

## 78MS305.3: Represent the outputs of programs visually in terms of well formatted text and plots.

Item	AppXHrs		
Cl	10		
LI	02		
SW	2		
SL	2		
Total	16		

SessionOutcomes (SOs)	LaboratoryInstruction (LI)	ClassroomInstruction (CI)	SelfLearnin g (SL)
SO3.1To UnderstandControl instructions. SO3.2To learn Loops control structure. SO3.3 Explain array and character array.	3.1 Proramming in c for control statements. 3.2 Programming Array in C.	Unit-3 Control Structure:  3.1 Control instructions, if, if-else, if-else if, nested if  3.2 Loops control structure: while loop, for loop  3.3 Loops control structure: do—while loop, odd loop, nested loop  3.4 Break, continue, case-control structure  3.5 goto, exit statement switch statement.  Array:  3.6 Array  3.7 Array initialization  3.8 2D array  3.9 Initialization of 1D and 2D array	1. Control instructions and Loops control structure. 2. What is Array.



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	3.10	Character Array.	

#### SW-3 SuggestedSessionalWork(SW):

- a. Assignments:-
- (1) Control instructions and Loops control structure.
- (2) Break, continue, case-control structure.
- (3) What is array and types of array.
- b. MiniProject:

Oral presentation, Poster presentation, Power Point Presentation.

**c.**Other Activities (Specify):

Quiz, Class Test.

78MS305.4:Apply the knowledgeto solve complex problems and contribute meaningfully to the development of various software and systems.

Item	AppXHrs
Cl	10
LI	02
SW	2
SL	2
Total	16

SessionOutcomes (SOs)	LaboratoryInstructi on (LI)	ClassroomInstruction (CI)	SelfLearning (SL)
SO4.1	4.1. Programming	Unit-4 Function:	1. What is
To UnderstandNeed	function in C.	4.1 Need of function	function
of function.	4.2 Passing parameter	4.2 Declaring a function	and types
<b>SO4.2</b> To learn types of function.	in the function.	<ul><li>4.3 Defining</li><li>4.4 Calling function</li><li>4.5 Types of function</li></ul>	of function.  2. Pointers  and Array  of Pointers.
SO4.3 To understand Advance C Concepts.		4.6 Passing parameter in the function.  Advance C Concepts: 4.7 Pointers	3. String and String Functions



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SO4.4 Explain Array of	4.8 Array of Pointers
Pointers.	4.9 Call by value
	4.10 all by reference, Structure
	and union,String,String
	Functions

#### SW-4 SuggestedSessionalWork(SW):

#### a. Assignments:

- (1) declaring a function, defining, calling function, types of function, passing parameter in the function
- (2) Pointers, Array of Pointers, Call by value, Call by reference, structure and union, String, String Functions.

#### b. MiniProject:

Oral presentation, Poster presentation, Power Point Presentation.

c.Other Activities (Specify):

NΔ

78MS305.5:Understand Microsoft Office is favored in professional settings due to its extensive features, compatibility, and support, while OpenOffice might be more suitable for personal use or organizations looking for a free and basic office suite.

Item	AppXHrs
Cl	10
LI	02
SW	2
SL	2
Total	16

SessionOutcomes	LaboratoryInstruction	ClassroomInstruction	SelfLearning
(SOs)	(LI)	(CI)	(SL)



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<b>SO5.1</b> To	5.1. Documents		1. Introduction
understandIntroductio	editing in MS-word.	Unit 5 (1)	and FeaturesMS
n and FeaturesMS	5.2 Creating table in	MS Office Vs Open	Office.
Office.	MS-EXCEL.	Office:	2. Computer
<b>SO5.2</b> To learn about	WIS EXCEE.	5.1 Introduction and	Networks and
Open Office.		Features	Google
SO5.3Explain Google		(Comparison).	Workspace.
Workspace.		5.2MS Word:	
<b>SO5.4</b> define Computer		Introduction,	
Networks.		Features, and	
		Applications,	
		Applications,	
		5.3Menus &	
		Commands,	
		5.4 Toolbars & Buttons	
		5.5MS Excel:-	
		Introduction, working	
		with MS Excel, Use of	
		Formulas and	
		Functions.	
		<b>5</b> .6 MS PowerPoint:-	
		Introduction, working	
		with MS PowerPoint,	
		Creating a	
		Presentation.	
		5.7 Computer	
		Networks:-LAN and	
		WAN and Internet,	
		Bluetooth, Wi-Fi, Li-Fi,	
		Client-Server	
		architecture.	
		5.8Cloud-Based Services:	
		5.9Google Workspace:	
		DOCS, Sheets, Slides,	
		Forms, Calendar,	
		5.10 Chat, Meet,	
		Contacts, Maps,Jam	
		board; YouTube	

#### SW-5 SuggestedSessionalWork(SW):

- a. Assignments:-
- (1) Introduction and Features MS Office.
- (2) LAN and WAN and Internet, Bluetooth, Wi-Fi, Li-Fi, Client-Server architecture.
- (3) Explain Google Workspace.



b. MiniProject:NA

c. OtherActivities(Specify):NA

#### **Brief of Hours suggested for the Course Outcome**

Course Outcomes	Class Lecture (CI)	Laborato ryInstruc tion (LI)	Sessional Work (SW)	Self Learning (SI)	Total hour (CI+SW+S I)
78MS305.1: Understand and apply the programming concepts of C++ which is important for mathematical investigation and problem solving.	10	2	2	2	16
78MS305.2: Use mathematical libraries for computational objectives.	10	2	2	2	16
78MS305.3: Represent the outputs of programs visually in terms of well formatted text and plots.	10	2	2	2	16
78MS305.4:Apply the knowledgeto solve complex problems and contribute meaningfully to the development of various software and systems.	10	2	2	2	16
78MS305.5:Understand Microsoft Office is favored in professional settings due to its extensive features, compatibility, and support, while OpenOffice might be more suitable for personal use or organizations looking for a free and basic office suite.	10	2	2	2	16
Total Hours	50	10	10	10	80



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#### **Suggestion for End Semester Assessment**

#### **Suggested Specification Table(ForESA)**

СО	UnitTitles	MarksDistribution		ibution	Total Marks	
		R	U	Α		
CO-1	Computer Fundamental	03	01	01	05	
CO-2	Getting Started withC,Operator	02	02	01	05	
CO-3	Control Structure , Array	03	07	05	15	
CO-4	Function and Advance C Concepts	04	06	05	15	
CO-5	MS Office Vs Open Office	03	04	03	10	
	Total	15	20	15	50	

Legend: R:Remember, U:Understand, A:Apply

TheendofsemesterassessmentforIntroduction to Portland cement willbeheld with written examination of 50 marks

**Note**. Detailed Assessment rubric need to be prepared by the course wiseteachers for above tasks. Teachers can also design different tasks as per requirement, for endsemesterassessment

#### SuggestedInstructional/ImplementationStrategies:

- 1. ImprovedLecture
- 2. Tutorial
- 3. CaseMethod
- 4. GroupDiscussion
- 5. RolePlay
- 6. Visittocementplant
- 7. Demonstration
- 8. ICTBasedTeachingLearning(VideoDemonstra tion/TutorialsCBT,Blog,Facebook, Twitter,WhatsApp,Mobile,Onlinesources)
- 9. Brainstorming



#### Suggested Learning Resources:

#### A. Books:

S.	Title	Author	Publisher	Edition
No.				&Year
1	"Computer	Pradeep K. Sinha and	ВРВ	Fourth Edition
	Fundamentals"	Priti Sinha	Publications	
2	"Let Us C" BPB	YashvantKanetkar	BPB Publications,	Seventh Edition
	Publications, 2007			2007
3	Learning Computer	Maidasani,	Laxmi Publications	2005
	Fundamentals, MS	D.		
	Office and Internet &			
	Web Tech.			

#### **Curriculum Development Team**

- 1. Dr.Sudha Agrawal, HOD, Department of Mathematics.
- 2. Dr.Ekta Shrivastava, Assistant Professor, Department of Mathematics.
- 3. Mr. Neelkanth Napit, Assistant Professor, Department of Mathematics.
- 4. Mrs. Vandana Soni, Assistant Professor, Department of Mathematics.
- 5. Mr.Radhakrishna Shukla, Assistant Professor, Department of Mathematics.
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- 8. Ms. ArpanaTripathi, Assistant Professor, Department of Mathematics.

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### CO, PO and PSO Mapping

Course: M.Sc. Mathematics CourseCode: 78MS305

**Course Title: Fundamentals of Computers & Programming** 

					Pro	gram(	Outco						ProgramSpecific Outcome						
Course Outcom	PO1	PO 2	PO 3	PO 4	PO 5	PO 6	PO 7	PO8	PO 9	PO1 0	PO 11	P O 1 2	PSO1	PSO2	PSO3	PSO4			
es	Advanced Mathematical Knowledge	m-	Researc h Abilities	ative	g and	tical	Commun ication Skills	ons	ion in	Enginee ring and Technol ogy	Governm ent and Public Sector	Consulti ng	Understand the mathematic al concepts and applications in the field of algebra	the advanc ed techniq		hematica Models			
CO.1: 78MS305.1 Computer Fundamen tal	1	1	2	2	3	2	3	2	2	1	3	2	2	3	3	1			
CO.2: <b>78MS305</b> .2 .2 .3 .2 .2 .2 .2 .2 .2 .2 .2 .2 .2 .2 .2 .2	1	1	2	2	1	2	3	2	1	1	2	2	2	2	2	1			
CO.3: 78MS305 .3 Control Structure, Array	2	2	1	1	1	2	2	2	1	2	1	2	1	1	2	2			
CO.4: <b>78MS305</b> .4 Function and Advance C Concepts	3	2	2	2	3	2	3	2	2	1	2	3	3	3	3	2			



### **Faculty of Basic Science**

### **Department of Mathematics**

### Curriculum & Syllabus of M.Sc. Mathematics program

CO.5 : <b>78MS305</b>	3	2	1	1	1	3	3	3	1	1	2	2	3	3	1	3
.5 MS Office Vs Open Office																

Legend:1-Low,2-Medium,3-High

### **Course Curriculum Map:**

POs&PSOsNo.	Cos	SOsN	Labora	Classroom	SelfLearnin
	No.&Titles	0.	toryIn	Instruction(CI)	g(SL)
			structi		
			on		
			(LI)		
PO1,2,3,4,5,6	CO.1: <b>78MS305.1</b> Computer Fundamental	SO1.1, SO1,		Unit-1.	
7,8,9,10,11,12		SO1.3,SO1.4		1.1.1,1.1.2,1.1.3,1.1.4,	
PSO1,2,3,4,5		·		1.2.1,1.2.2,1.2.3,1.1.4,	
				1.3.1, 1.3.2,1.3.3 1.1.4	
PO1,2,3,4,5,6	CO.2: 78MS305.2	SO2.1,		Unit-2	
	Getting Started withC, Operator	SO2.2,			
7,8,9,10,11,12		SO2.3,SO2.4			
				2.1.1,2.1.2,2.1.3,2.1.4 ,2.1.5,2.1.6,2.1.7	
PSO1,2,3,4,5				2.2.1,2.2.2.,2.2.3,2.2.	
1301,2,3,4,3				4,2.2.5	
				4,2.2.3	
		600			
PO1,2,3,4,5,6	CO.3 : <b>78MS305</b> .3	SO3		Unit-3:	
7,8,9,10,11,12	Control Structure , Array	.1S 03.			
		2			
PSO1,2,3,4,5		SO3.3		3.1.1,3.1.2,3.1.3,3.1.4, 3.1.5,3.1.6,3.1.7	



#### 3.2.1,3.2.2,3.2.3,3.2.4 ,3.2.5 CO.4: **78MS305**.4 Unit-4: PO1,2,3,4,5,6 SO4.1 Function and Advance C Concepts 7,8,9,10,11,12 SO4.2 4.1.1,4.1.2,4.1.3,4.1.4, SO4.3 4.1.5 PSO1,2,3,4,5 **SO4.4** 4.2.1,4.2.2,4.2.3,4.2.4, 4.2.5,4.2.6,4.2.7 CO.5 : **78MS305**.5 Unit5: PO1,2,3,4,5,6 SO5.1 5.1,5.2,5.3,5.4,5.5,5. 7,8,9,10,11,12 SO5.2 MS Office Vs Open Office 6,5.7,5.8,5.9,5.10,5.1 SO5.3

PSO1,2,3,4,5

\*\*\*\*\*\*\*\*\*\*

SO5.4

1,5.12



#### Semester-III

Course Code: 78MS306-A
Course Title: Scientific writing
Pre -requisite: Graduate Student Standing

Rationale: This course will guide graduate students through

the process of scientific writing. Students will select a project of interest for which there is existing data. With this data, we will cover developing sound objectives, writing a scientific manuscript including basic analyses, developing figures, and then presenting scientific results at a

conference

Course Outcome: CO1-78MS306-A .1 Do review of literature

#### CO2-78MS306-A.2

Write review paper thesis write and Generate report

#### CO3-78MS306-A.3

Aware to format of publications

#### CO4-78MS306-A .4

Understand concept of impact factor, H index

#### CO5-78MS306-A.5

Understand implementation of Softwares to writing research papers and plotting the graphs.



Board of	Course Code	Course Title	Scheme of studies (Hours/Week)					Tota
Study		Title	Cl	LI	sw	SL	Total Study Hours (CI+LI+SW+SL)	ts (C)
RC	78MS306-A	Scientific Writing	2	1	1	1	(2+1+1+1)	3

#### Legend:

**CI:** Classroom Instruction (Includes different instructional strategies i.e. Lecture (L) and Tutorial (T) and others),

**LI:** Laboratory Instruction (Includes Practical performances in laboratory workshop, field or other locations using different instructional strategies)

SW: Sessional Work (includes assignment, seminar, mini project etc.),

SL: Self Learning,

C:Credits.

**Note:** SW & SL has to be planned and performed under the continuous guidance and feedback of teacher to ensure outcome of Learning.

#### **Scheme of Assessment:**

#### Theory

Board of	Couse	Course	Scheme of Assessment ( Marks )		
Study	Code	Title			
,			Progressive Assessment ( PRA )	End	Total
					Marks
				Semester	
				Assessm	(PRA+
				ent	
					ESA)
				(ESA)	



			Class/H	Class	Seminar	Class	Class	Total		
			ome	Test 2	one	Activit	Attend	Marks		
			Assign ment 5 numbe r 3 marks each (CA)	(2 best out of 3) 10 marks each (CT)	(SA)	y any one (CAT)	ance (AT)	(CA+CT+ SA +CAT+A T)		
RC	78MS30 6-A	Scientific Writing	15	20	5	5	5	50	50	100

#### **Course-Curriculum Detailing:**

This course syllabus illustrates the expected learning achievements, both at the course and session levels, which students are anticipated to accomplish through various modes of instruction including Classroom Instruction (CI), Laboratory Instruction (LI), Sessional Work (SW), and Self Learning (SL). As the course progresses, students should showcase their mastery of Session Outcomes (SOs), culminating in the overall achievement of Course Outcomes (COs) upon the course's conclusion.

### **CO1- 78MS306-A** .1 Do review of literature.

Item	AppX Hrs
Cl	9
LI	0
SW	1
SL	1
Total	11



Session Outcomes	Laboratory	Class room Instruction	Self Learning
(SOs)	Instruction (LI)	(CI)	(SL)
SO1.1 Understanding the Structure and Purpose of Research Writing SO 1.2 Developing Skills for Effective Research Writing SO 1.3 Mastering the Concepts of Bibliography and References	-	Unit-1.  1.1 Basic Concept of research journal  1.2 concept of Thesis Writing and Report Generation  1.3 Writing Research Abstract  1.4 Introduction, Review of Literature  1.5 discuss Result and Conclusion  1.6 discuss how to read a paper  1.7 concept of writing  1.8 Concepts of Bibliography  1.9 References	Practice by reviewing examples of well-written research papers or theses available in digital libraries or academic databases to see how experienced researchers organize and present their work.  SL.2  Write a brief introduction that sets the context for a chosen research topic, clearly stating the research problem and objectives.

#### SW-1 Suggested Sessional Work (SW):

- a. Assignment:
- i. Read a research papers and make a summary.
- b. Mini Project:

Oral presentation, Poster presentation, Power Point Presentation.

#### CO2-78MS306-A .2

Write review paper thesis write and Generate report.

Item	AppX Hrs
Cl	9



LI	0
SW	1
SL	1
Total	11

Session Outcomes	Laborator	Class room Instruction	Self Learning
(SOs)	y	(CI)	(SL)
	Instructio	,	
	n		
	(LI)		
SO 2.1		Unit:-2	SL 1
Understanding the Significance and		2.1 Significance of Report Writing	Gain a solid understanding of the different types of
Structure of Report		2.2 Steps of Report Writing	reports and publication
Writing SO 2.2		2.3 Types of Research Reports	formats, enabling you to choose the appropriate
Mastering Presentation		<b>2.4</b> Types of Research Reports	format for your work.
and Publication Formats		2.5 Formats of Publication in	SL2 Research and study
SO 2.3 Developing		Research Journal/ Book/ Conference	various types of research
Skills for Effective Oral		Etc	reports, such as technical
and Poster		EIC	reports, case studies, and
Presentations:		<b>2.6</b> Concept of Impact Factor, H-	white papers.
		Index	
		2.7 Seminar Presentation: Power Poir	
		For Oral And Poster Presentation	5
		Reference.	
		2.8 Oral Presentations	
		2.9 Poster Presentations	

#### SW-2 Suggested Sessional Work (SW):

#### a. Assignments:

i. study various types of research and make a report.

#### b. Mini Project:

Oral presentation, Power Point Presentation.



#### CO3-78MS306-A.3

Aware to format of publications

#### **Approximate Hours**

1 1	
Item	AppX Hrs
Cl	9
LI	0
SW	1
SL	1
Total	11

			Otal	11	
Session Outcomes (SOs)	Laboratory Instruction (LI)	Class room Instruction (CI)	Self (SL)	f Learning	
SO3.1 Understanding the Significance and Steps of Report Writing SO3.2 Familiarity with Types of Research Reports and Presentation Methods: SO3.3 Mastering Advanced Tools and Techniques for Research Communication:		3.1 Typesetting Mathematical Text V LATEX 3.2 Sample Document, Type Style 3.3 understand Environments, Lists, Centering, Tables, 3.4 study Vertical And Horizontal spa 3.5 learn Equation Environments, Fo 3.6 Hats And Underlining, Braces 3.7 Arrays And Matrices 3.8 learn Customized Commands 3.9 Theorem—Like Environments Math Styles	With and LaT  SL 2  Pra LaT by v type acing main onts, exp		s us

#### SW-3 Suggested Sessional Work (SW):

#### a Assignment:

**1** Access online tutorials and documentation for LaTeX to learn the basics of typesetting mathematical text.

#### b. Mini Project:

Oral presentation, Power Point Presentation.



#### CO4-78MS306-A .4

Understand concept of impact factor, H index

#### **Approximate Hours**

Item	AppX Hrs
Cl	9
LI	0
SW	1
SL	1
Total	11

#### **SW-4 Suggested Sessional Work (SW):**

#### a Assignment:

1 Practice creating simple documents.

#### b. Mini Project:

Oral presentation, Power Point Presentation.

Session Outcomes (SOs)	Laboratory Instruction (LI)	Class room Instruction (CI)	Self Learning (SL)
SO 4.1 Comprehension		UNIT 4	<b>SL 1</b> Study the
of Document Structure		<b>4.1</b> understand Document Classes and the	official documentation
and Tools.		Overall Structure	and online
SO4.2 Skill		<b>4.2</b> learn how to give Titles for Documents	tutorials for LaTeX or other
Development in		<b>4.3</b> learn Sectioning Commands	document
Document Creation		<b>4.4</b> Inputting Files, Inputting Pictures,	preparation SL2
SO4.3 Proficiency in		Making a Bibliography	Create sample
Data Analysis Tools		4.5 Making an Index	documents with various structures
		4.6 Packages.	(articles, reports,
		4.7 Slides	books) using LaTeX or another
		4.8Computer usage for collecting/analyzing	system,
		data-simulation	
		using Fortran/C/Mathematica/Matlab/	
		MathCAD/IBM-SPSS.	
		4.9under247nd how to insert Pictures and	
		graph in paper	



#### CO5-78MS306-A.5

Understand implementation of Softwares to writing research papers and plotting the graphs.

Item	AppX Hrs
Cl	9
LI	0
SW	1
SL	1
Total	11

Session Outcomes	Laboratory	Class room Instruction (CI)	Self Learning
(SOs)	Instruction		(SL)
(305)	(LI)	(CI)	(3L)



SO 5.1 Introduction to MATLAB Environment and Basic Operations SO 5.2 Participants will develop skills in creating, saving, and executing script and function files, as well as handling data operations SO5.3 Working with Arrays and Plotting Data	<ul> <li>Unit-5</li> <li>5.1 learn Basics of MATLAB, Window</li> <li>5.2 understand Input-Output, File types, Working with arrays of numbers.</li> <li>5.3 Creating and Printing Simple Plots,</li> <li>5.4 Creating, Saving and Executing a Script file</li> <li>5.5 Creating and Executing a function file.</li> <li>5.6 Indexing, Matrix manipulation,</li> <li>Creating Vectors, Matrix and Array operations</li> <li>5.7 Saving and Loading Data, Plotting Simple Graphs.</li> </ul>	SL 1 Explore MATLAB Documentation and Tutorials SL2 Write and execute simple script and function files to automate calculations and tasks, starting with basic examples
	5.7 Saving and Loading Data, Plotting	

#### SW-3 Suggested Sessional Work (SW):

#### a Assignment:

1 Create and customize simple plots using sample data, and practice saving and exporting these plots for use in reports and presentations.

#### b. Mini Project:

Oral presentation, Power Point Presentation

#### **Brief of Hours suggested for the Course Outcome**



Course Outcomes	Class Lecture (CI)	Sessional Work (SW)	Self Learning (SI)	Total hour (CI+SW+SI)
CO1-78MS306-A .1 Do review of literature.	9	1	1	11
CO2-78MS306-A .2 Write review paper thesis write and Generate report.	9	1	1	11
CO3-78MS306-A .3 Aware to format of publications	9	1	1	11
CO4-78MS306-A .4 Understand concept of impact factor, H index	9	1	1	11
CO5-78MS306-A.5 Understand implementation of Softwares to writing research papers and plotting the graphs.	9	1	1	11
Total Hours	45	5	5	65

#### **Suggestion for End Semester Assessment**

Suggested Specification Table For(ESA)

СО	Unit Titles	Marks Dis	Total Marks		
		R	U	А	
CO1-78MS306-A .1 Do review of literature.	Review of Literature	2	3	5	10
CO2-78MS306-A .2 Write review paper thesis write and Generate report.	Report Writing	2	3	5	10



CO3-78MS306-A .3 Aware to format of publications	Typesetting Mathematical Text With LATEX	2	3	5	10
CO4-78MS306-A .4 Understand concept of impact factor, H index	Packages	1	1	3	05
CO5-78MS306-A.5 Understand implementation of Softwares to writing research papers and plotting the graphs.	MATLAB	2	3	10	15
Total		9	13	28	50

Legend: R: Remember, U: Understand, A: Apply

The end of semester assessment for Introduction to Portland cement will be held with written examination of 50 marks

**Note**. Detailed Assessment rubric need to be prepared by the course wise teachers for above tasks. Teachers can also design different tasks as per requirement, for end semester assessment.

#### **Suggested Instructional/Implementation Strategies**

- 1. Improved Lecture
- 2. Tutorial
- 3. Presentation
- 4. Group Discussion
- 5. Online sources
- 6 .Seminar
- 7. Workshop

#### **Suggested Learning Resources:**

#### a) Books:

S.No.	Title	Author	Publisher	Edition
1	Scientific writing Booklet	Marc E. Tischler		



2	Scientific Writing For Graduate Students	F. Peter Woodford The Rockefeller University, New York	Library of Congress catalogue card number 68-56104,USA	
3	American Medical Association Manual of Style:a Guide for Authors and Editors	Williams & Wilkins	Baltimore	9th , 1998
4	Author's Handbook of Styles for Life Science Journals.; Iverson, Cheryl, Ed.;	Atlas, Michel C	CRC Press: Boca Raton,	1996
5	Byrne, Daniel W. Publishing your Medical Research Paper: What They Don't Teach You in Medical School	Williams & Wilkins:	Baltimore	1998

#### b) Reference Book:

S.	Title	Author	Publisher	Edition & Year
No.				
1	Interpreting the	Gehlbach, Stephen H.	McGraw Hill Medical	4 <sup>th</sup> , 2002
	Medical Literature		Publishing Division:	
			New York,	
2	Successful	Matthews, Janice R.;	Cambridge University	2nd ed. & 2000
	Scientific Writing: a	Bowen, John M.;	Press: New York,	
	Step-bystep Guide	Matthews, Robert W.		
	for Biomedical			
	Scientists,;			
3	Writing Papers in	McMillan, Vicky.	Bedford Books: Boston	3rd ed., 2001.
	the Biological			
	Sciences			
4	Short Guide to	Pechenik, Jan A. A	Longman: New York	4th ed.,2001.
	Writing about			
	Biology, ,			



5	Essentials of	Essentials of Zeiger, Mimi. McGraw-Hill, Health		2nd ed. 2000.
	Writing Biomedical		Professions Division:	
	Research Papers		New York	

#### c) Suggetsed Digital Platform Web links:

Suggested	http://www.organicworldwide.net/writing.html							
Digital	http://www.mang.canterbury.ac.nz/courseinfo/AcademicWriting/Scientific.html							
Platforms	http://mason.gmu.edu/~arichar6/logic.htm							
Web links:	- Logical Fallacies In Scientific Writing; A. Stephen Richardson							
	http://www.stark.kent.edu/writing/outline.html							
	- outlines							
	http://bio.winona.edu/delong/EcoLab/21%20Suggestions.html							
	- Twenty-One Suggestions for Writing Good Scientific Papers:							
	http://www.mco.edu/lib/instr/libinsta.html							
	- Instructions to Authors in the Health Sciences (a plethora of journals) B							

#### **Curriculum Development Team**

- 1. Dr.Sudha Agrawal, HOD, Department of Mathematics.
- 2. Dr.Ekta Shrivastava, Assistant Professor, Department of Mathematics.
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- 8. Ms. Arpana Tripathi, Assistant Professor, Department of Mathematics.

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### **Cos, POs and PSOs Mapping**

**Course Title: M.Sc. Mathematics** 

Course Code: 78MS306-A
Course Title: Scientific writing

Course Outcome	PO1  Adv ance d Mat hem atica l Kno wled ge	PO 2  Pro ble m-sol vin g Skil ls	P O 3 R es ea rc h A bil iti es	PO 4  Qu anti tati ve Ana lysi s	PO5  Teach ing and Acad emia	PO 6  The ore tica I Un der sta ndi ng	PO7  Com muni catio n Skills	Oper ation s Rese arch	Appli catio n in Indus try	PO10  Engin eerin g and Tech nolog y	PO 11 Gov ern men t and Publ ic Sect or	PO 12  Co ns ult in g	PSO 1  Understand the mathemati cal concepts and applications in the field of algebra	PSO 2 Han dle the adva nced tech niqu es	PSO 3  Develop necessary skills and expertise in the field of research	PSO 4  Creates Mathem atical Models
<b>CO1- 78MS306- A</b> .1  Do review of literature.	2	1	3	2	1	2	3	3	1	1	2	1	1	2	1	2



### AKS University Faculty of Basic Science Department of Mathematics

### Curriculum & Syllabus of M.Sc. Mathematics program

CO2- 78MS306- A .2  Write review paper thesis write and Generate report.	2	1	3	2	1	2	3	3	1	2	2	1	3	2	1	1
<b>78MS306-A .3</b> Aware to format of publication	2	1	2	2	1	3	3	2	2	2	1	1	2	2	1	1
CO4- 78MS306-A .4 Understand concept of impact factor, H index	2	1	2	2	2	2	3	2	3	2	2	2	2	1	1	1
CO5- 78MS306- A.5 Understand implement ation of Softwares to writing research papers and plotting the graphs.	2	2	2	2	3	3	2	2	2	1	1	3	1	1	2	1



Legend: 1 – Low, 2 – Medium, 3 – High

### **Course Curriculum Map**:

POs & PSOs No.	COs No.& Titles	SOs No.	Labora tory Instru ction(L I)	Classroom Instruction (CI)	Self Learning (SL)
PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2, 3, 4	CO1-78MS306-A .1 literature.	SO1.1 SO1.2 SO1.3		Unit-1.0 linear programming problem. 1.1,1.2,1.3,1.4,1.5,1.6,1.7,1.8, 1.9	SL1.1 SL1.2
PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2, 3, 4	CO2-78MS306-A .2 Write review paper thesis write and Generate report.	SO1.1 SO1.2 SO1.3		Unit-2 solution of linear programming problem. 2.1, 2.2, 2.3, 2.4, 2.5, 2.6, 2.7, 2.8,2.9	SL2.1 SL2.2
PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2, 3, 4	CO3-78MS306-A .3  Aware to format of publications	SO1.1 SO1.2 SO1.3		Unit-3 . Assignment problem: 3.1, 3.2, 3.3, 3.4, 3.5, 3.6, 3.7, 3.8,3.9	SL3.1 SL3.2
PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2, 3, 4	CO4-78MS306-A .4 Understand concept of impact factor, H index	SO1.1 SO1.2 SO1.3		Unit-4 Transportation problem: 4.1, 4.2, 4.3, 4.4, 4.5, 4.6, 4.7, 4.8,4.9	SL4.1 SL4.2



## AKS University Faculty of Basic Science Department of Mathematics

### Curriculum & Syllabus of M.Sc. Mathematics program

PO 1,2,3,4,5,6	CO5-78MS306-A.5	SO1.1	Unit-5 Network Analysis:	SL5.1
7,8,9,10,11,12	Understand	SO1.2		SL5.2
PSO 1,2, 3, 4	Onderstand	SO1.3	5.1, 5.2, 5.3, 5.4, 5	
	implementation of		.5, 5.6, 5.7, 5.8,5.9	
	Softwares to writing			
	research papers and			
	plotting the graphs.			

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#### Semester-IV

Course Code: 78MS401

Course Title : Analytic Number Theory

**Pre- requisite:**• Basic knowledge of complex analysis

• Familiarity with number theory concepts

• Understanding of basic calculus

Rationale: Analytic number theory aims to understand the

distribution of prime numbers, study their arithmetic properties, and investigate connections between prime numbers and other

mathematical objects.

**78MS401.1** Be able to effectively express the concepts and results of number theory.

**78MS401.2** Learn basic theory of arithmetical functions and Dirichlet multiplication, averages of some arithmetical functions.

**78MS401.3** Understand distribution of prime numbers and prime number theorem.

**78MS401.4** Learn the concept of quadratic residue and Quadratic reciprocity laws.

**78MS401.5** Get a basic knowledge in Cryptography.

#### Scheme of Studies:

Board of	Course Code	Course Title	Scheme of	studies (Hour	s/Week)			Total Credi	
Study	Code	nue	CI	LI	SW	SL	Total Study Hours (CI+LI+SW+SL)	ts (C)	
Program Core (PCC)	78MS401	Analytic Number Theory	4[3+1]	0	1	1	6	4	

#### Legend:

**CI:** Classroom Instruction (Includes different instructional strategies i.e. Lecture (L) and Tutorial (T) and others),



**LI:** Laboratory Instruction (Includes Practical performances in laboratory workshop, field or other locations using different instructional strategies)

**SW:** Sessional Work (includes assignment, seminar, mini project etc.)

**SL:** Self Learning,

C:Credits.

**Note:** SW & SL has to be planned and performed under the continuous guidance and feedback of teacher to ensure outcome of Learning.

#### Scheme of Assessment:

#### **Theory**

Boar	Couse	Course Title	Scheme of Assessment ( Marks )							
d of Stud y	Code		Progres	sive Asses	End Semester Assessment (ESA)	Total Marks (PRA+ ESA)				
			Class/Home Assignment 5 number 3 marks each ( CA)	Class Test 2 (2 best out of 3) 10 marks each (CT)	Seminar one ( SA)	Class Activit y any one (CAT)	Class Attendanc e (AT)	Total Marks (CA+CT+ SA + CAT+AT)		
PCC	78MS40 1	Analytic Number Theory	15	20	5	5	5	50	50	100

#### **Course-Curriculum Detailing:**

This course syllabus illustrates the expected learning achievements, both at the course and session levels, which students are anticipated to accomplish through various modes of instruction including Classroom Instruction (CI), Laboratory Instruction (LI), Sessional Work (SW), and Self Learning (SL). As the course progresses, students should showcase their mastery of Session Outcomes (SOs), culminating in the overall achievement of Course Outcomes (COs) upon the course's conclusion.



**CO1-78MS401.1** Be able to effectively express the concepts and results of number theory.

Item	AppX Hrs
Cl	12
LI	0
SW	1
SL	1
Total	14

Session Outcomes	Laboratory	Class room Instruction	Self Learning
(SOs)	Instruction	(CI)	(SL)
	(LI)		
SO1.1		Unit-1 Dirichlet Series and	SL.1
Real-world applications of		<b>Euler Products</b>	Basic
Dirichlet series and Euler		1.1 Introduction	knowledge of
products in number theory.		1.2 Briefly review the	complex
		concepts of complex analysis	analysis
SO1.2	-	1.3 Dirichlet characters and	SL.2
Students will understand the		the Dirichlet convolution.	Familiarity with
concepts of Dirichlet Series			number theory
and Euler Products, and		1.4 Definition and	
their applications in number		Convergence of Dirichlet	
theory.		Series	
		1.5 Introduce the need for	
		Dirichlet series in number	
		theory.	
		1.6 Dirichlet Characters	
		1.7 Tutorial-I	
		1.8 Euler Products	
		1.9 Explore applications of	
		Euler products in number	
		theory	
		1.10 Work through examples	
		of Dirichlet series and Euler	
		products.	
		<b>1.11</b> Motivate the study of	
		Euler products by discussing	
		their role in representing	
		certain arithmetic functions	
		1.12 Tutorial-II	



#### SW-1 Suggested Sessional Work (SW):

#### a. Assignments:

Exercises and problems related to Dirichlet series and Euler products .

#### b. Mini Project:

Oral presentation

**c.** Other Activities (Specify):

Quiz, Class Test.

**CO2-78MS401.2** Learn basic theory of arithmetical functions and Dirichlet multiplication, averages of some arithmetical functions.

Item	AppX Hrs
Cl	12
LI	0
SW	1
SL	1
Total	14

		Total	14
Session Outcomes	Labora	Class room Instruction	Self Learning
(SOs)	tory	(CI)	(SL)
,	Instruc		` ,
	tion		
	(LI)		
SO2.1		Unit-2.0 The Function defined	SL.1
Students will understand the		by Series, The half plane of	Basic knowledge
concept of functions defined by		convergence of a Dirichlet	of complex
series and the half plane of		Series.	analysis
convergence of a Dirichlet series.			SL.2
		2.1 Briefly review complex	Understanding
SO2.2		numbers, complex	of series
Convergence and divergence		functions, and series	convergence
criteria		convergence	
		2.2 Introduction to Functions	
		Defined by Series	
		2.3 Power Series	
		2.4 Introduce the notion of the	
		interval of convergence for	
		a power series.	
		2.5 Tutorials-I	
		2.6 Function Representation	
		2.7 The concept of the Taylor	



	series and its role in representing functions.  2.8 Examples and Applications  2.9 Half Plane of Convergence: Introduction  2.10 Convergence in a Half Plane  2.11 Conditions for Convergence  2.12 Tutorials-II	
--	--	--

#### SW-2 Suggested Sessional Work (SW):

#### a. Assignments:

Assign exercises and problems related to functions defined by series and Dirichlet series convergence for further practice.

**b.** Other Activities (Specify): Quiz, Class Test.

**CO3-78MS401.3** Understand distribution of prime numbers and prime number theorem.

Item	AppX Hrs
Cl	12
LI	0
SW	1
SL	1
Total	14

Session Outcomes	Laboratory	Class room Instruction	Self
(SOs)	Instruction	(CI)	Learning
	(LI)		(SL)
SO3.1		Unit-3.0	SL.1
Student able to		The Integral formula for the	Definition of
understand the Dirichlet		coefficients of Dirichlet Series	Dirichlet
Series Representation			Series
		3.1 Brief overview of Dirichlet series	
SO3.2		3.2 Importance of coefficients in	
Student able to Identify		analyzing the behaviour of series	SL.2
the poles of the function		3.3 Statement of the integral	Derivation
F(s)/s within the contour.		formula for coefficients	of Euler's
and Student able to use		3.4 Definition of Dirichlet series	Formula for



the residue theorem to evaluate the integral. The	3	.5 Convergence and divergence criteria	Dirichlet Series
residues at the poles	3	.6 Basic properties and examples.	
contribute to the value of the integral.	3	<ul><li>.7 Introduction to analytic continuation</li></ul>	
	3	<ul><li>.8 The need for analytic continuation in Dirichlet series</li></ul>	
	3	<ul><li>.9 Key theorems and concepts related to analytic continuation</li></ul>	
	3	.10 Application of complex integration to Dirichlet series	
	3	.11 Application of the integral formula in number theory	
	3	.12 Tutorial	

#### SW-3 Suggested Sessional Work (SW):

#### a. Assignments:

The Integral formula for the coefficients of Dirichlet Series.

**b.** Other Activities (Specify): Quiz, Class Test.

**CO4-78MS401.4** Understanding of the concept of gravitational waves, their detection, and their significance as a powerful tool to study astrophysical phenomena.

Item	AppX Hrs
Cl	12
LI	0
SW	1
SL	1
Total	14

Session Outcomes (SOs)	Laboratory Instruction (LI)	Class room Instruction (CI)	Self Learning (SL)
SO4.1		Unit-4.0 Analytic Properties of	SL.1
Understand the		Dirichlet Series	Ensure you have a solid
Basics of Convergence		<b>4.1</b> Introduction	understanding of
and Divergence		<b>4.2</b> Convergence of Dirichlet Series	complex analysis,
		<b>4.3</b> Pointwise convergence	including topics like
SO4.2		<b>4.4</b> Uniform convergence	complex numbers,
Student will Learn		<b>4.5</b> Application of Dirichlet's	power series, and



about the concept of	Theorem to prime distribu	tion contour integration.
analytic continuation	<b>4.6</b> Extension to more general	SL.2
for Dirichlet series.	arithmetic functions	Familiarize yourself
	<b>4.7</b> Tutorial-I	with basic concepts in
	4.8 Introduction to analytic	number theory, such as
	continuation	prime numbers,
	<b>4.9</b> Connection between Diricl	hlet arithmetic functions,
	Series and Analytic Continu	uation and Euler's totient
	<b>4.10</b> Mean value formula for	function.
	Dirichlet Series.	
	<b>4.11</b> Advanced analytic techni	iques in
	the study of Dirichlet Ser	ies
	4.12 Tutorial-II	

#### SW-4 Suggested Sessional Work (SW):

a. Assignments:

Analytic Properties of Dirichlet Series

**b.** Other Activities (Specify): Quiz, Class Test.

**CO5-78MS401.5** Understanding of the concepts, principles, and mathematical framework of the General Theory of Relativity.

Item	AppX Hrs
Cl	12
LI	0
SW	1
SL	1
Total	14

Session Outcomes (SOs)	Laboratory Instruction (LI)	Class room Instruction (CI)	Self Learning (SL)
SO5.1		Unit-5.0 zeta function	SL.1
Understand the			Knowledge of
concept of zeta		5.1 Gamma Function	complex number
function		5.2 Properties of Gamma Function	SL.2
		5.3 Examples on Gamma Function	Knowledge of
SO5.2		5.4 The Riemann zeta function and	Gamma Function
Understand the		its analytic continuation	
application of Hurwitz		<b>5.5</b> Hurwitz zeta function	
zeta function		<b>5.6</b> Integral representation of	



Hurwitz zeta function
5.7 Tutorial-I
5.8 Analytic Continuation of
Hurwitz zeta function
5.9 Examples on analytic
Continuation of Hurwitz zeta
function.
<b>5.10</b> Calculation of Hurwitz Zeta
Function
5.11 Examples
<b>5.12</b> Tutorial-I

#### SW-5 Suggested Sessional Work (SW):

#### a. Assignments:

Bending of light rays in a gravitational field. Gravitational redshift ,Spectral lines. nergy-momentum tensor of a perfect fluid. Schwarzschild internal solution. Boundary conditions. Energy-Momentum tensor of an electromagnetic field.

**b.** Other Activities (Specify): Quiz, Class Test.

#### **Brief of Hours suggested for the Course Outcome**

Course Outcomes	Class Lecture (CI)	Sessional Work (SW)	Self Learning (SI)	Total hour (Cl+SW+SI)
78MS401.1 Be able to effectively express the concepts and results of number theory.	12	1	1	14
CO2-78MS401.2 78MS401.2 Learn basic theory of arithmetical functions and Dirichlet multiplication, averages of some arithmetical functions.	12	1	1	14
78MS401.3 Understand distribution of prime numbers and prime number theorem.	12	1	1	14
78MS401.4 Learn the concept of quadratic residue and Quadratic	12	1	1	14



reciprocity laws.				
78MS401.5Get a basic knowledge in Cryptography.	12	1	1	14
Total Hours	60	5	5	70

#### **Suggestion for End Semester Assessment**

Suggested Specification Table (For ESA)

СО	Unit Titles	Marks [	Distributio	n	Total Marks
		R	U	Α	
CO-1	Dirichlet Series and Euler Products	05	05	05	15
CO-2	Convergence of Dirichlet Series	05	05	05	15
CO-3	coefficients of Dirichlet Series	03	01	02	06
CO-4	Analytic Properties of Dirichlet Series	03	03	02	08
CO-5	Zeta Function	03	01	02	06
	Total	25	17	08	50

Legend: R: Remember, U: Understand, A: Apply

The end of semester assessment for Introduction to Portland cement will be held with written examination of 50 marks

**Note**. Detailed Assessment rubric need to be prepared by the course wise teachers for above tasks. Teachers can also design different tasks as per requirement, for end semester assessment.

#### **Suggested Instructional/Implementation Strategies**

- 1. Improved Lecture
- 2. Tutorial
- 3. Presentation
- 4. Group Discussion
- 5. Online sources



- 6. Seminar
- 7. Workshop

#### **Suggested Learning Resources:**

#### a) Books:

S. N o.	Title	Author	Publisher	Edition & Year
1	Introduction to Analytic Number Theory	T. M. Apostol	Narosa Pub. House	1989
2	Introduction to Analytic Number Theory	Apostol, T. M.,	Springer International Student Edition,Narosa Publishing House, New Delhi	1993.
3	An Introduction to the Theory of Numbers	Hardy, G.H. and Wright, E. M.	Oxford University Press	4th Edition, 1960
4	An Introduction to the Theory of Numbers	Niven, I. and Zuckerman, H.	Wiley Eastern, New Delhi	5th Edition, 2000
5	A classical introduction to modern number theory	Kenneth Ireland and Michael Rosen	Springer	(2010)

#### **Curriculum Development Team**

- 1. Dr. Sudha Agrawal, HOD, Department of Mathematics.
- 2. Dr. Ekta Shrivastava, Assistant Professor, Department of Mathematics.
- 3. Mr. Neelkanth Napit, Assistant Professor, Department of Mathematics.
- 4. Mrs. Vandana Soni, Assistant Professor, Department of Mathematics.
- 5. Mr.Radhakrishna Shukla, Assistant Professor, Department of Mathematics.
- 6. Mr.Ghanhyam sen, Assistant Professor, Department of Mathematics.
- 7. Ms. Pushpa Kushwaha, Assistant Professor, Department of Mathematics.
- 8. Ms. Arpana Tripathi, Assistant Professor, Department of Mathematics.



### **Cos, POs and PSOs Mapping**

**Course Title: M.Sc. Mathematics** 

Course Code: 78MS401

**Course Title: Analytic Number Theory** 

	PO 1	PO2	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10	PO1 1	PO12	PSO 1	PSO 2	PSO 3	PS O 4
Course	Ad	Prob	Res	Qu	Teac	Th	Com	Oper	Appli	Engi	Go	Cons	Under	На	Dev	Cre
Outcome	va	lem-	ear	ant	hing	eor	muni	ation	catio	neeri	ver	ultin	stand	ndl	elo	ate
	nc	solvi	ch	itat	and	etic	catio	S	n in	ng	nm	g	the	е	р	S
	ed	ng	Abil	ive	Acad	al	n	Rese	Indu	and	ent		mathe	the	nec	Ma
	М	Skill	itie	An	emia	Un	Skills	arch	stry	Tech	an		matica	ad	ess	the
	at	S	s	aly		der				nolo	d		1	va	ary	mat
	he			sis		sta				gy	Pu		conce	nc	skill	ical
	m					ndi					blic		pts	ed	S	Мо
	ati					ng					Sec		and	tec	and	del
	ca										tor		applic	hni	ехр	S
	1												ations	qu	erti	
	Kn												in the	es	se	
	О												field		in	
	wl												of		the	
	ed												algebr		fiel	
	ge												а		d of	
															res	
															ear	
															ch	
CO1-	2	3	1	2	1	2	2	2	1	1	1	1	2	1	1	<u>3</u>
78MS401.1																
Be able to																
effectively																
express the																
concepts																
and results																
of number																
theory.																



78MS401.2	1	3	2	1	1	1	1	1	1	2	3	1	<u>3</u>	1	1	2
Learn basic	_		_	_	-	_	_	_	-	_	J	-	<u> </u>	=	=	=
theory of																
arithmetical																
functions																
and Dirichlet																
multiplicatio																
n, averages																
of some																
arithmetical																
functions.																
78MS401.3		3	2	2	1	1	3	2	1	1	3	1	<u>2</u>	<u>1</u>	<u>2</u>	2
Understand													_	_	_	
distribution																
of prime																
numbers																
and prime																
number																
theorem.																
78MS401.4	2	3	2	2	1	1	3	2	1	1	3	1	<u>2</u>	1	2	2
Learn the																
concept of																
quadratic																
residue and																
Quadratic																
reciprocity																
laws.																
	2	3	2	2	1	1	3	2	1	1	3	1	2	1	<u>2</u>	3
Get a basic																
knowledge																
										ì			•			
in Crypto -																

Legend: 1 – Low, 2 – Medium, 3 – High



### **Course Curriculum Map:**

POs & PSOs	COs No.& Titles	SOs No.	Laboratory	Classroom Instruction	Self Learning (SL)
No.			Instruction(	(CI)	
20	004 70140444 8	504.4	LI)		CLAA
PO	CO1-78MS401.1 Be	SO1.1		Unit-1.0 Group	SL1.1
1,2,3,4,5,6	able to effectively	SO1.2		1.1,1.2,1.3,1.4,1.5,1.6,1.	SL1.2
7,8,9,10,11,1	express the concepts			7,1.8,1.9,1.10,1.11.1.12	SL1.3
2	and results of number				
PSO 1,2, 3, 4	theory.				
РО	78MS401.2	SO1.1		Unit-2 Ring	SL2.1
1,2,3,4,5,6	Learn basic theory of	SO1.2		2.1, 2.2, 2.3, 2.4, 2.5, 2.6,	SL2.2
7,8,9,10,11,1	arithmetical functions			2.7, 2.8,2.9,2.10,	
2	and Dirichlet			2.11,1.12	
PSO 1,2, 3, 4	multiplication averages				
	of some arithmetical				
	functions.				
PO	78MS401.3 Understand	SO1.1		Unit-3	SL3.1
1,2,3,4,5,6	distribution of prime	SO1.2		3.1, 3.2, 3.3, 3.4, 3.5, 3.6,	SL3.2
7,8,9,10,11,1	numbers and prime			3.7, 3.8,3.9,3.10,	
2	number theorem.			3.11,3.12	
PSO 1,2, 3, 4					
PO	78MS401.4 Learn the	SO1.1		Unit-4	SL4.1
1,2,3,4,5,6	concept of quadratic	SO1.2		4.1, 4.2, 4.3, 4.4, 4.5, 4.6,	SL4.2
7,8,9,10,11,1	residue and Quadratic			4.7, 4.8,4.9,4.10,	
2	reciprocity laws.			4.11,4.12	
PSO 1,2, 3, 4					
PO	78MS401.5 Get a basic	SO1.1		Unit-5	SL5.1
1,2,3,4,5,6	knowledge in Crypto -	SO1.2		5.1, 5.2, 5.3, 5.4, 5.5, 5.6,	SL5.2
7,8,9,10,11,1	graphy.			5.7, 5.8,5.9,5.10.	
2				5.11,5.12	
PSO 1,2, 3, 4					

\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*



#### Semester-IV

Course Code: 78MS402

Course Title : Functional Analysis

Pre-requisite: Students should have basic knowledge of and

deep understanding of the theory of the

advanced numerical techniques.

Rationale: The program aims to develop advanced problem-

solving and analytical skills and prepares students for careers in academia, research, industry, or other sectors that require advanced

mathematical expertise.

#### **Course Outcomes:**

CO1-78MS402.1 Understand the importance of Normed Linear spaces and Banach spaces

CO2-78MS402.2 Determine the Fundamental theorems on Normed linear space

CO3-78MS402.3 Demonstrate an understanding of the Applications of Normed linear space

**CO4-78MS402.4** Define and recognize the Hilbert Spaces

CO5-78MS402.5 Students will create the concept of aOperator Theory and Sturm-Liouville System

#### **Scheme of Studies:**

Board of	Course Code	Course Title	Scheme of studies (Hours/Week)					
Study	Code		Cl	LI	sw	SL	Total Study Hours (CI+LI+SW+SL)	ts (C)
Program Core (PCC)	78MS402	Function al Analysis	4[3+1]	0	1	1	6	4

#### Legend:

**CI:** Classroom Instruction (Includes different instructional strategies i.e. Lecture (L) and Tutorial (T) and others),

**LI:** Laboratory Instruction (Includes Practical performances in laboratory workshop, field or other locations using different instructional strategies)



SW: Sessional Work (includes assignment, seminar, mini project etc.),

SL: Self Learning,

C:Credits.

**Note:** SW & SL has to be planned and performed under the continuous guidance and feedback of teacher to ensure outcome of Learning.

#### **Scheme of Assessment:**

#### Theory

Board of	Couse	Course Title	Scheme of	Assessme	ent ( Marks	)				
Study	Code			Progressive Assessment ( PRA )						Total Marks (PRA+ ESA)
			Class/Ho me Assignme nt 5 number 3 marks each ( CA)	Class Test 2 (2 best out of 3) 10 marks each (CT)	Seminar one ( SA)	Class Activit y any one (CAT)	Class Attend ance (AT)	Total Marks (CA+CT+ SA +CAT+A T)	(ESA)	
PCC	78MS402	Functional Analysis	15	20	5	5	5	50	50	100

#### **Course-Curriculum Detailing:**

This course syllabus illustrates the expected learning achievements, both at the course and session levels, which students are anticipated to accomplish through various modes of instruction including Classroom Instruction (CI), Laboratory Instruction (LI), Sessional Work (SW), and Self Learning (SL). As the course progresses, students should showcase their mastery of Session Outcomes (SOs), culminating in the overall achievement of Course Outcomes (COs) upon the course's conclusion.

CO1-78MS402.1 Understand the importance of Normed Linear spaces and Banach spaces



#### **Approximate Hours**

Item	AppXHrs
Cl	13
LI	0
SW	1
SL	1
Total	15

Session Outcomes (SOs)	Laboratory Instruction (LI)	Class room Instruction (CI)	Self Learning (SL)
SO1.1 Understand the concept of Normed linear spaces SO1.2 Understand the Banach space  SO1.3 Understand the Basic properties of finite dimensional Normed spaces. SO1.4 Understand Completion of a Normed linear space		Unit-1.0 1.1 Norm 1.2 Normed linear spaces. 1.3 Tutorial 1 1.4 Quotient space of Normed linear space 1.5 Subspace 1.6 Completeness, 1.7 Banach space 1.8 Equivalent norms. 1.9 Basic properties of finite dimensional Normed spaces 1.10 Tutorial 2 1.11 Projections 1.12 Completion of a Normed linear space, 1.13 Riesz lemma	SL1.1Examples of offinite dimensional Normed spaces

#### SW-1 Suggested Sessional Work (SW):

#### a. Assignments:

- (i) State and prove Riesz lemma
- (ii) Any finite dimensional normed linear space is a Banach space



(iii) Define Norm and Normed Linear Space and Show that  $\mathbb{R}^n$  is nls with the following norms

$$(i) \| x \|_{1} = \sum_{i=1}^{n} |x_{i}| (ii) \| x \|_{2} = \left(\sum_{i=1}^{n} |x_{i}|^{2}\right)^{\frac{1}{2}}$$

$$(iii) \| x \|_{\infty} = \max_{1 \le i \le n} |x_{i}|$$

(iv) Show that  $l_{\infty} \ c$  are normed linear space with the norm

$$\parallel x \parallel = \lim_{n \to \infty} \lvert x_n \rvert \ \ \text{define a norm on c}$$

(v)Show that the real linear space R and the complex linear space are Banach space under the **norm** 

$$||x|| = |x|$$
,  $x \in C$  or R

#### b. Mini Project:

Oral presentation, Poster presentation, Power Point Presentation.

**c.** Other Activities (Specify): Quiz, Class Test.

CO2-78MS402.2 Determine the Fundamental theorems on Normed linear space

F F	
Item	AppXHrs
Cl	10
LI	0
SW	1
SL	1
Total	11

Session Outcomes	Laboratory Instruction	Class room Instruction	Self Learning
(SOs)	(LI)	(CI)	
SO2.1		Unit2.0	S.L.1 some theorems
Understand the		2.1 Bounded linear	on weak and strong
concept Bounded linear		transformations	convergence
transformations		2.2 Dual spaces with	



	examples	
SO2.2	2.3 Tutorial 1	
Understand the dual	2.4 Weak Convergence,	
spaces	2.5 Uniform	
	boundedness principle	
SO2.3		
Understand the Open	2.6 Uniform	
mapping and closed	boundedness theorem	
graph theorems		
	2.7 Consequences.	
SO2.4	2.8 Tutorial 2	
Understand the Weak	2.9 Open mapping	
Convergence	theorem	
	2.10 Closed graph	
	theorems.	

#### SW-2 Suggested Sessional Work (SW):

#### a. Assignments:

- (I) State and prove closed graph theorems
- (ii)State and prove uniform boundedness theorem
- (iii) State and prove open mapping theorem
- (iv) Weak convergence does not necessarily imply strong convergence.

#### b. Mini Project:

Oral presentation, Poster presentation, Power Point Presentation.

**c.** Other Activities (Specify):

Quiz, Class Test.

CO3-78MS402.3 Demonstrate an understanding of the Applications of Normed linear space.

Approximate mours				
Item	AppXHrs			
Cl	10			
LI	0			
SW	1			
SL	1			
Total	12			



Session Outcomes	Laboratory	Class room Instruction	Self Learning
(SOs)	Instruction (LI)	(CI)	(SL)
<b>SO3.1</b> Understand the		Unit-3.0	SL.1
theHahn-Banach			Solve the
theorem for real linear		3.1 Hahn-Banach theorem for real	many
space		linear space	problems
			reflexive
		3.2 linear spaces,	space
SO3.2 Understand the			
Complex linear spaces		3.3 Banach's theorem	
		3.4 Complex linear spaces.	
<b>SO3.3</b> Understand the			
Reflexive spaces		3.5 Reflexive spaces.	
603.4 Hadanstond the		3.6 Tutorial 1	
<b>SO3.4</b> Understand the			
Solvability of linear		3.7 Weak Sequential	
equations in Banach		Compactness.	
spaces			
		3.8 Solvability of linear equations	
		in Banach spaces	
		3.9 Tutorial 2	
		3.10 application of Hahn-Banach	
		theorem	

#### SW-3 Suggested Sessional Work (SW):

#### a. Assignments:

- (i) State and prove Hahn Banach theorem for a real normed linear space
- (ii)Show that every finite dimensional nls is reflexive
- (iii) State and prove Banach theorem
- (iv) Define reflexive space with one example

#### b. Mini Project:

Oral presentation, Poster presentation, Power Point Presentation.

c. Other Activities (Specify):

Quiz, Class Test.



**CO4-78MS402.4** Define and recognize the Hilbert Spaces

### **Approximate Hours**

Item	AppXHrs
Cl	14
LI	0
SW	1
SL	1
Total	16

Session Outcomes (SOs)	Laboratory Instruction (LI)	Class room Instruction (CI)	Self Learning (SL)
<b>SO4.1</b> Understand the		Unit-4.0	SL.1
Inner-product spaces		4.1 Inner-product	Some problems on
		spaces	Reflexivity of Hilbert
<b>SO4.2</b> Understand the		4.2 Cauchy-Schwarz	spaces
Hilbert spaces		Inequality	
		4.3 The Triangle	
		Inequality,	
SO4.3		4.4 Polarization Identity	
		4.5 Hilbert spaces,	
Understand the		4.6 Orthonormal Sets.	
Cauchy-Schwarz		4.7 Bessel's inequality.	
Inequality		4.8 Parseval's identity	
		4.9 Structure of Hilbert	
		spaces.	
		4.10 Projection	
SO4.4		theorem 4.11Riesz -	
Understand and		Fischer theorem	
problems solving on		4.12 Riesz	
Structure of Hilbert		representation	
spaces.		theorem	
		4.13 Tutorial 1	
		4.14 Tutorial 2	

### SW-4 Suggested Sessional Work (SW):

### a. Assignments:

- (i) State and prove Bessel's inequality
- (ii) Prove that every inner product space is a normed space
- (iii) State and prove Riesz -Fischer theorem,
- (iv) State and prove Riesz representation



(v) State and prove Parseval's identity

### b. Mini Project:

Oral presentation, Poster presentation, Power Point Presentation.

**c.** Other Activities (Specify):

Quiz, Class Test.

**CO5-78MS402.5** Students will create the concept of aOperator Theory and Sturm-Liouville System.

Item	Appx Hrs
Cl	13
LI	0
SW	1
SL	1
Total	15

Session Outcomes (SOs)	Laboratory Instruction (LI)	Class room Instruction (CI)	Self Learning (SL)
SO5.1 Understand the conceptLinear Operators SO5.2 Understand the Self-Adjoint operators SO5.3 Understand Normal and Unitary operators SO5.4 Understand The The Closed Range Theorem. SO5.5 Understand The Sturm-Liouville Problems		Unit-5.0 5.1 Linear Operators, 5.2 Adjoint of an operator on a Hilbert space. 5.3 Tutorial 1 5.4 Self-Adjoint operators 5.5 Positive operators, 5.6 Compact Operators, 5.7 Invertible operators, 5.8 Identity operators 5.9 Projection operators, 5.10 Normal and Unitary operators.	SL.1 Application to Sturm- Liouville Problems.



	5.11 The Closed Range	
	Theorem.	
	5.12Sturm-Liouville Problems.	
	5.13 Tutorial 2	

### SW-3 Suggested Sessional Work (SW):

### a. Assignments

- (i) State and prove The Closed Range Theorem
- (ii) Prove that Every positive operator is self adjoint
- (iii) An operator T on a Hilbert space H is unitary if and only if it is an isometric isomorphism of H onto itself
- (iv) Let T be an operator on H then prove that I\*=I where I is the identity operator

### b. Mini Project:

Oral presentation, Poster presentation, Power Point Presentation.

### **c.** Other Activities (Specify):

Quiz, Class Test.

### **Brief of Hours suggested for the Course Outcome**

Course Outcomes	Class Lecture (CI)	Sessional Work (SW)	Self Learning (SI)	Total hour (Cl+SW+SI)
CO1-78MS402.1 Understand the importance of Normed Linear spaces and Banach spaces	13	1	1	15
CO2-78MS402.2 Determine the Fundamental theorems on Normed linear space	10	1	1	12
CO3-78MS402.3 Demonstrate an understanding of the Applications of	10	1	1	12



Normed linear space				
CO4-78MS402.4 Define and recognize the Hilbert Spaces	14	1	1	16
CO5-78MS402.5 Students will create the concept of a Operator Theory and Sturm-Liouville System	13	1	1	15
Total Hours	60	5	5	70

### **Suggestion for End Semester Assessment**

Suggested Specification Table (For ESA)

СО	Unit Titles	Mark	s Distribu	ution	Total Marks	
		R	U	Α		
CO-1	Understand the importance of Normed Linear spaces and Banach spaces	03	01	01		05
CO-2	Determine the Fundamental theorems on Normed linear space	02	06	02		10
CO-3	Demonstrate an understanding of the Applications of Normed linear space	03	07	05		15
CO-4	Define and recognize the Hilbert Spaces	-	10	05		15
CO-5	Students will create the concept of an Operator Theory and Sturm-Liouville System	03	02		-	05
Total	•	11	26		13	50



Legend: R: Remember, U: Understand, A: Apply

The end of semester assessment for Introduction to Portland cement will be held with written examination of 50 marks

**Note**. Detailed Assessment rubric need to be prepared by the course wise teachers for above tasks. Teachers can also design different tasks as per requirement, for end semester assessment.

### **Suggested Instructional/Implementation Strategies**

- 1. Improved Lecture
- 2. Tutorial
- 3. Presentation
- 4. Group Discussion
- 5. Online sources
- 6 .Seminar
- 7. Workshop

#### **Suggested Learning Resources:**

#### a) Books:

S. No.	Title	Author	Edition & Year		
1	Functional Analysis with Application.	H. K. Pathak		Third Revised Edition :2018- 2019	
2	Functional Analysis	Rudin W.		McGraw Hill,2000	
3	Introduction to Functional Analysis	A.H. Siddique	Real world education publisher New Delhi	2014	

#### **Curriculum Development Team**

- 1. Dr.Sudha Agrawal, HOD, Department of Mathematics.
- 2. Dr. Ekta Shrivastava, Assistant Professor, Department of Mathematics.
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### **Cos, POs and PSOs Mapping**

**Course Title: M.Sc. Mathematics** 

Course Code: 78MS402

**Course Title: Functional Analysis** 

Course	PO 1	PO 2	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10	PO11	PO 12	PSO 1	PSO 2	PSO 3	PSO 4
Outcome	Adv anc ed Ma the ma tica I Kno wle dge	Pr ob le m- sol vin g Ski Ils	Research Abilities	Qua ntita tive Anal ysis	Teachi ng and Acade mia	Theo retic al Und ersta ndin g	Comm unicati on Skills	Operat ions Resear ch	Appl icati on in Indu stry	Engine ering and Techno logy	Gove rnme nt and Publi c Sect or	Co ns ulti ng	Understan d the mathemat ical concepts and applicatio ns in the field of algebra	Han dle the adv anc ed tec hni que s	Develo p necess ary skills and expert ise in the field of resear ch	Creates Mathe matical Models
CO1- 78MS402.1 Understand the importance of Normed Linear spaces and Banach spaces	3	2	2	2	1	2	1	1	2	1	1	1	2	2	1	
CO2- 78MS402.2 Determine the Fundamenta I theorems on Normed linear space	2	3	1	1	1	1	2	1	1	1	1	1	1	2	2	
CO3- 78MS402.3 Demonstrat e an understandi	3	3	1	1	1	1	3	2	2	1	2	2	1	<u>2</u>	<u>3</u>	



ng of the Applications of Normed linear space																
CO4- 78MS402 .4 Define and recogniz e the Hilbert Spaces	2	3	1	2	3	2	3	1	1	2	1	2	2	1	1	
CO5- 78MS402 .5 Students will create the concept of aOperato r Theory and Sturm- Liouville System	3	2	3	1	2	1	2	3	1	1	1	1	1	1	1	

Legend: 1 – Low, 2 – Medium, 3 – High



### **Course Curriculum Map:**

POs & PSOs No.	COs No.& Titles	SOs No.	Laborat Instruct (LI)	- I		Self Learning (SL)
PO 1,2,3,4,5,6 7,8,9,10,11,1 2 PSO 1,2, 3, 4	CO1-78MS402.1 Understand the importance of Normed Linear spaces and Banach spaces.	SO1.1 SO1.2 SO1.3 SO1.4		spa spa	it-1.0 Normed Linear ices and Banach ices1.1,1.2,1.3,1.4,1.5,1. i.7,1.8,1.9,1.10,1.11,1.12,	SL1.1
PO 1,2,3,4,5,6 7,8,9,10,11,1 2 PSO 1,2, 3, 4	CO2-78MS402.2 Determine the Fundamental theorems on Normed linear space	SO2.1 SO2.2 SO2.3 So2.4		the spa	it-2 Fundamental orems on Normed linear ice2.1, 2.2, 2.3, ,2.5,2.6,2.7,2.8,2.9,2.10	SL2.1
PO 1,2,3,4,5,6 7,8,9,10,11,1 2 PSO 1,2, 3, 4	CO3-78MS402.3  Demonstrate an understanding of the Applications of Normed linear space	SO3.1 SO3.2 SO3.3 SO3.4		No.	it-3 Applications of rmed linear space , 3.2, 3.3, 3.4, 3.5 5,3.7,3.8,3.9,3.10	SL3.1
PO 1,2,3,4,5,6 7,8,9,10,11,1 2 PSO 1,2, 3, 4	CO4-78MS402.4 Define and recognize the Hilbert Spaces	SO4.1 SO4.2 SO4.3 SO4.4		4.1, 4.7, 4.8,	t-4 Hilbert Spaces , 4.2, 4.3, 4.4, 4.5, 4.6, , ,4.9,4.9,4.10,4.11,4.12,4. 4.14	SL4.1
PO 1,2,3,4,5,6 7,8,9,10,11,1 2 PSO 1,2, 3, 4	CO5-78MS402.5 Students will create the concept of aOperator Theory and Sturm-Liouville System	SO5.1 SO5.2 SO5.3 SO5.4 SO5.5		Stu 5.1	it-5Operator Theory and rm-Liouville System , 5.2, 5.3, 5.4, 5.5, 5.6 7,5.8,5.9,5.10,5.11,5.12,5	SL5.1

\*



#### Semester-IV

Course Code: 78MS403

**Course Title :** General Theory of Relativity

**Pre- requisite:** Students should have basic knowledge of group

theory and Mapping

**Rationale:** The objective of the General Theory of Relativity,

developed by Albert Einstein, is to provide a comprehensive and mathematically rigorous description of gravity as a fundamental force in the universe. It aims to explain the behavior of massive objects and the curvature of space time

in the presence of matter and energy.

#### **Course Outcome:**

- **78MS403.1** Understanding of Einstein's Field Equations.
- **78MS403.2** Understanding of the concept of tensor calculus, which is essential for expressing and manipulating the equations of General Relativity.
- **78MS403.3** Students should gain insights into the properties of black holes, their formation, and their role in the universe.
- **78MS403.4** Understanding of the concept of gravitational waves, their detection, and their significance as a powerful tool to study astrophysical phenomena.
- **78MS403.5** Understanding of the concepts, principles, and mathematical framework of the General Theory of Relativity.

### **Scheme of Studies:**

Board of Study	Course Code	Course Title	Scheme of studies (Hours/Week)					Total Credi
Study	Code		CI	LI	SW	SL	Total Study Hours (CI+LI+SW+SL)	ts (C)
Program Elective Core (PEC)	78MS403	General Theory of Relativity	4[3+1]	0	1	1	6	4



#### Legend:

**CI:** Classroom Instruction (Includes different instructional strategies i.e. Lecture (L) and Tutorial (T) and others),

LI: Laboratory Instruction (Includes Practical performances in laboratory workshop, field or other locations using different instructional strategies)

**SW:** Sessional Work (includes assignment, seminar, mini project etc.)

SL: Self Learning,

C:Credits.

**Note:** SW & SL has to be planned and performed under the continuous guidance and feedback of teacher to ensure outcome of Learning.

#### **Scheme of Assessment:**

### Theory

Boar	Couse	Course Title		Schem	e of Asses	sment ( M	arks )			
d of Stud	Code		Progr	Progressive Assessment ( PRA ) End					Semest	Total Mark
У									er Assess	s (PRA
									ment (ESA)	+ ESA)
			Class/Ho me Assignme nt 5 number 3 marks each ( CA)	Class Test 2 (2 best out of 3) 10 marks each (CT)	Semin ar one ( SA)	Class Activity any one (CAT)	Class Attend ance (AT)	Total Marks (CA+CT+ SA + CAT+AT)		
Prog ram Elect	78MS40 3	General Theory of Relativity	15	20	5	5	5	50	50	100
ive Core (PEC)										



### **Course-Curriculum Detailing:**

This course syllabus illustrates the expected learning achievements, both at the course and session levels, which students are anticipated to accomplish through various modes of instruction including Classroom Instruction (CI), Laboratory Instruction (LI), Sessional Work (SW), and Self Learning (SL). As the course progresses, students should showcase their mastery of Session Outcomes (SOs), culminating in the overall achievement of Course Outcomes (COs) upon the course's conclusion.

**78MS403.1** Understanding of Einstein's Field Equations.

Item	AppX Hrs
Cl	15
LI	0
SW	1
SL	1
Total	17

Session Outcomes (SOs)	Laboratory Instruction (LI)	Class roor (CI)	n Instruction	Self Learning (SL)
SO1.1	(2.7)	Unit-1 T	ensor	SL.1
understand the Coordinate			ansformation of	Transformation of
system and its dimension		coordi		coordinates
			immation Convention	SL.2
SO1.2			onecker Delta	Kronecker delta
understand the difference	_		ensor: definition	
between vector and tensor		<b>1.5</b> A	gebra of tensors :	SL.3
			on, Subtraction and	Outer product and
SO1.3		Multiplication		contraction
understand the law of		<b>1.6</b> Ty	pes of Tensors	
Transformation		<b>1.7</b> R	ank of tensors	
SO1.4		<b>1.8</b> Tu	ıtorials-I	
understand the properties		<b>1.9</b> Ir	nner product of two	
of tensor		vector	S	
SO1.5		<b>1.10</b> Ft	ındamental tensor	
understand the properties		<b>1.11</b> C	uotient law of tensors	
of Christoffel's Symbols		<b>1.12</b> C	hristoffel's Symbols	
		<b>1.13</b> Pr	operties of Christoffel's	



Symbols	
<b>1.14</b> Law of transformation	
for Christoffel's Symbols.	
1.15 Tutorial-II	

### SW-1 Suggested Sessional Work (SW):

### a. Assignments:

Kronecker Delta, Tensor, Types of Tensors, Rank of tensors, Inner product of two vectors, Fundamental tensor, Quotient law of tensors, Christoffel's Symbols

### b. Mini Project:

Oral presentation

### **c.** Other Activities (Specify):

Quiz, Class Test.

**78MS403.2** Understanding of the concept of tensor calculus, which is essential for expressing and manipulating the equations of General Relativity.

Item	AppX Hrs
Cl	14
LI	0
SW	1
SL	1
Total	16

Session Outcomes (SOs)	Labora tory Instruc tion (LI)	Class room Instruction (CI)	Self Learning (SL)
SO2.1		Unit-2.0 Covariant	SL.1
Understand the Covariant		Differentiation	learn to find the
Differentiation		2.1 Covariant Differentiation	covariant derivative
		2.2 Covariant Differentiation	of vectors
SO2.2		of a tensor of rank one	
Understand the rank of tensors		2.3 Covariant Differentiation	SL.2
SO2.3		of a tensor of rank two	Understand the
2.1 Understand the Ricci's		2.4 Gradient of a scalar	application of
Theorem		2.5 Curl of a vector	Divergence, curl and



SO2.4	2.6 Divergence of a vector gr	radient
Understand the concept of	2.7 Ricci's Theorem	
Riemannian Christoffel's curvature	2.8 Riemannian Christoffel's	
tensor	curvature tensor	
SO2.5	:Introduction	
Understand the Bianchi Identities	2.9 Riemannian Christoffel's	
	curvature tensor	
	:Properties	
	2.10 Tutorials-I	
	2.11 Covariant curvature tensor	
	2.12 Properties of Covariant	
	curvature tensor	
	2.13 Bianchi Identities	
	2.14 Tutorials-II	

### SW-2 Suggested Sessional Work (SW):

### a. Assignments:

Covariant Differentiation, Gradient of a scalar, Curl of a vector, Divergence of a vector, Ricci's Theorem, Riemannian Christoffel's curvature tensor, Covariant curvature tensor, Properties of Covariant curvature tensor, Bianchi Identities.

### **b.** Other Activities (Specify):

Quiz, Class Test.

**78MS403.3** Students should gain insights into the properties of black holes, their formation, and their role in the universe.

Item	AppX Hrs
Cl	10
LI	0
SW	1
SL	1
Total	12

Session Outcomes	Laborat	Class room Instruction	Self
(SOs)	ory	(CI)	Learning
	Instructi		(SL)
	on		
	(LI)		



SO3.1	Unit-3.0 Theory of relativity	SL.1
Understand the hypothesis of the	3.1 Review of the special	Understand
theory of relativity	theory of relativity	the concept
SO3.2	3.2 Review of Newtonian	of Einstein's
Understand the hypothesis of	Theory of gravitation	field
Newtonian Theory of gravitation	3.3 Principle of equivalence	equations
SO3.3 Understand Principle of	3.4 General covariance	
equivalence	3.5 Geodesic principle	SL.2
S03.4	3.6 Differential Equation of	Understand
Understand the hypothesis of	Geodesics	the solution
General covariance	3.7 Newtonian approximation	of
S03.5	of relativistic equations of	differential
Understand the application of	motion	equation
Einstein's field equations	3.8 Einstein's field equations :Introduction	
	3.9 derivation of Einstein's	
	field equations	
	3.10 Newtonian approximation	

#### SW-3 Suggested Sessional Work (SW):

#### a. Assignments:

Special theory of relativity, General theory of relativity, Difference between special theory of relativity and General theory of relativity, Newtonian Theory of gravitation, Principle of equivalence, General covariance, Geodesic principle.

Newtonian approximation of relativistic equations of motion. Einstein's field equations and its Newtonian approximation

### b. b. Mini Project:

Oral presentation, Power point presentation

**c.** Other Activities (Specify): Quiz, Class Test.

**78MS403.4** Understanding of the concept of gravitational waves, their detection, and their significance as a powerful tool to study astrophysical phenomena

Item	AppX Hrs			
Cl	10			



LI	0
SW	1
SL	1
Total	12

Session Outcomes (SOs)	Laboratory Instruction	Class room Instruction (CI)	Self Learning (SL)
()	(LI)		
SO4.1		Unit-4.0 General relativity	SL.1
Understand the			learn the properties of
hypothesis of General		4.1 General relativity:Introduction	Christoffel's Symbols
relativity		<b>4.2</b> Christoffel's Symbols of Second	
		kind	SL.2
SO4.2		4.3 Line element	Learn the properties of
Understand the		4.4 Fundamental Tensor	metric tensor
Schwarzschild		<b>4.5</b> Schwarzschild external solution-	
external solution		part I	
		<b>4.6</b> Schwarzschild external solution-	
SO4.3		part II	
Understand The		4.7 Isotropic form	
Kepler's Laws		4.8 Planetary orbits	
·		<b>4.9</b> Anologues of Kepler's Laws in	
		general relativity	
		<b>4.10</b> Advance of perihelion of a	
		planet.	

### SW-4 Suggested Sessional Work (SW):

### a. Assignments:

Schwarzschild external solution and its isotropic form. Planetary orbits and anologues of Kepler's Laws in general relativity. Advance of perihelion of a planet.

### b. Mini Project:

Oral presentation

**c.** Other Activities (Specify):

Quiz, Class Test.

**78MS403.5** Understanding of the concepts, principles, and mathematical framework of the General Theory of Relativity.

, the community	C 110 W10
Item	AppX Hrs
Cl	11



LI	0
SW	1
SL	1
Total	13

Session Outcomes (SOs)	Laboratory Instruction (LI)	Class room Instruction (CI)	Self Learning (SL)
SO5.1		Unit-5.0 Gravitational field	SL.1
Understand the			Knowledge of
concept of		5.1 Bending of light rays in a	gravitational
gravitational field		gravitational field	Force
		5.2 Gravitational redshift	
SO5.2		5.3 Gravitational redshift of	SL.2
Understand the role of		spectral lines	Knowledge of
Energy-momentum		5.4 Radar echo-delay	gravitational red
tensor		5.5 Energy-momentum tensor	shift
		5.6 Energy-momentum tensor of a perfect fluid	
SO5.3		5.7 Schwarzschild internal	
Understand the		solution-Part-I	
calculation of		5.8 Schwarzschild internal	
Schwarzschild internal		solution-Part-II	
solution		5.9 Boundary conditions	
		5.10 Electromagnetic field	
		5.11 Energy-Momentum tensor of	
		an electromagnetic field	

### SW-5 Suggested Sessional Work (SW):

### a. Assignments:

Bending of light rays in a gravitational field. Gravitational redshift ,Spectral lines. nergy-momentum tensor of a perfect fluid. Schwarzschild internal solution. Boundary conditions. Energy-Momentum tensor of an electromagnetic field.

**b.** Other Activities (Specify): Quiz, Class Test.



### **Brief of Hours suggested for the Course Outcome**

Course Outcomes	Class Lecture (CI)	Sessional Work (SW)	Self Learning (SI)	Total hour (Cl+SW+SI)
78MS403.1 Understanding of Einstein's Field Equations.	15	1	1	17
78MS403.2 Understanding of the concept of tensor calculus, which is essential for expressing and manipulating the equations of General Relativity.	14	1	1	16
78MS403.3 Students should gain insights into the properties of black holes, their formation, and their role in the universe.	10	1	1	12
78MS403.4 Understanding of the concept of gravitational waves, their detection, and their significance as a powerful tool to study astrophysical phenomena.	10	1	1	12
78MS403.5 Understanding of the concepts, principles and mathematical framework of the General Theory of Relativity.	11	1	1	13
Total Hours	60	5	5	70



### **Suggestion for End Semester Assessment**

Suggested Specification Table (For ESA)

СО	Unit Titles	Marks D	n	Total Marks	
		R	U	Α	
CO-1	Tensor	05	05	05	15
CO-2	Covariant Differentiation	05	05	05	15
CO-3	Theory of Relativity	03	01	02	06
CO-4	General Relativity	03	03	02	08
CO-5	Gravitational Field	03	01	02	06
	Total	25	17	08	50

Legend: R: Remember, U: Understand, A: Apply

The end of semester assessment for Introduction to Portland cement will be held with written examination of 50 marks

**Note**. Detailed Assessment rubric need to be prepared by the course wise teachers for above tasks. Teachers can also design different tasks as per requirement, for end semester assessment.

### **Suggested Instructional/Implementation Strategies**

- 1. Improved Lecture
- 2. Tutorial
- 3. Presentation
- 4. Group Discussion
- 5. Online sources
- 6. Seminar
- 7. Workshop

### **Suggested Learning Resources:**

a) Books:



S.	Title	Author	Publisher	Edition & Year
N				
0.				100=
1	Theory of Relativity	S.R.Roy and Raj Bali	Jaipur Publishing House,Jaipur	1987
2	General Relativity and Cosmology	S. K. Shrivastva	PHI, NewDelhi.	-
3	General Relativity and Cosmology	J.V. Narlikar	The Macmillan Company of India Limited	1978
4	Introducing Einstein's Relativity	Ray A. d'Inverno	Oxford University Press, In print, ISBN 0-19-859686-3.	1992
5	Tensor Calculus and Riemannian Geometry	J.K. Goyal &K.P.Gupta	Pragati Prakasan	1972

### b) Reference Books:

S. N	Title	Author	Publisher	Edition & Year
0.				
1	Relativity Thermodynamics and Cosmology,	Tolman Richard C.	The Clarendon Press, Oxford, London	(Hindi)1934
2	Mathematical theory of relativity,	A.S.Edington,	Cambridge At The University Press	1923
3	Gravitation and Cosmology: Principles and Applications of the General Theory of Relativity.	Steven Weinberg,	Wiley	Ist Eition,1972



4	Einstein's general theory of relativity, sigbom Hervik,	Øyvind GrØn	Springer science &Business Media.	2007
5	An Introduction to cosmology	Jayant,V.Narlik ar	Cambridge University Press	2010

### c) Suggetsed Digital Platform Web links:

Suggested	1.http://www.gutenberg.org/ebooks/5001
Digital	
Platforms	2.https://www.googleadservices.com/pagead/aclk?sa=L&ai=DChcSEwiwofuE7v
Web links:	-EAxVdwUwCHZS-
	B20YABAAGgJ0bQ&ase=2&gclid=EAIaIQobChMIsKH7hO7_hAMVXcFMAh
	2UvgdtEAMYASAAEgJHtfD BwE&ohost=www.google.com&cid=CAASJeRo
	xBtCkX3PcVWlqe9GzlNxcQJNYrgF9vbHAHKw7kFLxnrh7M&sig=AOD64_3
	XX3ZyfwFLiVnLoibj5kLQmz7Bzg&q⋼=4&adurl&ved=2ahUKEwib6fWE7
	v-EAxWMr1YBHdA-AzkQ0Qx6BAgJEAE
	3. https://www.freebookcentre.net/Physics/Relativity-Books-Download.html

### **Curriculum Development Team**

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### **Cos, POs and PSOs Mapping**

**Course Title: M.Sc. Mathematics** 

Course Code: 78MS403

**Course Title: General Theory of Relativity** 

	PO	PO2	РО	PO4	PO5	PO6	PO7	PO8	PO9	PO10	PO1	PO12	PSO	PSO 2	PSO	PSO
	1		3								1		1		3	4
Course	Ad	Probl	Res	Qua	Teachi	Theo	Comm	Operat	Applic	Engine	Gov	Consul	Unde	Handle	Dev	Crea
Outcome	van ced	em- solvi	ear ch	ntita tive	ng and Acade	retic al	unicati on	ions Resear	ation in	ering and	ern men	ting	rstan d the	the advanced	elop nece	tes Mat
Outcome	Ma	ng	Abi	Anal	mia	Und	Skills	ch	Industr	Techn	t		math	technique	ssar	hem
	the	Skills	liti	ysis		ersta			У	ology	and		emati	S	y	atical
	ma tica		es			ndin g					Publi c		cal conc		skills and	Mod els
	1										Sect		epts		expe	
	Kn owl										or		and		rtise in	
	ed												appli catio		the	
	ge												ns in		field	
													the field		of rese	
													of		arch	
													algeb			
													ra			
78MS403.1	2	3	1	2	1	2	2	2	1	1	1	1	<u>2</u>	<u>1</u>	<u>1</u>	<u>3</u>
Understandin																
g of Einstein's																
Field																
Equations.																
78MS403.2	1	3	2	1	1	1	1	1	1	2	3	1	<u>3</u>	<u>1</u>	1	2
Understandi																
ng of the																
concept of																
tensor																
calculus,																
which is																
essential for																
expressing																
and																
manipulating																
the																
equations of																
General																



### AKS University Faculty of Basic Science Department of Mathematics

### **Curriculum & Syllabus of M.Sc. Mathematics program**

Relativity.																
78MS403.3		3	2	2	1	1	3	2	1	1	3	1	2	1	2	2
Students should gain																
insights into																
the properties																
of black holes,																
their																
formation,																
and their role in the																
universe.																
78MS403.4	2	3	2	2	1	1	3	2	1	1	3	1	<u>2</u>	<u>1</u>	2	2
Understandin										_			_	_	_	
g of the																
concept of																
gravitational																
waves, their																
detection, and																
their																
significance as																
a powerful																
tool to study																
astrophysical																
phenomena.																
78MS403.5	2	3	2	2	1	1	3	2	1	1	3	1	<u>2</u>	<u>1</u>	<u>2</u>	3
Understandin																
g of the																
concepts,																
principles and																
mathematical																
framework of																
the General																
Theory of																
Relativity.																

Legend: 1 – Low, 2 – Medium, 3 – High



### **Course Curriculum Map:**

POs & PSOs No.	COs No.& Titles	SOs No.	Laboratory Instruction( LI)	Classroom Instruction (CI)	Self Learning (SL)
PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2, 3, 4 PO 1,2,3,4,5,6 7,8,9,10,11,12	78MS403.1 Understanding of Einstein's Field Equations.  78MS403.2 Understanding of the concept of	SO1.1 SO1.2 SO1.3 SO1.4 SO1.5 SO1.1		Unit-1.0 Group 1.1,1.2,1.3,1.4,1.5,1.6,1. 7,1.8,1.9,1.10, 1.11,1.12,1.13,1.14,1.15  Unit-2 Ring 2.1, 2.2, 2.3, 2.4, 2.5, 2.6,	SL1.1 SL1.2 SL1.3 SL2.1 SL2.2
PSO 1,2, 3, 4	tensor calculus, which is essential for expressing and manipulating the equations of General Relativity.	SO1.3 SO1.4 SO1.5		2.7, 2.8,2.9,2.10, 1.11,1.12,1.13,1.14	
PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2, 3, 4	78MS403.3 Students should gain insights into the properties of black holes, their formation, and their role in the universe.	SO1.1 SO1.2 SO1.3 SO1.4 SO1.5		Unit-3 2.1, 2.2, 2.3, 2.4, 2.5, 2.6, 2.7, 2.8,2.9,2.10	SL3.1 SL3.2
PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2, 3, 4	78MS403.4 Understanding of the concept of gravitational waves, their detection, and their significance as a powerful tool to study astrophysical phenomena.	SO1.1 SO1.2 SO1.3		Unit-4 2.1, 2.2, 2.3, 2.4, 2.5, 2.6, 2.7, 2.8,2.9,2.10	SL4.1 SL4.2
PO 1,2,3,4,5,6 7,8,9,10,11,12	78MS403.5	SO1.1 SO1.2		Unit-5 2.1, 2.2, 2.3, 2.4, 2.5, 2.6,	SL5.1 SL5.2



PSO 1,2, 3, 4	Understanding of the	SO1.3	2.7, 2.8,2.9,2.10,2.11	
	concepts, principles			
	and mathematical			
	framework of the			
	General Theory of			
	Relativity.			

\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*



#### Semester-IV

Course Code: 78MS404

Course Title: Jacobi Polynomial and H-Function

**Pre-requisite:** Higher knowledge of mathematics.

Rationale: Theaimofthecourseistointroducetothefieldofmathematicswithem

phasis on its use to solve real world problems for which solutions are difficult to the control of the contro

culttoexpressusingthe different methods.

It explores the essential theory behind methods for developing system sthat demonstrate in telligent behavior including dealing with uncertainty and the state of the state

nty, learning from experience and following problem-solving

strategies founding nature.

### **Course Outcomes:**

- **CO-78MS404.1:**Understanding of special functions and their importance in various mathematical and physical applications.
- **CO-78MS404.2:**Using Jacobi polynomials as a basis and apply them to various mathematical and physical problems.
- **CO-78MS404.3:**Understand the concept of applied in manipulating and solving problems involving the H-function.
- **CO-78MS404.4:**Understand the concept of integral transforms, specifically the H-transform, and its use in solving integral equations.
- **CO-78MS404.5:**Understanding of fractional calculus and its importance in modeling complex systems with fractional derivatives and integral.



#### **Scheme of Studies**

Board of Study	Course		Course				me of ies(Hours <i>)</i>	/Week)	Total Credits(C
	Code	Title	CI	LI	SW	SL	Total Study Hours(CI+LI+S W+SL)	)	
Program	78MS404		4	0	1	1	6	6	
Elective		Polynomial							
Course		and H-							
(PEC)		Function							

#### Legend:

CI: Class room Instruction (Includes different instructional strategies i.e. Lecture (L) and Tutorial (T) and others),

**LI:**LaboratoryInstruction(IncludesPracticalperformancesinlaboratoryworkshop,fiel dorotherlocationsusingdifferentinstructionalstrategies)

**SW:**SessionalWork(includesassignment,seminar,miniprojectetc.),

SL:SelfLearning,

C: Credits.

#### Note:

SW&SL has to be planned and performed under the continuous guidance and feedback of teacher to ensure outcome of Learning.

### **Scheme of Assessment:**

### Theory

				Scheme o	f Asses	sment (M	arks )			
					_	essiveAss ent(PRA)	e		EndSe mest	
Board of Study	Cou rse	Cours eTitle	Class/H omeAss ignmen t5numb er 3 mar kse ach (CA)	Class Test2 (2best out of3)10 marks each( CT)	Sem inar one (SA)	Class Activity anyone (CAT)	ClassAt tendan ce (AT)	TotalMarks (CA+CT+SA+CAT+AT)	erAss essm ent	Tota IMar ks (PR A+E SA)
Ü	78MS 404	Jacobi Polyn omial and H- Functi on	1 5	20	5	5	5	50	5 0	100



### **Course-CurriculumDetailing:**

This course syllabus illustrates the expected learning achievements, both at the course and sessionlevels, which students are anticipated to accomplish through various modes of instruction includingClassroom Instruction (CI), Laboratory Instruction (LI), Sessional Work (SW), and Self-Learning (SL). Asthecourseprogresses, students should show case their mastery of Session Outcomes (SOs), culminating in the overall achievement of Course Outcomes (COs) upon the course's conclusion.

**CO-78MS404.1:**Understanding of special functions and their importance in various mathematical and physical applications.

, the community is					
Item	AppXHrs				
Cl	12				
LI	0				
SW	2				
SL	1				
Total	15				

SessionOutco	LaboratoryInstructi	ClassroomInstruct	Self-
mes	on	ion	Learning
(SOs)	(LI)	(CI)	(SL)
SO1.1 Understand the concept of Jacobi polynomial  SO1.2 Understand the concept of special function	·	Unit-1.0 Jacobi polynomial  1.1 Introduction 1.2 Recurrence relation 1.3 Examples of recurrence relation 1.4 Rodrigue's formula 1.5 Examples of Rodrigues formula 1.6 Generating functions 1.7 Examples of generating function 1.8 Orthogonal	1. Write s speci al functi ons and their impor tance



properties
1.9 Expansions of
polynomials.
1.10 Uses of
recurrence
relation.
1.11 Uses of
properties
1.12 Solve
polynomials

SW-1SuggestedSessionalWork(SW):

### **Assignments:**

- i. Numerical based on Jacobi polynomial.
- ii. Numerical based on recurrence relation
- iii. Solve related example generating function

**CO-78MS404.2:**Using Jacobi polynomials as a basis and apply them to various mathematical and physical problems.

Item	AppXHrs
Cl	12
LI	0
SW	2
SL	1
Total	15

SessionOutc		LaboratoryInstruc	ClassroomInstruc	Self-	
	omes	tion	tion	Learning	
	(SOs)	(LI)	(CI)	(SL)	



### Faculty of Basic Science Department of Mathematics

### Curriculum & Syllabus of M.Sc. Mathematics program

SO2.1 Understand the	. Unit-2.0 H	1. Writes
concept variable	Functionon one	exampl
	variable	es of
SO2.2Understand the		one
concept of	2.1. Definition and	variable
Differentiation	notation.	
	2.2. Related	2. Solve
	examples	Partial
	2.3. Differentiation	derivati veswith
	formulas	exampl
	2.4. Related	es.
	examples	
	2.5. Partial	
	derivatives	
	2.6. Examples of	
	partial	
	derivatives	
	2.7. Parameters	
	2.8. Parameter	
	related	
	examples	
	2.9. Expansion	
	formula	
	2.10. Solve partial	
	differential	
	2.11. Uses of	
	parameters	
	2.12. Solve	
	expansion	
	formula	

SW-1SuggestedSessionalWork(SW):

### **Assignments:**

- iv. Numerical based differentiationFunction.
- v. Numerical based on partial derivatives.
- vi. Examples of expansion formula.

**CO-78MS404.3:**Understand the concept of applied in manipulating and solving problems involving the H-function.



Item	AppXHrs
Cl	12
LI	0
SW	2
SL	1
Total	15

SessionOutc	LaboratoryInstruc	ClassroomInstru	Self-
omes	tion	ction	Learn
(SOs)	(LI)	(CI)	ing
			(
			S
			L
			)
<b>SO3.1</b> Understand the	•	Unit-3.0 The H Functions	1. Writes
concept of partial		of two variables	example
two variables		3.1. Definition and	s of two
		notation.	variable
<b>SO3.2</b> Usesof properties and		3.2. Related examples	S
functions		3.3. Examples of two	2. Writes
		variables,	example
		3.4. elementary	s of
		properties	special
		3.5. Related examples of	cases.
		elementary	
		properties	
		3.6. Uses of elementary	
		properties	
		3.7. Special cases	
		3.8. Examples of special	
		cases	
		3.9. Uses of special cases	
		3.10. Definitions	
		3.11. Elementary	
		examples	
		3.12. Two variables	
		examples	
		'	
		1	



SW-1SuggestedSessionalWork(SW):

### Assignments:

- vii. Numerical based on two variables.
- viii. Numerical based on elementary properties
- ix. Writes related examples special cases.

**CO101.4:**Understand the concept of integral transforms, specifically the H-transform, and its use in solving integral equations.

111	
Item	AppXHrs
Cl	12
LI	0
SW	2
SL	1
Total	15

SessionOutc	LaboratoryIn	ClassroomInstruction		Self-
omes	struction	(CI)		Learn
(SOs)	(LI)			ing
				(
				S
				L
				)
<b>SO4.1</b> Understand the	•	<b>Unit-4.0</b> Finite Summation	1.	H-
concept of H-		formulas		Function
Functions		4.1. H- Functions of two		s of two
		variables		variables
SO4.2Application of H-		4.2. Examples of H- function		
Functions		4.3. Derivatives		
<b>SO4.3</b> How to learn one and		4.4. Related examples of		
two variable on H-		derivatives		
Functions		4.5. Examples of H- Functions		
		of two variables		
		4.6. Contiguous relations		
		4.7. Example of contiguous		
		relation		
		4.8. Total Count of		
		recurrences.		
		4.9. Example of Total Count		
		of recurrences.		
		4.10. Basic H function		
		4.11. Derivation examples		
		4.12. Examples of H		
		functions		



SW-1SuggestedSessionalWork(SW):

### **Assignments:**

- i. Questions based on H- Functions.
- ii. Questions based on Count of recurrences.
- iii. Questions based on one and two variables.

**CO-78MS404.5:**Understanding of fractional calculus and its importance in modeling complex systems with fractional derivatives and integrals. **ApproximateHours** 

Item	AppXHrs
Cl	12
LI	00
SW	02
SL	01
Total	15

SessionOutc omes	LaboratoryInstruc tion	ClassroomInstru ction	Self- Learn
(SOs)	(LI)	(CI)	ing
			(
			S
			L
<b>SO5.1</b> Understand the		Unit-5.0 Method and	1. Method
	•	schemes	
concept of finite and infinite series		5.1. Writes different	for obtainin
illillite selles		methods	
<b>SO5.2</b> uses some method		5.2. sum of finite series.	g sum of finite or
to solve the		5.3. sum of infinite	infinite
		series.	series.
examples.			series.
		5.4. Examples of finite series	
		5.5. Uses of finite and	
		infinite deries	
		5.6. Example of infinite	
		series	
		5.7. Double summation	
		formulas	
		5.8. Uses of summation	
		formula	
		5.9. Example of double	
		summation formula	
		5.10. Uses of finite	



	series 5.11. Uses of infinite series 5.12. Uses of Double summation	



SW-1 Suggested Sessional Work (SW):

### **Assignments:**

- i. Different types of methods
- ii. Writes Examples of finite and infinite series.

### **Brief of Hours suggested for the Course Outcome:**

CourseOutcomes	ClassLecture (CI)	SessionalWork (SW)	Self- Learning (SI)	Total hour(Cl+SW+SI)
D1-78MS404.1: nderstanding of special functions and their importance in various mathematical and physical applications.	12	02	01	15
D2-78MS404.2:Using Jacobi polynomials as a basis and apply them to various mathematical and physical problems	12	02	01	15
D3-78MS404.3:  nderstand the concept of applied in manipulating and solving problems involving the H-function.	12	02	01	15
D4-78MS4044: nderstand the concept of integral transforms, specifically the H- transform, and its use in solving integral equations.	12	02	01	15
D4-78MS404.5: nderstanding of fractional calculus and its importance in modeling complex systems with	12	02	01	15



fractional derivatives and integrals.				
TotalHours	60	10	5	75

#### SuggestionforEndSemesterAssessment

SuggestedSpecificationTable(ForESA)

СО	UnitTitles	MarksDistribution		TotalMark	
		R	U	Α	s
CO-1	Jacobi polynomial	03	02	03	08
CO-2	The H Functions of one variables	03	01	05	09
CO-3	The H Functions of two variables	03	07	02	12
CO-4	Finite Summation formulas	03	05	05	13
CO-5	Method and schemes	03	02	03	08
	Total	15	17	18	50

Legend: R:Remember, U:Understand, A:Apply

 $The end of semester assessment for Introduction to Portland cement will be held with written examination of 50\ marks$ 

 $\label{lem:note} \textbf{Note}. Detailed Assessment rubric need to be prepared by the course wise teachers for above tasks. \\ Teachers can also design different tasks as per requirement, for end semester assessment. \\$ 

### SuggestedInstructional/ImplementationStrategies:

1. ImprovedLecture



- 2. Tutorial
- 3. CaseMethod
- 4. GroupDiscussion
- 5. RolePlay
- 6. Visittocementplant
- 7. Demonstration
- 8. ICTBasedTeachingLearning(VideoDemonstration/T utorialsCBT,Blog,Facebook, Twitter, WhatsApp,Mobile,Onlinesources)
- 9. Brainstorming

#### **Suggested Learning Resources:**

#### A. Books:

S. No.	Title	Author	Publisher	Edition &Year
1	Special Functions	Rainville. E.D.	The Macmillan Co. New. York.	1971
2	The H- Functions of One and Two Variables with applications.	Shrivastava. H.M., Gupta K.C. and Goyal. S.P.	South Asian Publication New Delhi	-
3	The H-Function: Theory and Applications	A.M. Mathai and R.K. Saxena.	-	-
4	Special functions and Their Applications.	Lebdev. N.N.	Prentice Hall. Englewood Hall phase new Jersy USA	1965

#### **Curriculum Development Team**

- 1. Dr. Sudha Agrawal, HOD, Department of Mathematics.
- 2. Dr. Ekta Shrivastava, Assistant Professor, Department of Mathematics.
- 3. Mr. Neelkanth Napit, Assistant Professor, Department of Mathematics.
- 4. Mrs. Vandana Soni, Assistant Professor, Department of Mathematics.
- 5. Mr. Radhakrishna Shukla, Assistant Professor, Department of Mathematics.
- 6. Mr. Ghanhyam sen, Assistant Professor, Department of Mathematics.
- 7. Ms. Pushpa Kushwaha, Assistant Professor, Department of Mathematics.



### CO, PO and PSO Mapping

CourseTitle:M.Sc. Mathematics

Course Code: -78MS404

Course Title: Jacobi Polynomial and H-Function

						Progra	m Outcom	nes					Program Specific Outcomes			
	PO1	PO2	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10	PO11	PO12	PSO1	PSO2	PSO3	PSO4
Course Outcomes	Advan ced Math emati cal Knowl edge	Probl em- solvin g Skills	Resea rch Abiliti es	Quant itative Analy sis	Teach ing and Acade mia	Theor etical Under standi ng	Com munic ation Skills	Opera tions Resea rch	Applic ation in Indust ry	Enginee ring and Technol ogy	Govern ment and Public Sector	Consult ing	Underst and the mathe matical concept s and applicat ions in the field of algebra	Handle the advanc ed techniq ues	Develo p necessa ry skills and expertis e in the field of researc h	Creates Mathe matical Models
co1:Unders tanding of special functions and their importance in various mathematic al and physical applications	3	2	2	2	2	1	1	1	1	1	1	3	2	2	3	3
CO2:Using Jacobi polynomials as a basis and apply them to various mathematic al and physical problems	2	3	3	2	2	2	1	1	1	1	1	3	2	3	2	3



#### Curriculum & Syllabus of M.Sc. Mathematics program

CO3:Unders tand the concept of applied in manipulatin g and solving problems involving the H- function.	3	2	3	3	2	2	1	1	1	1	1	3	2	2	2	3
co4:Unders tand the concept of integral transforms, specifically the H-transform, and its use in solving integral equations.	3	3	3	2	2	2	1	1	1	1	1	3	2	2	3	2
CO5: Understand ing of fractional calculus and its importance in modeling complex systems with fractional derivatives and integrals.	3	2	3	2	2	2	1	1	1	1	1	3	2	2	3	2



### **Course Curriculum Map:**

POs&PSOsN o.	COsNo.&Titles	SOsNo	Laborato ryInstruc tion(LI)	Classroom Instruction(CI)	SelfLearnin g(SL)
PO: 1,2,3,4,5,6,7, 8,9,10,11,12 PSO: 1,2,3,4	CO1:Understanding of special functions and their importance in various mathematical and physical applications.	SO1.1 SO1.2		Unit-1.0 Jacobi polynomial 1.1,1.2,1.3,1.4,1.5,1.6,1.7,1 .8,1.9,1.10,1.11,1.12	
PO: 1,2,3,4,5,6,7, 8,9,10,11,12 PSO: 1,2,3,4	CO2:Using Jacobi polynomials as a basis and apply them to various mathematical and physical problems	SO2.1		Unit-2The H Functions of one variables	
		SO2.2		2.1,2.2,2.3,2.4,2.5,2.6,2.7, 2.8,2.9,2.10,2.11,2.12	
PO: 1,2,3,4,5,6,7, 8,9,10,11,12	CO3:Understand the concept of applied in manipulating and solving problems	SO3.1 SO3.2		Unit-3 : The H Functions of two variables	



#### Curriculum & Syllabus of M.Sc. Mathematics program

PSO: 1,2,3,4	involving the H- function.	SO3.3	3.1,3.2,3.3,3.4,3.5,3.6,3.7,3 .8,3.9,3.10,3.11,3.12
PO: 1,2,3,4,5,6,7, 8,9,10,11,12 PSO: 1,2,3,4	CO4:Understand the concept of integral transforms, specifically the H-transform, and its use in solving integral equations.	SO4.1 SO4.2 SO4.3	Unit-4: Finite Summation formulas 4.1,4.2,4.3,4.4,4.5,4.6,4. 7,4.8,4.9,4.10,4 .11,4.12
PO: 1,2,3,4,5,6,7, 8,9,10,11,12 PSO: 1,2,3,4	CO5: Understanding of fractional calculus and its importance in modeling complex systems with fractional derivatives and integrals.	SO5.1 SO5.2	Unit5:Method and schemes5.1,5.2 ,5.3,5.4,5.5,5.6, 5.7,5.8,5.9,5.10 ,5.11,5.12

\*\*\*\*\*\*\*\*\*\*\*



#### Semester-IV

Course Code: 78MS405

Course Title: ADVANCED MATHEMATICAL STATISTIC

Pre- requisite: Students should have basic knowledge of

calculus, linear algebra, and ODE theory.

Rationale: Advanced mathematical statistics

provides a deeper understanding of statistical inference, which involves drawing conclusions about populations based on sample data. It explores the theoretical foundations of estimation and hypothesis testing, enabling practitioners to make more informed and rigorous

statistical inferences.

#### **Course Outcome:**

- **CO1-.78MS405.1** Learn the statistical methods to describe the central or typical value in a set of data to have clear understanding of the concept of central tendency and its importance in summarizing data.
- **CO2-78MS405.2**. To understand the concepts in probability theory and the probability distributions associated with various random variables foundational knowledge and skills.
- **CO3-78MS405.3**. Theory of Estimators typically covers the mathematical foundations and principles behind statistical estimation to develop a clear understanding of the fundamental concepts of statistical estimation, including point estimation and interval estimation.
- **CO4-78MS405.4 To** understanding and applying exact methods for generating and studying sampling distributions, Learn and apply exact sampling methods, which may include techniques such as Monte Carlo simulation, bootstrapping, permutation tests, or other re-sampling methods.
- **CO5-78MS405.5** Analysis of Variance (ANOVA) typically covers the statistical methods used to analyze differences among group means in a dataset to develop a solid understanding of the



fundamental concepts of Analysis of Variance, including the partitioning of variance and the comparison of group means.

#### **Scheme of Studies:**

Board of Study	Course Code	Course Title	CI LI SW SL Total Study Hours (CI+LI+SW+SL)					Total Credit
Study		THE						s (C)
Program Elective Course	78MS405	ADVANCED MATHEMA TICAL	4[3+1]	0	1	1	6	4
(PEC)		STATISTIC						

#### Legend:

**CI:** Classroom Instruction (Includes different instructional strategies i.e. Lecture (L) and Tutorial (T) and others),

**LI:** Laboratory Instruction (Includes Practical performances in laboratory workshop, field or other locations using different instructional strategies)

SW: Sessional Work (includes assignment, seminar, mini project etc.),

SL: Self Learning,

C:Credits.

**Note:** SW & SL has to be planned and performed under the continuous guidance and feedback of teacher to ensure outcome of Learning.

#### Scheme of Assessment:

#### Theory

Board of	Couse	Course Title	Scheme of Assessment ( Marks )							
Study	Code		Progressive Assessment ( PRA )						End Semester Assessm ent (ESA)	Total Marks (PRA+ ESA)
			Class/Home Assignment 5 number 3 marks each (CA)	Class Test 2 (2 best out of 3)10 marks each (CT)	Semi nar one (SA)	Class Activity any one (CAT)	Class Attend ance (AT)	Total Marks (CA+CT+SA +CAT+AT)		
Program Elective Course (PEC)	78MS4 05	ADVANCD MATHEMATI CAL STATISTIC	15	20	5	5	5	50	50	100



#### **Course-Curriculum Detailing:**

This course syllabus illustrates the expected learning achievements, both at the course and session levels, which students are anticipated to accomplish through various modes of instruction including Classroom Instruction (CI), Laboratory Instruction (LI), Sessional Work (SW), and Self Learning (SL). As the course progresses, students should showcase their mastery of Session Outcomes (SOs), culminating in the overall achievement of Course Outcomes (COs) upon the course's conclusion.

**CO1-78MS405.1** Learn the statistical methods to describe the central or typical value in a set of data to have clear understanding of the concept of central tendency and its importance in summarizing data.

Item	AppX Hrs
Cl	12
LI	0
SW	1
SL	2
Total	15

Session Outcomes (SOs)	Laboratory Instruction (LI)	Class room Instruction (CI)	Self Learning (SL)
SO1.1 concept of central tendency in statistics . SO1.2 Differentiate between mean, median, and mode SO1.3 Identify the properties and characteristics of each measure of central tendency So1.4 Calculate	-	Unit-1.0 Central tendencies 1.1 Definitions of central tendencies, 1.2 Calculation of mean 1.3 Calculation of median 1.4 Calculation of mode 1.5 Calculation of mode 1.6 Measure of dispersions with variance in detail,	SL.1 write all formula used in central tendencies SL.2 learn all formula used in correlation and regeneration



and interpret	1.7 Method of least
•	square for curve
percentiles and	•
quartiles in	fitting,
various contexts	<b>1.8</b> Correlation
	concept and
<b>So1.5</b> Use	formula
	1.9 Questions besed on
statistical software	corelation
(e.g., Excel, R,	
Python) to	1.10 Regression
calculate and	concept and
	formula
analyze measures	1.11 Regression Question
of central	based on formula
tendency.	
	1.12 Tutorial

#### SW-1 Suggested Sessional Work (SW):

#### a. Assignments:

- i. write all formula of measure of central tendency.
- ii. Write any 3 Application of mean, median and mode in real life.
- iii. Write any 3 Application of corelation and Regression in real life.
- **b.**Other Activities (Specify):

Class Test.

**CO2-78MS405.2** To understand the concepts in probability theory and the probability distributions associated with various random variables foundational knowledge and skills.

Item	AppX Hrs
Cl	12
LI	0
SW	1
SL	2
Total	15

Session Outcomes	Laboratory Instruction	Class room Instruction	Self Learning
(SOs)	(LI)	(CI)	(SL)



#### Curriculum & Syllabus of M.Sc. Mathematics program

SO2.1 Define and	Unit-2.0 Probability	SL.1
understand random	&Distributions	Write all formula of
variables and their	1.1 Theory of	probability
types	probability &	SL.2
	distributions:	Write and learn all
	various	formula of distribution
SO2.2 Explore the	definitions,	
concept of probability	1.2 additive &	
distributions associated	multiplicative	
with random variables	law,	
	1.3 Bayes'	
SO2.3 Understand the	theorem.	
probability	1.4 Continuous	
density/mass function	variable,	
and cumulative	1.5 Mathematical	
distribution function	expectation,	
SO2.4 Calculate and	1.6 Binomial	
interpret the expected	distribution	
value (mean) and	1.7. Poisson	
variance of random	distribution	
variables	1.8 Normal	
SO2.5 Explore higher	distribution,	
moments of probability	1.9 Rectangular	
distributions	distribution,	
	1.10 Exponential	
	distribution,	
	1.11Moment	
	generation function,	
	1.12marginal &	
	conditional probability	
	distributions &	
	conditional expectation	

#### SW-2 Suggested Sessional Work (SW):

#### a. Assignments:

i. write the application of probability.

#### **b.** Other Activities (Specify):

Presentation



**CO3-78MS405.3** Theory of Estimators typically covers the mathematical foundations and principles behind statistical estimation to develop a clear understanding of the fundamental concepts of statistical estimation, including point estimation and interval estimation.

Item	AppX Hrs
Cl	12
LI	0
SW	1
SL	1
Total	14

Session Outcomes (SOs)	Laboratory Instruction	Class room Instruction (CI)	Self Learning (SL)
	_		•
and maximum likelihood estimation		3.6 Tutorial 1 3.7 maximum likelihood estimators 3.8 Question based on maximum likelihood estimators 3.9 Cramer-Rao inequality 3.10 formula of Cramer-Rao inequality 3.11 questions based on Cramer-	



	Rao inequality	
	3.12 Tutorial 2	

#### **SW-3 Suggested Sessional Work (SW):**

#### a. Assignments:

i. write application of Cramer-Rao inequality

**CO4-78MS405.4 To** understanding and applying exact methods for generating and studying sampling distributions, Learn and apply exact sampling methods, which may include techniques such as Monte Carlo simulation, bootstrapping, permutation tests, or other re-sampling methods.

Item	AppX Hrs
Cl	12
LI	0
SW	1
SL	1
Total	14

Session Outcomes (SOs)	Laboratory Instruction (LI)	Class room Instruction (CI)	Self Learning (SL)
SO4.1 Gain a solid understanding of sampling distributions, including the concept of a sampling distribution and its importance in statistical inference.  SO4.2 Learn and apply exact sampling methods  SO4.3 Develop the ability to make		Unit-4.0 Sampling distributions  4.1 explanation of Exact sampling distributions  4.2 methods of sampling  4.3 t tests formula  4.4 Question based on t tests	SL.1 Learn all testing used in this unit



statistical inferences based on the observed data, considering the uncertainty inherent in the sampling process SO4.4 Apply the knowledge gained to solve real-world problems SO4.5 Problem solving	<ul> <li>4.5 F tests formula</li> <li>4.6 Question based on F tests</li> <li>4.7 Z tests formula</li> <li>4.8 Question based on Z tests</li> <li>4.9 Wilcoxon's signed rank sumtest</li> <li>4.10 Medial test and Mann Whitney</li> <li>4.11 U-test</li> <li>4.12 run test for</li> </ul>	
	randomness	

#### **SW-4 Suggested Sessional Work (SW):**

#### a. Assignments:

i. write a short note on different testing .

**CO5-78MS405.5**. Analysis of Variance (ANOVA) typically covers the statistical methods used to analyze differences among group means in a dataset to develop a solid understanding of the fundamental concepts of Analysis of Variance, including the partitioning of variance and the comparison of group means

<u> </u>	
Item	AppX Hrs
Cl	12
LI	0
SW	1
SL	1
Total	14

Session Outcomes (SOs)	Laboratory Instruction (LI)	Class room Instruction (CI)	Self Learning (SL)
			. ,



SO5.1 Define terms	Unit-5.0	SL.1
such as treatment,	Analysis of variance	Understand one and
factor, level, and error.	5.1 Analysis of	two-way classifications
SO5.2 Learn and apply	variance: one way	
the one-way ANOVA	classifications	
technique for	5.2 two-way	
comparing means	classifications.	
across more than two		
groups	5.3 difference between	
SO5.3 Extend the	one and two-way	
understanding to two-	classifications	
way ANOVA for	5 4 Davis suinciulas of	
studying the effects of	5.4 Basic principles of	
two independent	design: Replication,	
variables	5.5 randomization,	
SO5.4 Explore post hoc tests for identifying	5.6 questions based on	
specific group	randomization,	
differences after	Tundomization,	
detecting a significant	5.7 local control,	
ANOVA result	5.0 law aut and analysis	
	5.8 lay out and analysis	
SO5.5 Apply ANOVA	of completely	
techniques in the context of	randomized,	
experimental designs	5.9 randomized block	
	5 10 1	
	5.10 Latin square	
	design,	
	5.11 missing plot	
	techniques in	
	randomized block	
	5 12 1 - 1 - 1 - 1 - 1	
	5.12 Latin square	
	design.	



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Course Outcomes	Class Lecture (CI)	Sessional Work (SW)	Self Learning (SI)	Total hour (CI+SW+SI)
co1-78MS405.1 Learn the statistical methods to describe the central or typical value in a set of data to have clear understanding of the concept of central tendency and its importance in summarizing data.	12	1	2	15
CO1-78MS405.2 To understand the concepts in probability theory and the probability distributions associated with various random variables foundational knowledge and skills.	12	1	2	15
CO1-78MS405.3 Theory of Estimators typically covers the mathematical foundations and principles behind statistical estimation to develop a clear understanding of the fundamental concepts of statistical estimation, including point estimation and interval estimation.	12	1	1	14
CO1-78MS405.4 To understanding and applying exact methods for generating and studying sampling distributions, Learn and apply exact sampling methods, which may include techniques such as Monte Carlo simulation, bootstrapping, permutation tests, or other re-	12	1	1	14



#### Curriculum & Syllabus of M.Sc. Mathematics program

sampling methods.				
CO1-78MS405.5 Analysis of Variance (ANOVA) typically covers the statistical methods used to analyze differences among group means in a dataset to develop a solid understanding of the fundamental concepts of Analysis of Variance, including the partitioning of variance and the comparison of group means	12	1	1	14
Total Hours	60	5	7	72

#### **Suggestion for End Semester Assessment**

#### Suggested Specification Table (For ESA)

СО	Unit Titles	Marks	Distribu	tion	Total	
		R	U	Α	Marks	
CO-1	Measure of central tendencies	05	04	01	10	
CO-2	Theory of probability & distributions	02	06	02	10	
CO-3	Theory of estimators:	03	05	02	10	
CO-4	Sampling and testi ng	05	03	02	10	
CO-5	Analysis of variance	05	04	01	10	
Total		20	22	08	50	

Legend: R: Remember, U: Understand, A: Apply



The end of semester assessment for Introduction to Portland cement will be held with written examination of 50 marks

**Note**. Detailed Assessment rubric need to be prepared by the course wise teachers for above tasks. Teachers can also design different tasks as per requirement, for end semester assessment.

#### **Suggested Instructional/Implementation Strategies**

- 1. Improved Lecture
- 2. Tutorial
- 3. Presentation
- 4. Group Discussion
- 5. Online sources
- 6 .Seminar
- 7. Workshop

#### **Suggested Learning Resources:**

#### a) Books:

S.	Title	Author	Publisher	Edition & Year
N				
0.				
1	Fundamental of	Gun, A.M., Gupta,	World Press, Kolkata	Vol I,2013
	Statistics,	M.K. and		
		Dasgupta, B.		
2	Mathematics of Statistics. Part II.	Kenney, J.F. and Keeping, E.S.	Chapman & Hall.	2nd Edition.1951
3	Introduction to the Theory of Statistics,	Mood, A.M. Graybill, F.A. and Boes, D.C.	Tata McGraw-Hill Pub. Co. Ltd.	3rd Edn.2011.



#### **Curriculum Development Team**

- 1. Dr.Sudha Agrawal, HOD, Department of Mathematics.
- 2. Dr.Ekta Shrivastava, Assistant Professor, Department of Mathematics.
- 3. Mr. Neelkanth Napit, Assistant Professor, Department of Mathematics.
- 4. Mrs. Vandana Soni, Assistant Professor, Department of Mathematics.
- 5. Mr.Radhakrishna Shukla, Assistant Professor, Department of Mathematics.
- 6. Mr.Ghanhyam sen, Assistant Professor, Department of Mathematics.
- 7. Ms. Pushpa Kushwaha, Assistant Professor, Department of Mathematics.
- 8. Ms. Arpana Tripathi, Assistant Professor, Department of Mathematics.

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#### **Cos, POs and PSOs Mapping**

**Course Title: M.Sc. Mathematics** 

Course Code: 78MS405

**Course Title: ADVANCED MATHEMATICAL STATISTICS** 

	PO1	РО	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10	PO11	PO12	PSO 1	PSO	PSO 3	PSO
Course		2												2		4
Outcome	Adva	Pr	Research	Qua	Teachi	Theo	Comm	Operat	Applica	Engine	Gover	Cons	Understa	Hand	Develop	Crea
Outcome	nced	ob	Abilities	ntita	ng and	retic	unicati	ions	tion in	ering	nment	ulting	nd the	le	necessar	tes
	Mat	le		tive	Acade	al	on	Resear	Industr	and	and		mathem	the	y skills	Mat
	hem	m-		Anal	mia	Und	Skills	ch	У	Techno	Public		atical	adva	and	hem
	atica	sol		ysis		ersta				logy	Sector		concepts	nced	expertise	atic
	1	vin				ndin							and	tech	in the	al
	Kno	g				g							applicati	niqu	field of	Mod
	wled	Ski											ons in	es	research	els
	ge	lls											the field			
													of			
													algebra			
CO1-	2	3	1	2	1	2	2	2	1	1	1	1	<u>2</u>	<u>1</u>	<u>1</u>	2
78MS405.1																
Learn the																
statistical																
methods to																
describe the																
central or																
typical value in																
a set of data to																
have clear																
understanding																
of the concept of central																
tendency and											1					



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its importance in summarizing data.																
CO2- 78MS405.2. To understand the concepts in probability theory and the probability distributions associated with various random variables foundational knowledge and skills.	1	3	2	1	1	1	1	1	1	2	3	1	3	1	1	1
CO3- 78MS405.3 Theory of Estimators typically covers the mathematical foundations and principles behind statistical estimation to develop a clear understanding of the fundamental concepts of statistical estimation, including point estimation and interval estimation.	1	3	2	2	1	1	3	2	1	1	3	1	2	1	2	
CO4- 78MS405.4 To understanding and applying exact methods for generating and studying sampling distributions, Learn and apply exact sampling methods, which may include	2	3	2	2	1	1	3	2	1	1	3	1	2	1	2	2



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techniques																
such as Monte																
Carlo																
simulation,																
bootstrapping,																
permutation																
tests, or other																
re-sampling																
methods.																
CO5-	2	3	2	2	1	1	3	2	1	1	3	1	<u>2</u>	<u>1</u>	<u>2</u>	2
78MS405.5																
Analysis of																
Variance																
(ANOVA)																
typically covers																
the statistical																
methods used																
to analyze																
differences																
among group																
means in a																
dataset to																
develop a solid																
understanding																
of the																
fundamental																
concepts of																
Analysis of																
Variance,																
including the																
partitioning of																
variance and																
the comparison																
of group means																

Legend: 1 – Low, 2 – Medium, 3 – High



### **Course Curriculum Map:**

POs & PSOs No.	COs No.& Titles	SOs No.	Laborato ry Instructi on(LI)	Classroom Instruction (CI)	Self Learning (SL)
PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2, 3, 4	CO1-78MS405.1 Learn the statistical methods to describe the central or typical value in a set of data to have clear understanding of the concept of central tendency and its importance in summarizing data.	SO1.1 SO1.2 SO1.3 SO1.4 SO1.5		Unit-1.0 1.1,1.2,1.3,1.4,1.5,1.6,1. 7,1.8,1.9,1.10,1.11,1.12	SL1.1 SL1.2
PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2, 3, 4	CO2- <b>78MS405</b> .2.To understand the concepts in probability theory and the probability distributions associated with various random variables foundational knowledge and skills.	SO1.1 SO1.2 SO1.3 SO1.4 SO1.5		Unit-2 2.1, 2.2, 2.3, 2.4, 2.5, 2.6, 2.7, 2.8,2.9,2.10 2.11,2.12	SL2.1 SL2.2
PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2, 3, 4	CO3-78MS405.3. Theory of Estimators typically covers the mathematical foundations and principles behind statistical estimation to develop a clear understanding of the fundamental concepts of statistical estimation, including point estimation and interval estimation.	SO1.1 SO1.2 SO1.3 SO1.4 SO1.5		Unit-3 3.1, 3.2, 3.3, 3.4, 3.5, 3.6, 3.7,3.8,3.9,3.10,3.11, 3.12	SL3.1
PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2, 3, 4	CO4-78MS405.4 To understanding and applying exact methods for generating and studying sampling distributions, Learn and apply exact sampling methods, which may include techniques such as Monte Carlo simulation, bootstrapping, permutation tests, or other resampling methods.	SO1.1 SO1.2 SO1.3 SO1.4 SO1.5		Unit-4 4.1,4.2,4.3, 4.4, 4.5, 4.6, 4.7, 4.8,4.9,4.10,4.11,4.12	SL4.1
PO 1,2,3,4,5,6 7,8,9,10,11,12 PSO 1,2, 3, 4	CO5-78MS405.5 Analysis of Variance (ANOVA) typically covers the statistical methods used to analyze differences among group means in a dataset to develop a solid understanding of the fundamental concepts of Analysis of Variance, including the partitioning of variance and the comparison of group means.	SO1.1 SO1.2 SO1.3 SO1.4 SO1.5		Unit-5 5.1, 5.2, 5.3, 54, 55, 56, 57, 58,5.9,5.10,5.11,5.12	SL5.1

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